

# GEARING UP TO CLOSE THE BOOK ON WIMP DM

ROBERTO FRANCESCHINI

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INCLUDING WORKS WITH SALVATORE **BOTTARO**, MARCO **COSTA**, LUDOVICO **VITTORIO**, XIAORAN ZHAO AND DARIO BUTTAZZO, PAOLO PANCI, DIEGO REDIGOLO

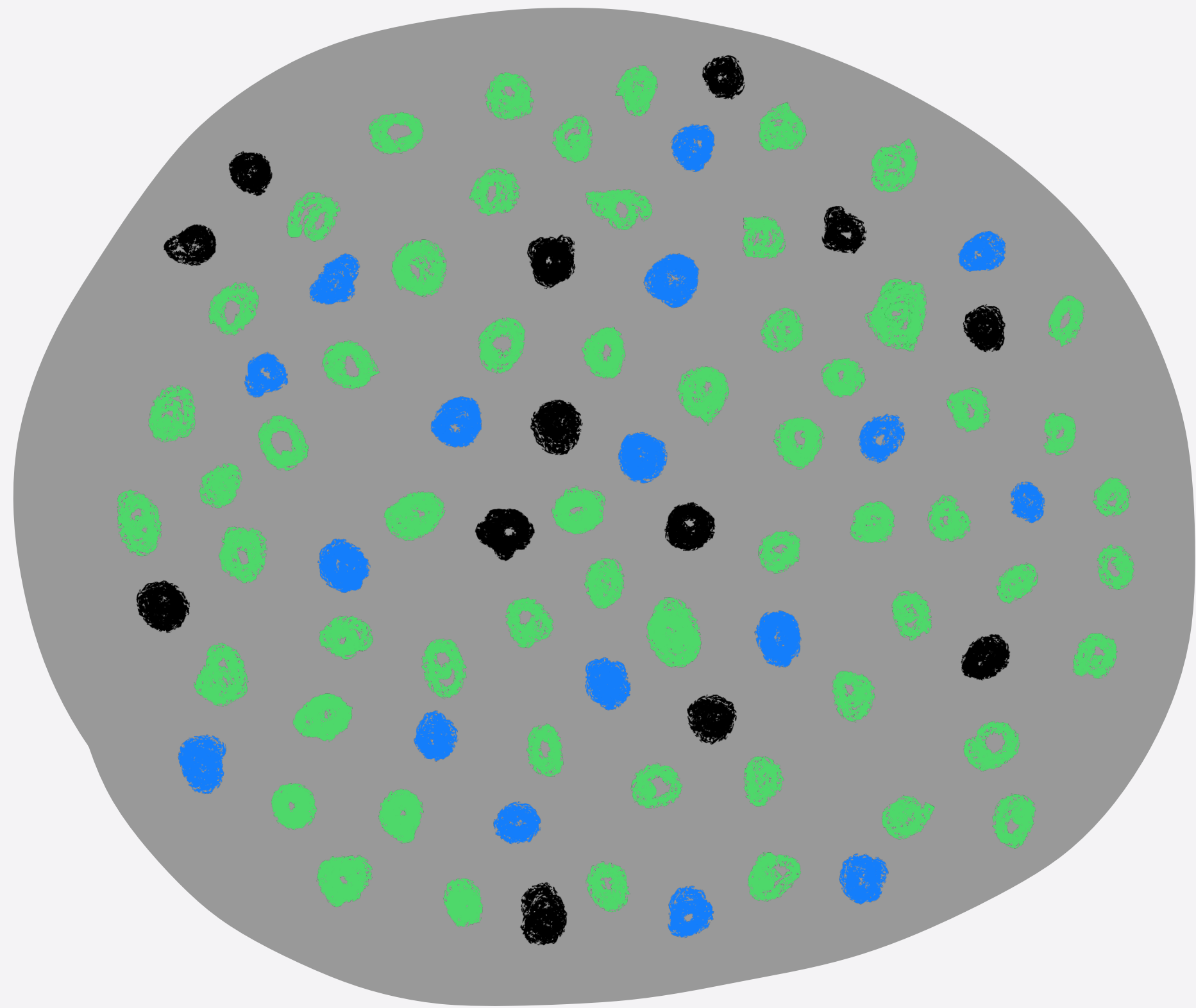
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# INTRO



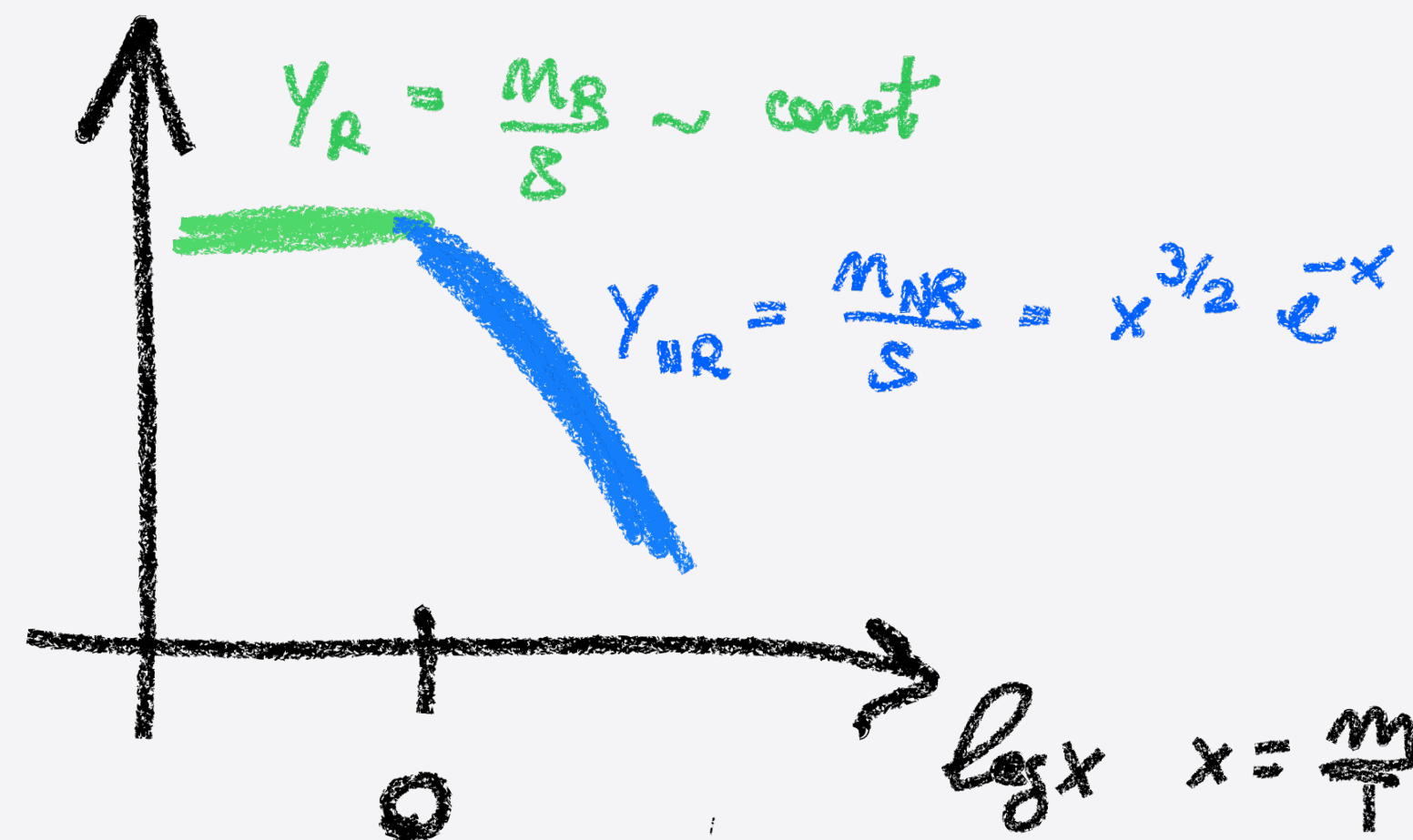
# A SIMPLEST EXPLANATION FOR ITS PRODUCTION



- SM RELATIVISTIC
- DARK MATTER
- SM NON-RELATIVISTIC

Following equilibrium thermodynamics the number density of a specie can be predicted at all times it is in equilibrium. Once it drops out from equilibrium  $Y$  freezes out and the relic density is fixed.

$$\log \left( \frac{N(m/x)}{N(\infty)} \right)$$



$$\frac{dY}{dx} = \frac{-x \langle \sigma_a v \rangle s}{H/w} (y^2 - y_{eq}^2)$$

$$= \# m M_{pl} \bar{\sigma}_0 x^{-k-2}$$

$$Y_\infty = \# \frac{(x_f)^{k+1}}{M_{pl} m \bar{\sigma}_0} \sim \# \frac{m}{M_{pl}} (x_f)^{k+1}$$

# THE WIMP "CATALOG"

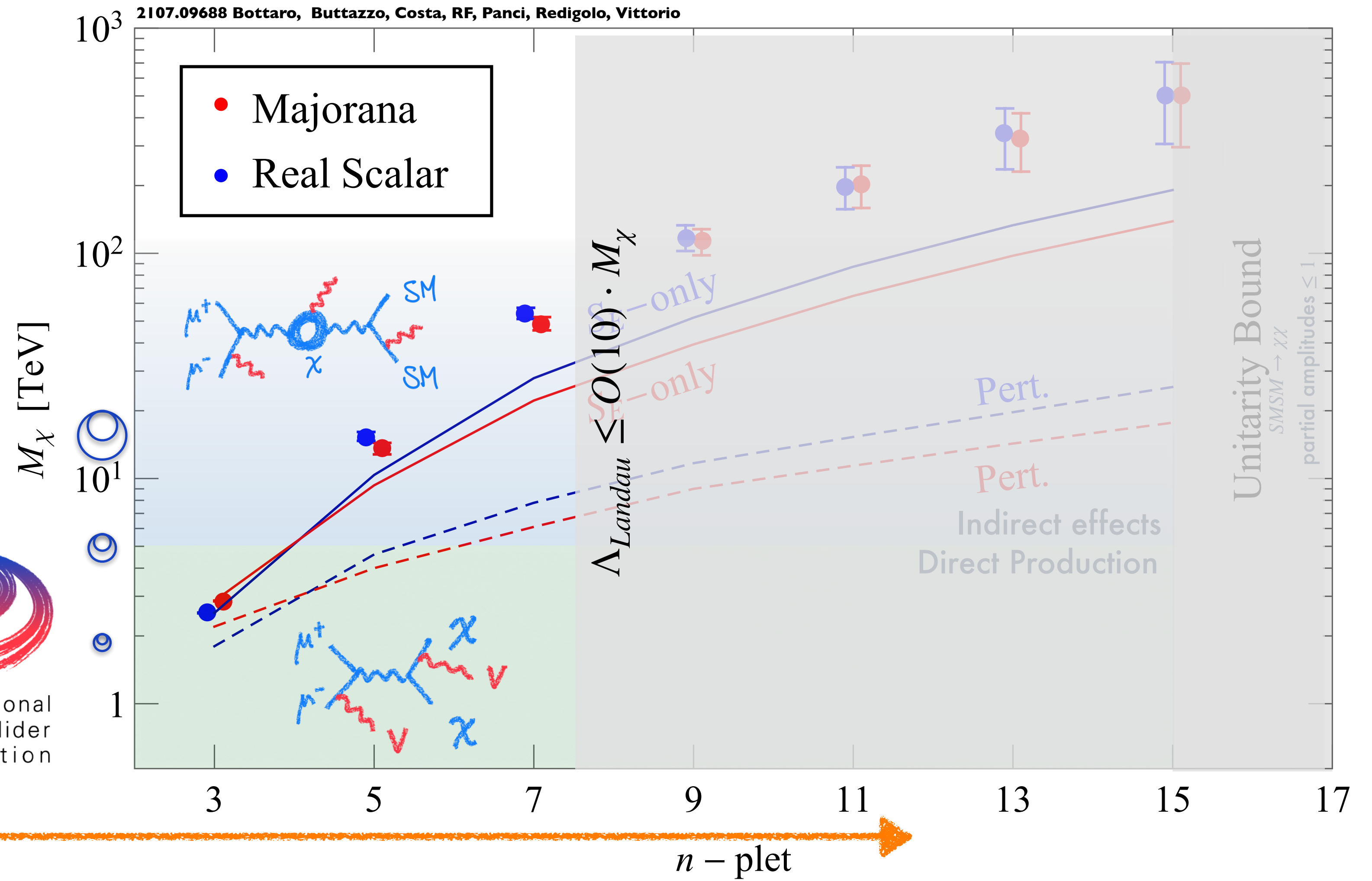
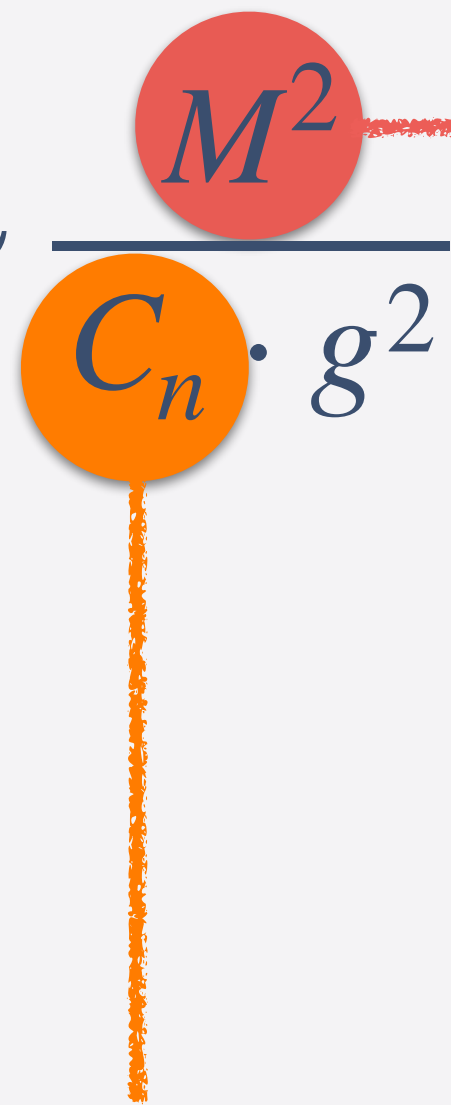
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$$\Omega_{nr} \sim \frac{1}{\sigma_{ann}} \sim \frac{M^2}{C_n \cdot g^2}$$

mass of the DM



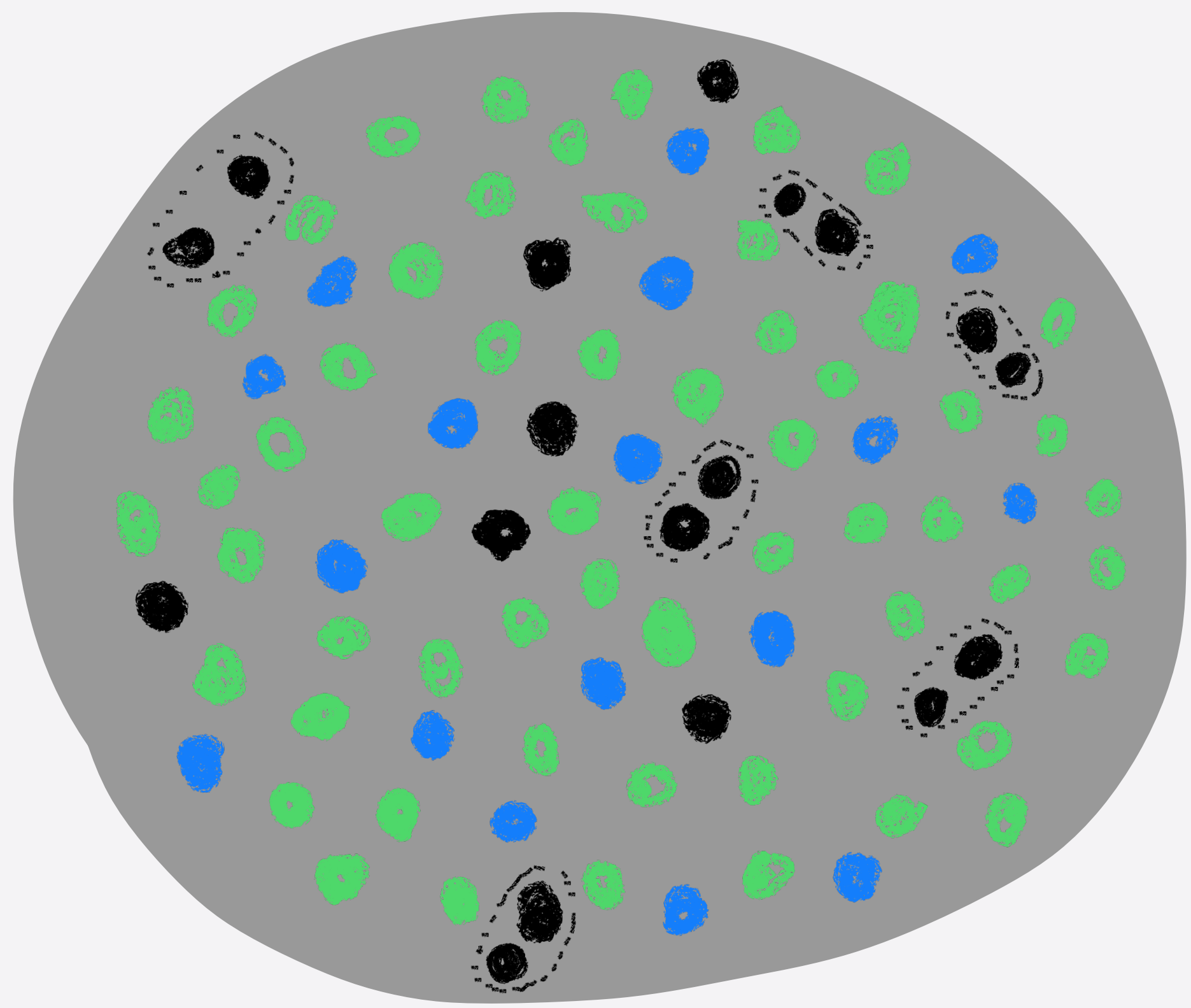
weak charge of the DM



WIMPs are clearly "muon collider material"



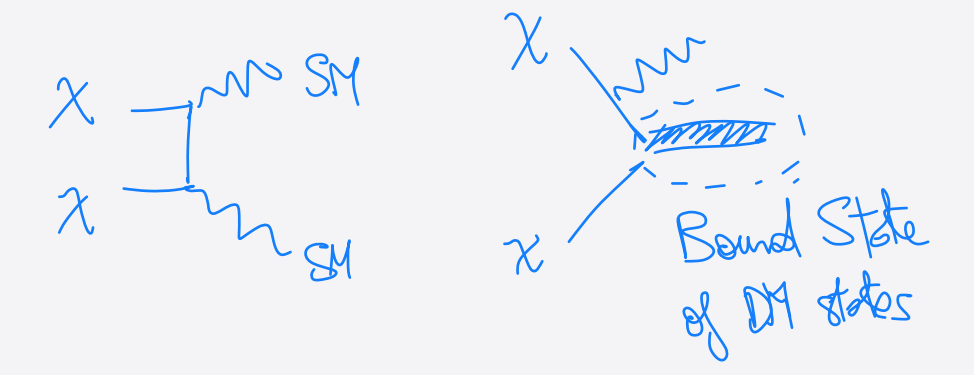
# A STILL SIMPLE EXPLANATION FOR ITS PRODUCTION



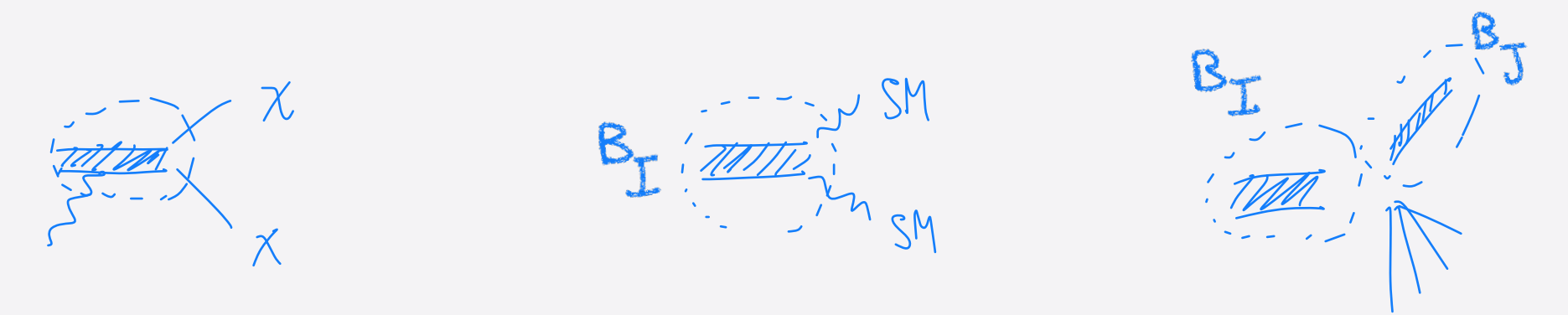
- SM RELATIVISTIC
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- DARK MATTER BOUND STATES

Following equilibrium thermodynamics the number density of a specie can be predicted at all times it is in equilibrium. Once it drops out from equilibrium  $Y$  freezes out and the relic density is fixed.

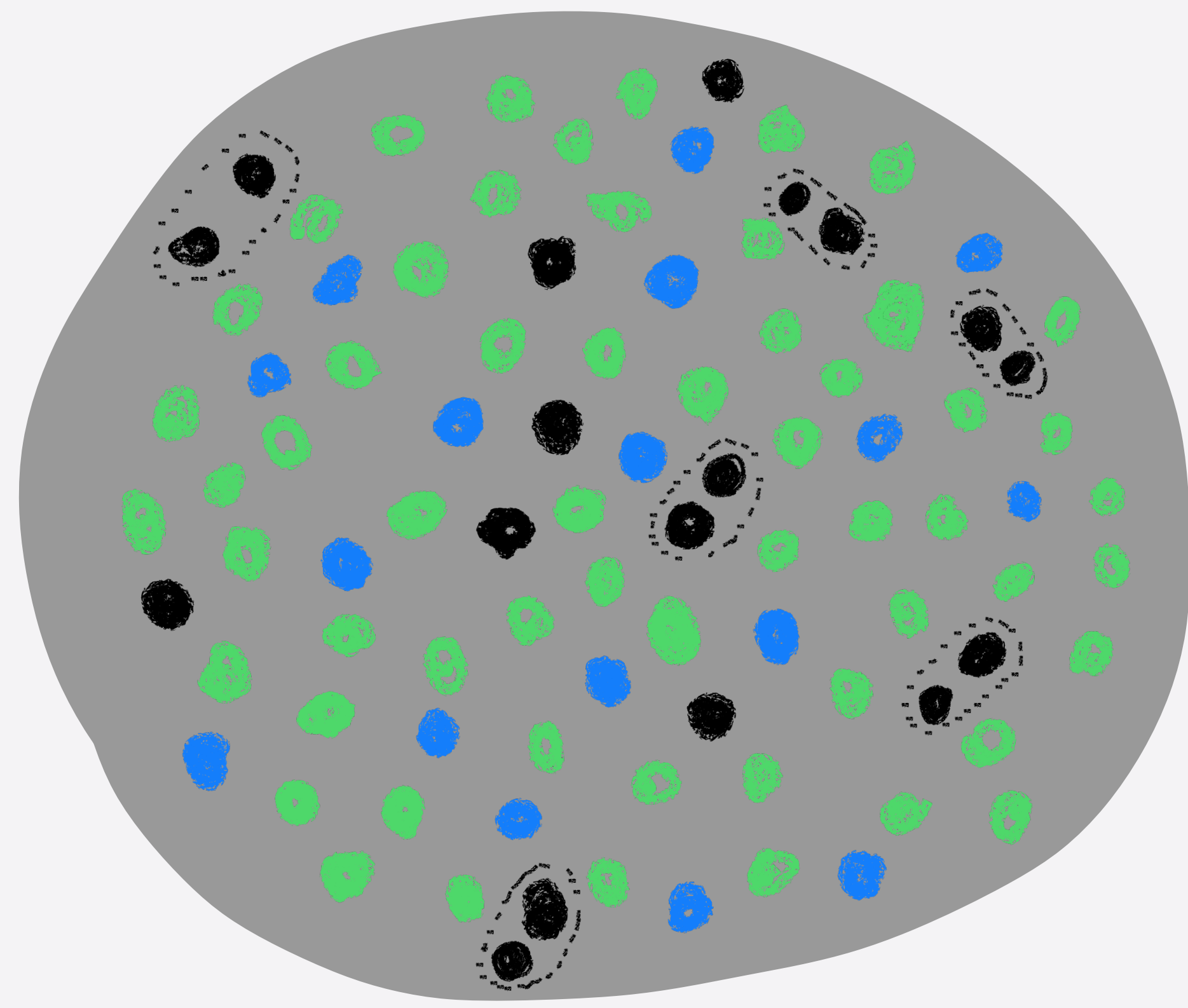
$$z \approx H(T) \frac{dY}{dx} = -\gamma \left( \frac{Y_{DM}^2}{Y_{eq}^2} - 1 \right) - \sum \gamma_i \left( \frac{Y_{SM}^2}{Y_{eq}^2} - \frac{Y_i}{Y_{eq}} \right)$$



$$s z H \frac{dY_{B_I}}{dx} = \Gamma_{B_I, \text{break}} \left( \frac{Y_{DM}^2}{Y_{eq}^2} - \frac{Y_{B_I}}{Y_{B_I}^{eq}} \right) + \Gamma_{B_I, \text{ann}} \left( 1 - \frac{Y_{B_I}}{Y_{B_I}^{eq}} \right) + \sum \Gamma_{I,J} \left( \frac{Y_{B_I}}{Y_{B_I}^{eq}} - \frac{Y_{B_J}}{Y_{B_J}^{eq}} \right)$$



# A STILL SIMPLE EXPLANATION FOR ITS PRODUCTION

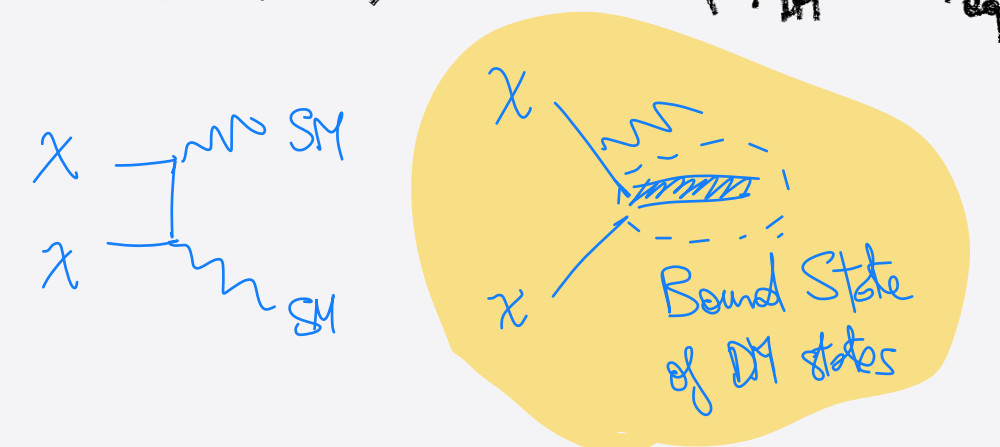


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 DARK MATTER BOUND STATES

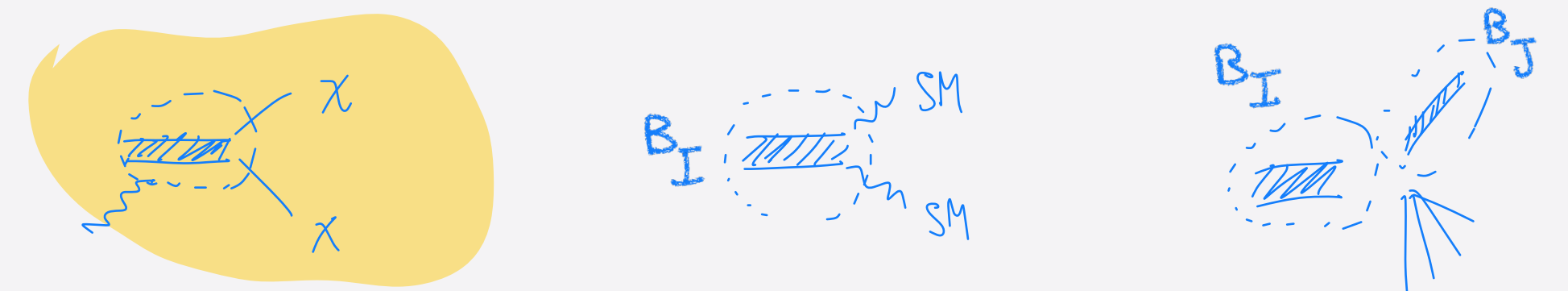
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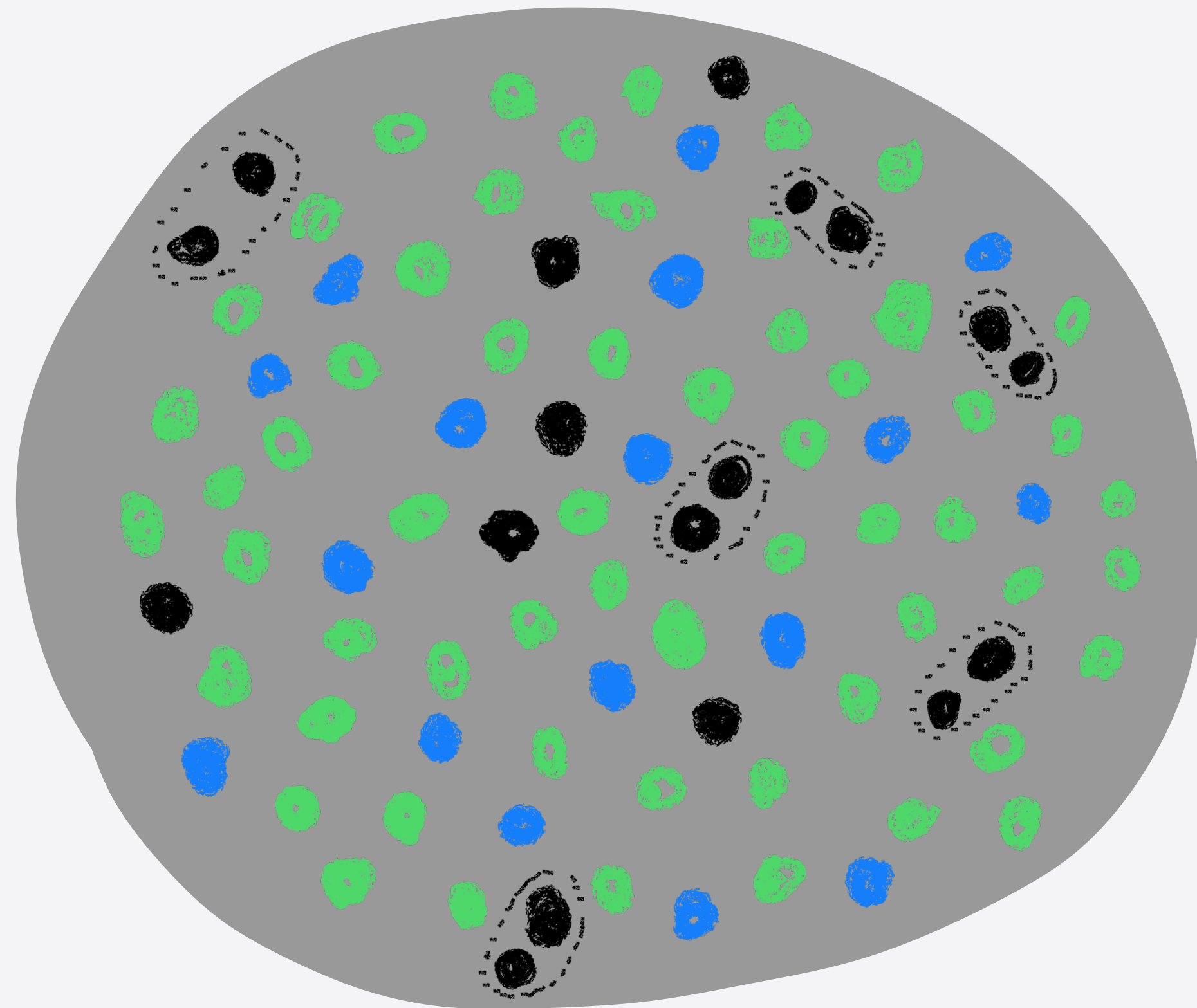
$H \ll \Gamma$

$$s z H \frac{dY_{B_I}}{dx} \Rightarrow \Gamma_{B_I, \text{break}} \left( \frac{Y_{DM}^2}{Y_{eq}^2} - \frac{Y_{B_I}}{Y_{B_I}^{eq}} \right) + \Gamma_{B_I, \text{ann}} \left( 1 - \frac{Y_{B_I}}{Y_{B_I}^{eq}} \right) + \sum \Gamma_{I,J} \left( \frac{Y_{B_I} Y_{B_J}}{Y_{eq}^2} - \frac{Y_{B_I}}{Y_{eq}} \right)$$





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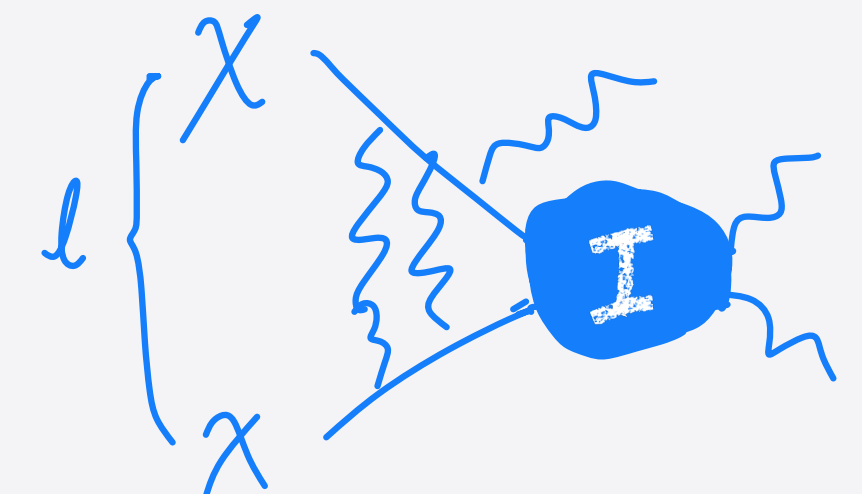
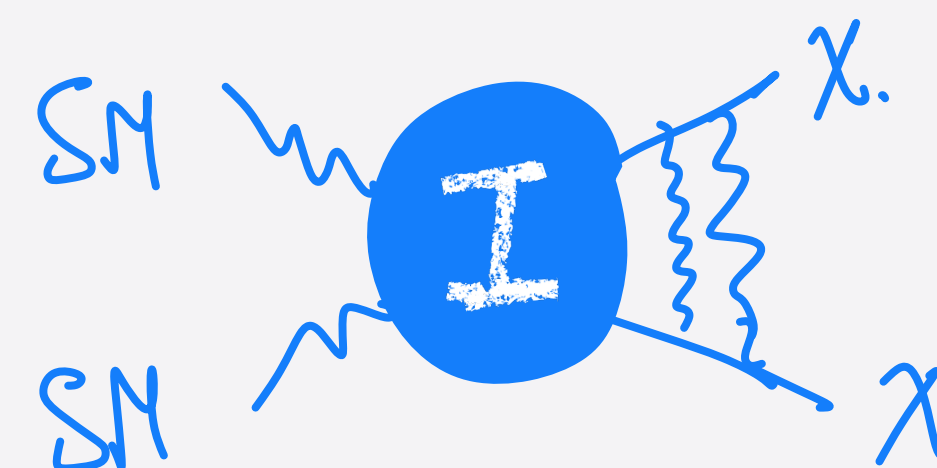
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DARK MATTER BOUND STATES

$$x H \frac{dY}{dx} = - \langle \sigma_{eff} v \rangle s (Y^2 - Y_{eq}^2)$$

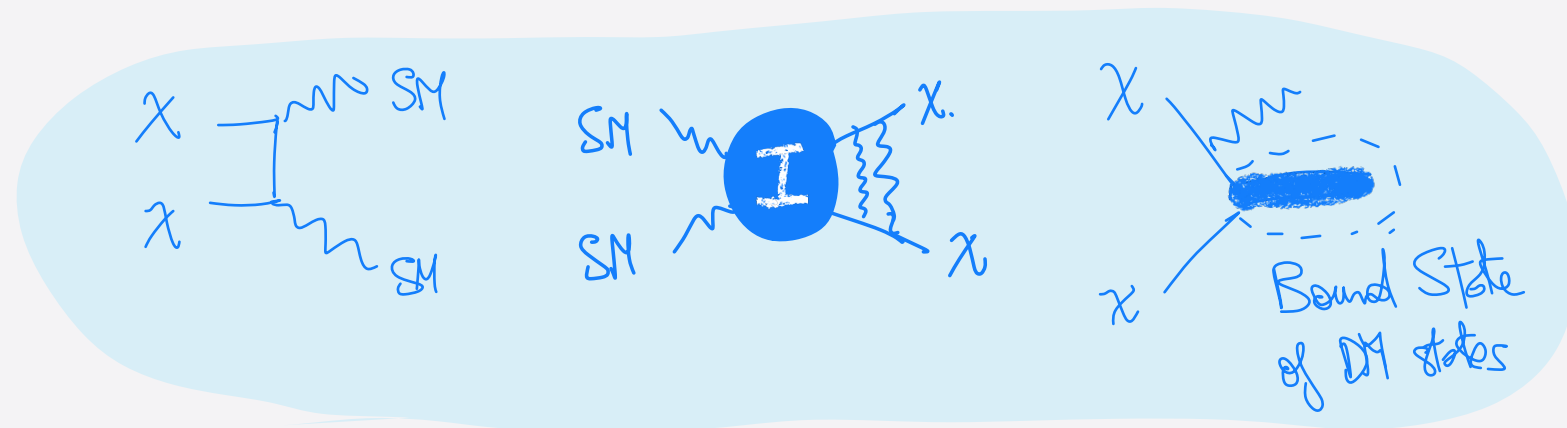
$$\langle \sigma_{eff} v_{rel} \rangle = \sum_I \langle S_E^{(I)} \tilde{\sigma}_{om}^{(I)} v_{rel} \rangle + \sum_{\mathcal{R}_I} \sum_{I, l} S_E^{(I)} S_{B_j}^{I, l} R_{B_j}$$



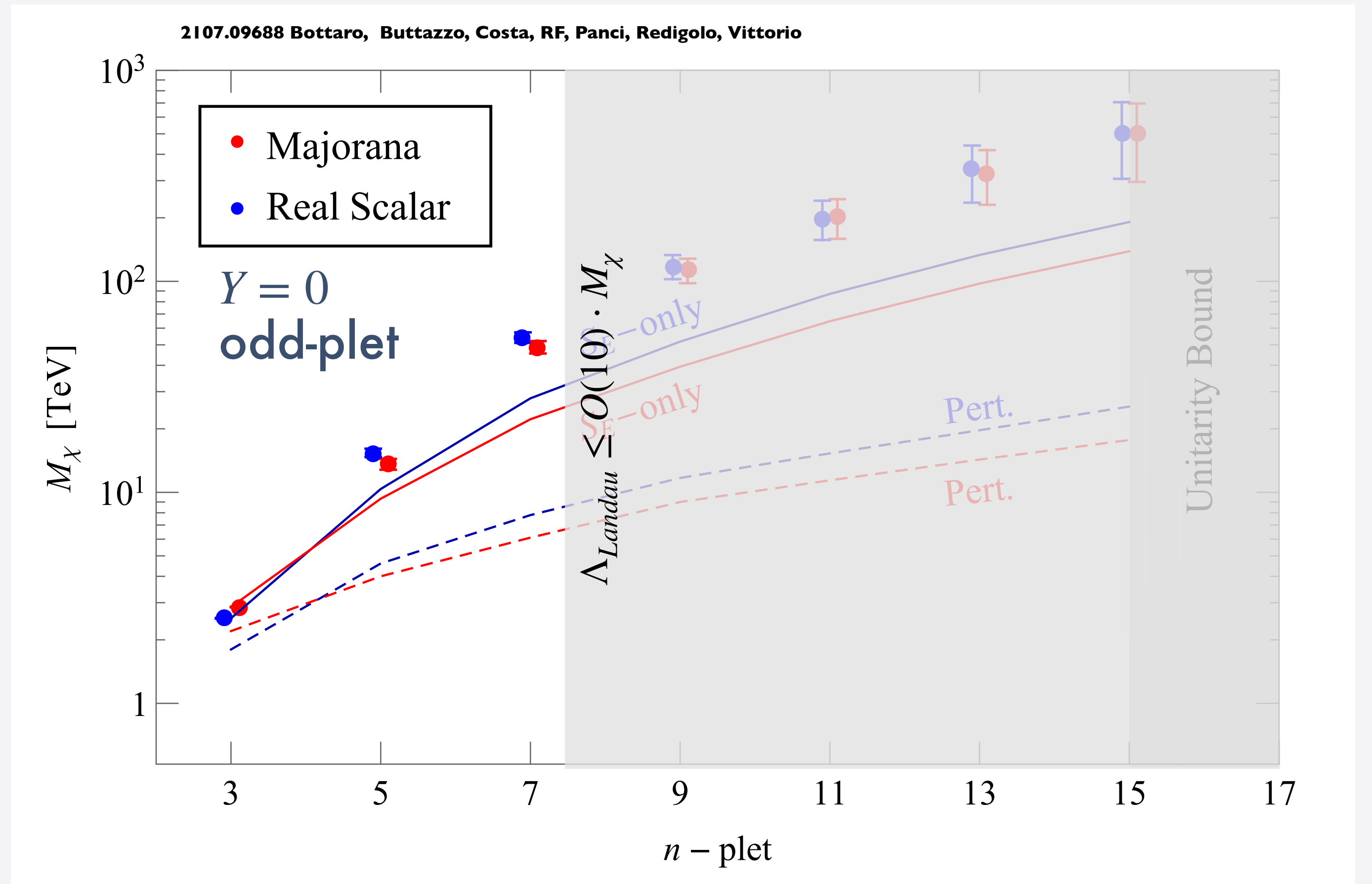
channel-by-channel Sommerfeld enhancement (resummation)

# AN "INTERPOLATOR" MODEL

$$\Omega_{nr} \sim \frac{1}{\sigma_{ann}} \sim \frac{M^2}{C_n \cdot g^2}$$



given  $n$  the mass is predicted  
understood as the maximal mass for that  $n$

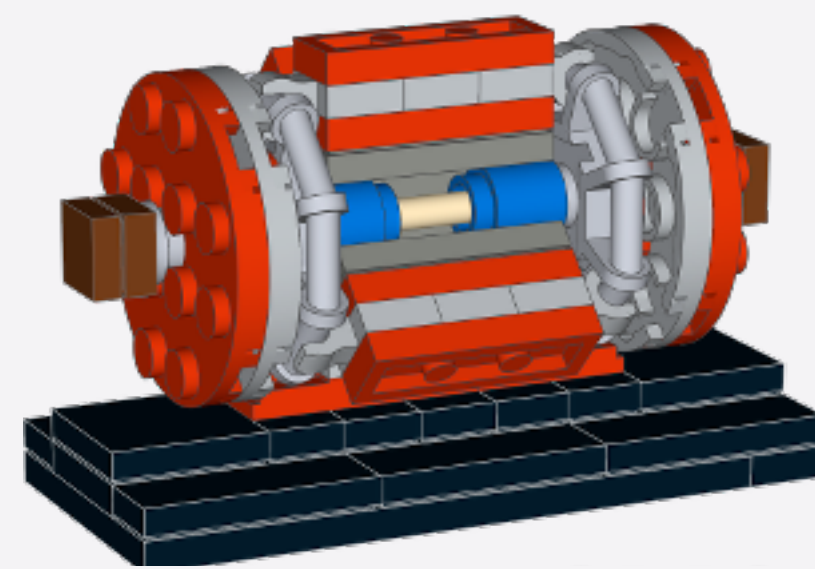


If Dark Matter feels SM weak interactions we can use the general  $n$ -plet WIMP to measure how well we are able to test this hypothesis and possibly discover or exclude one or several or the whole category of DM candidates.

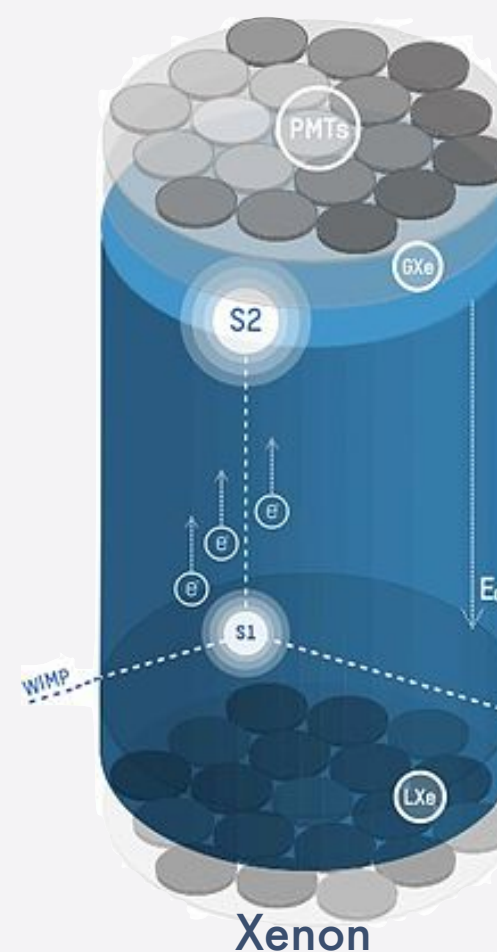
# AFTER DECADES OF WIMPs WE MIGHT START TO SEE THE END OF THE WAY (!)

## How to thoroughly test it?

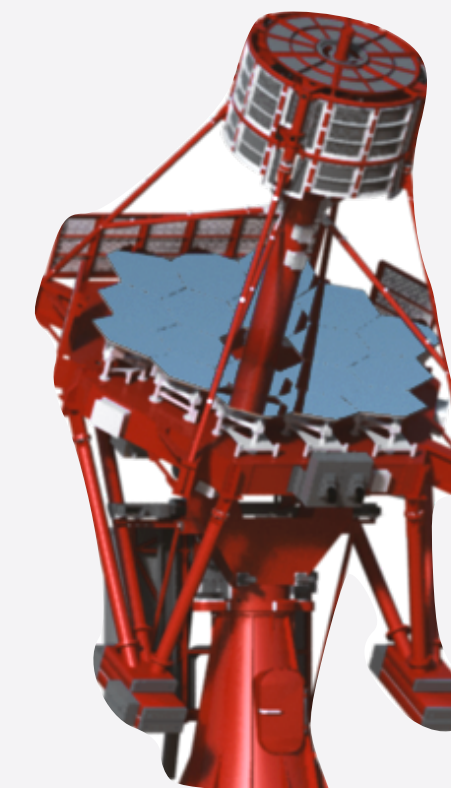
- Produce WIMPs in the lab
- Detect a WIMPs from natural source (big-bang)
- Observe WIMPs interactions (annihilation)
- Future Colliders sensitive to  $O(100)$  TeV
- Upcoming  $nT$  Xe detectors
- Upcoming Cosmic Rays observatories



Future Collider



Xenon

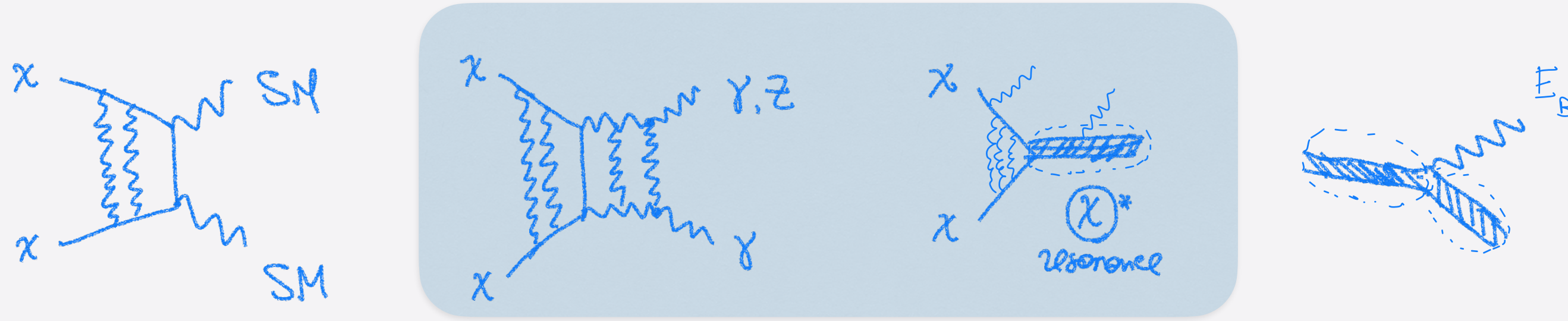


CTA



# INDIRECT DETECTION

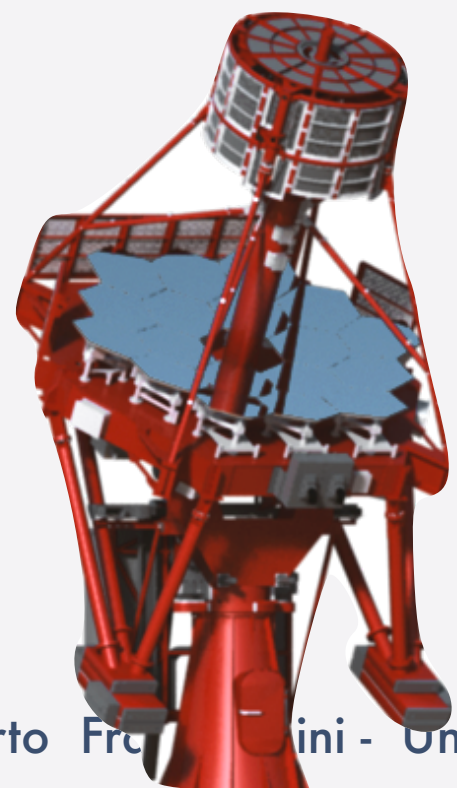
Thermal mass "lottery"



Annihilation in the astrophysical environment result in high-energy SM particle, which can be detector by cosmic rays observatories.

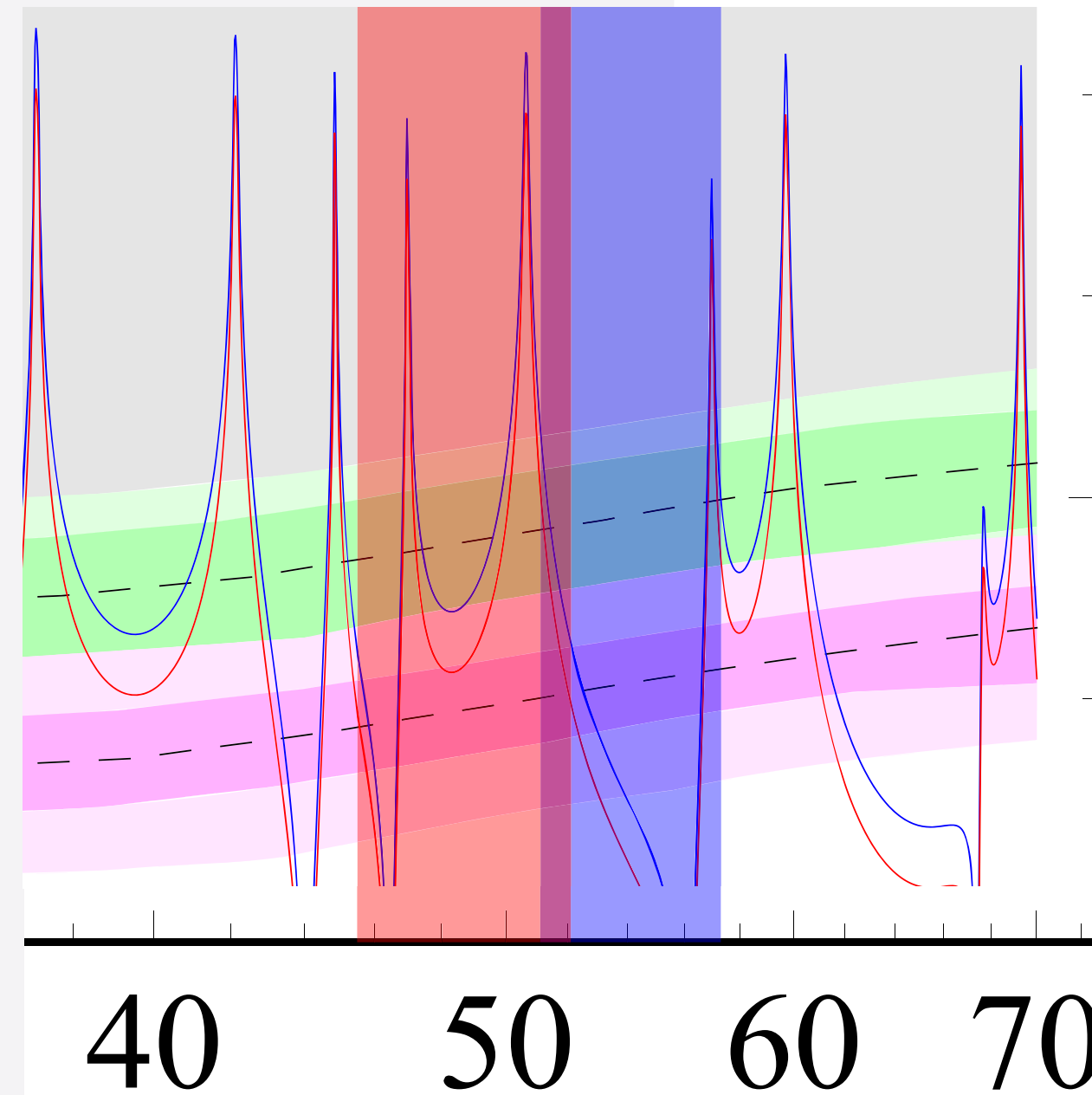
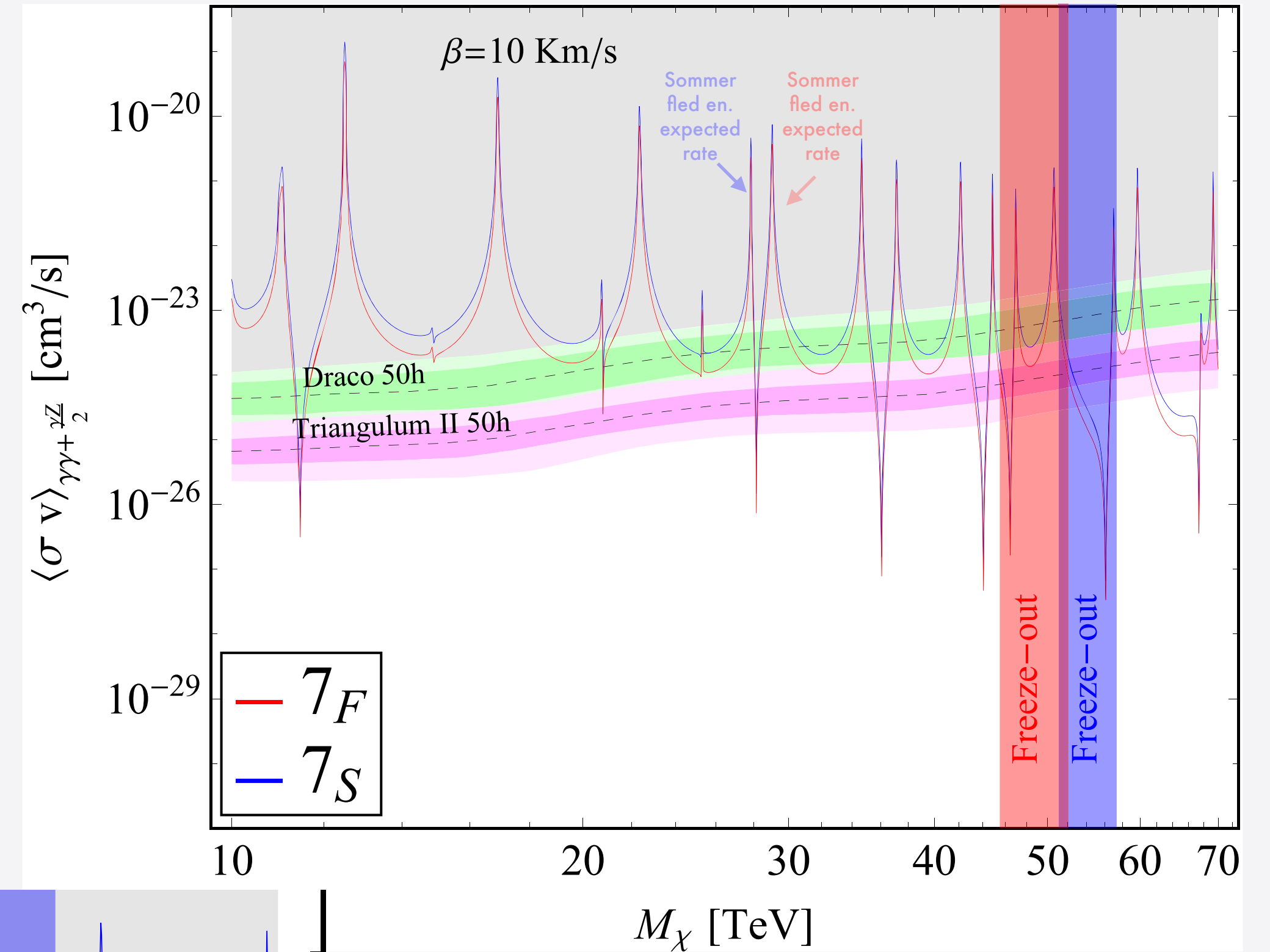
The signature depends on DM mass, possible resonant bound states formation and DM density profile

An excess on monochromatic multi-TeV photons would be quite convincing evidence of DM. The model can be even tested by the presence of multiple "lines" from bound states annihilations and lower energy de-excitation



## 2030s

up to 300 TeV,  $\frac{\Delta E}{E} \sim 10\%$

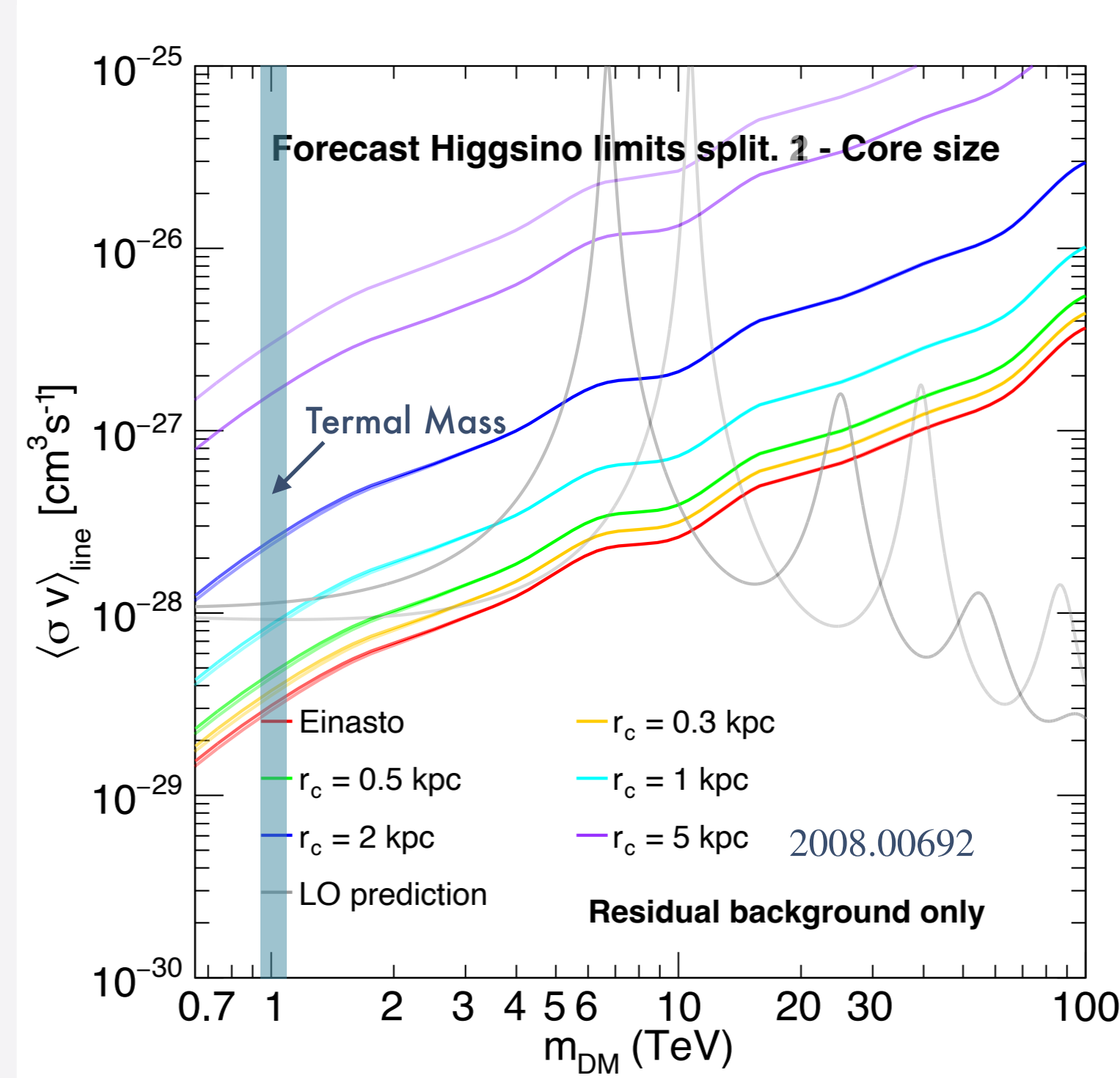
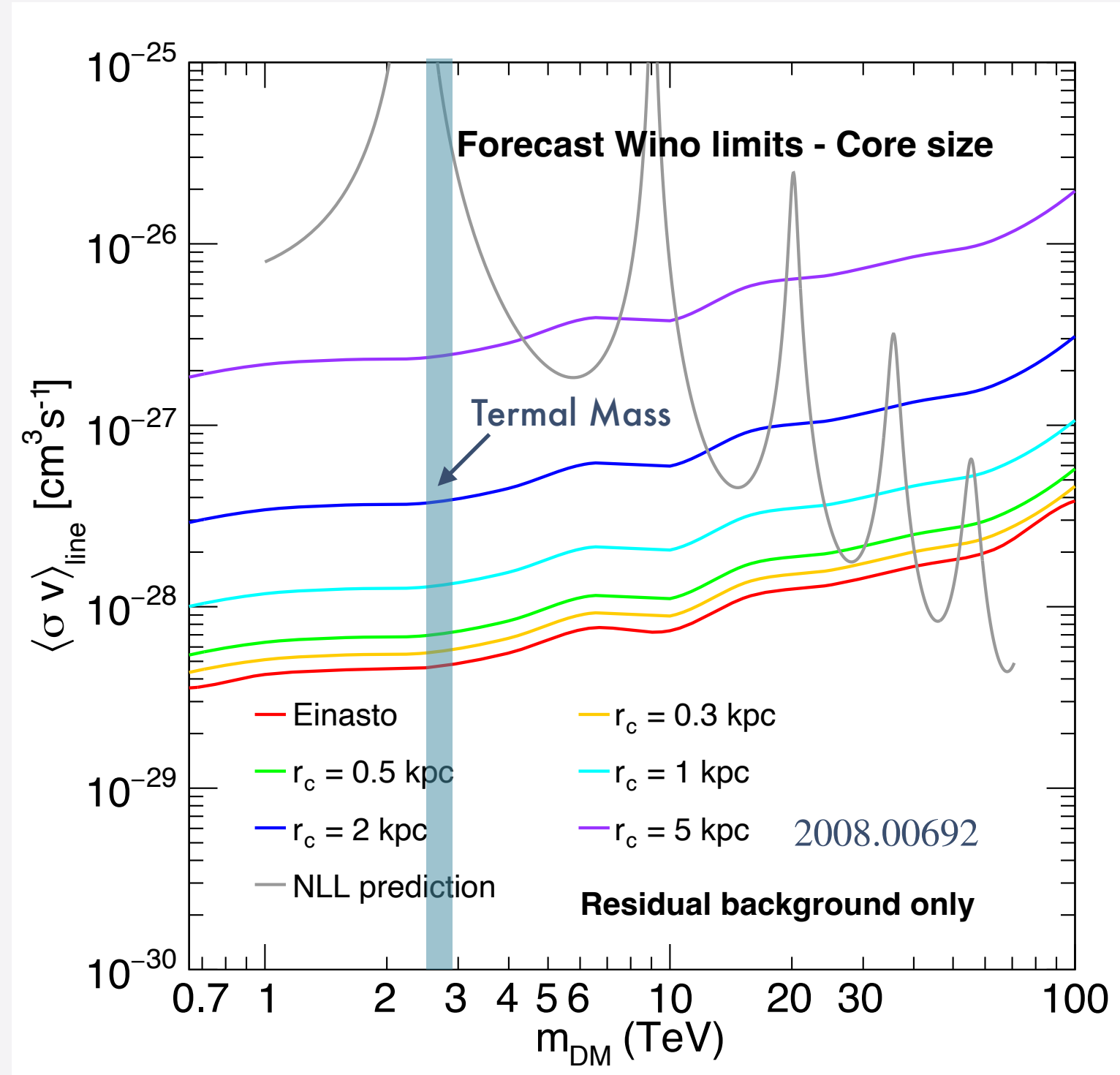


thermal mass "lottery": if the actual mass varies within the current theoretical uncertainty the signal strength changes by orders of magnitude!

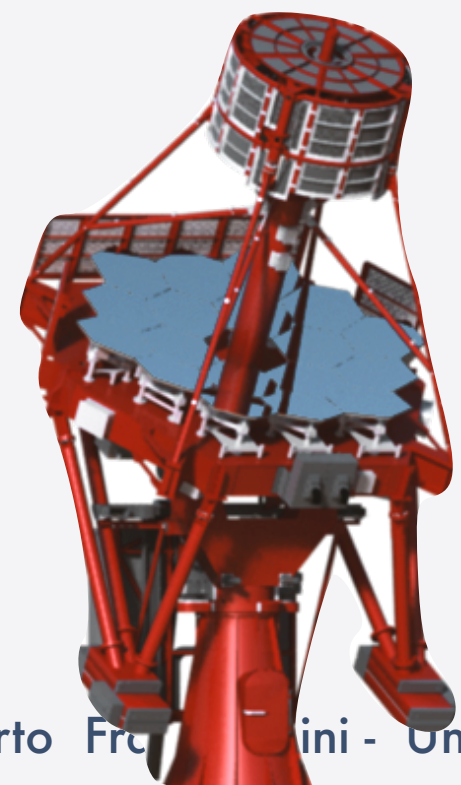
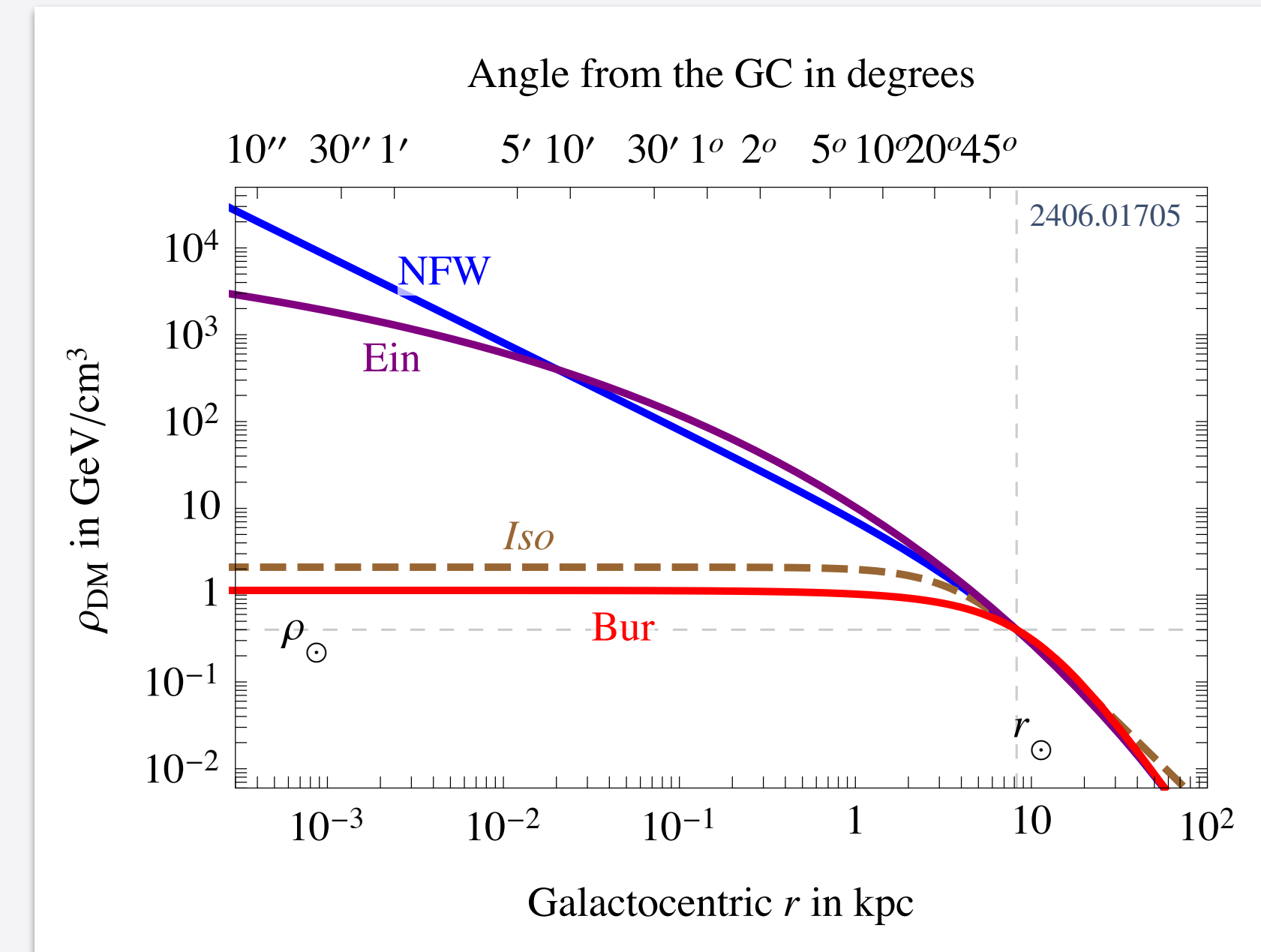


# INDIRECT DETECTION

Dark Mater profile "lottery"



For Milky-Way-sized galaxies, the core radius can be of order 1 kpc [79], or even larger; depending on the modeling of baryonic physics, cores extending to  $\sim 5$  kpc can potentially be obtained



## 2030s

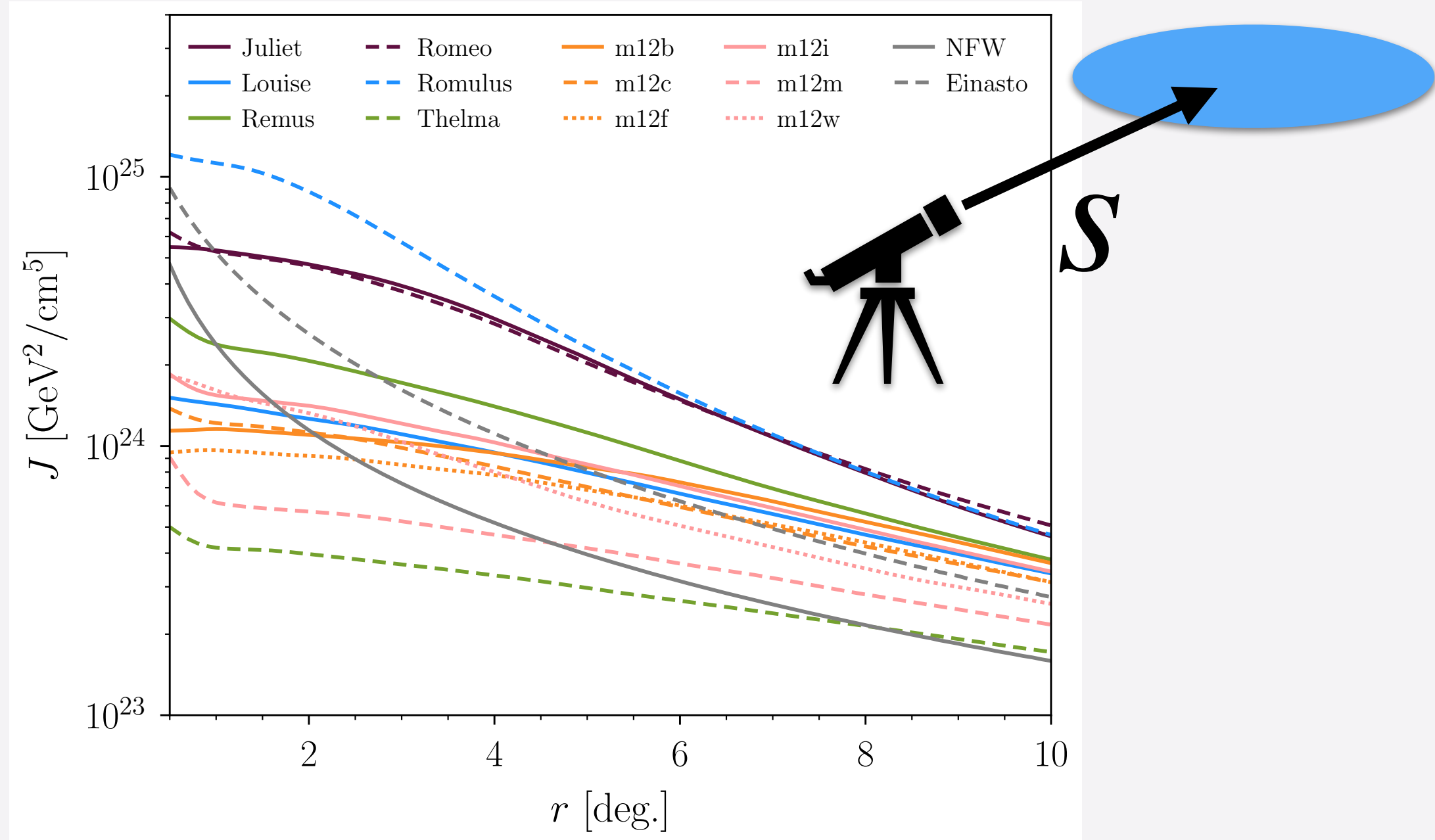
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Absence of a signal is hard to interpret, the host environment targeted by the indirect detection experiment may just not be rich enough in dark matter

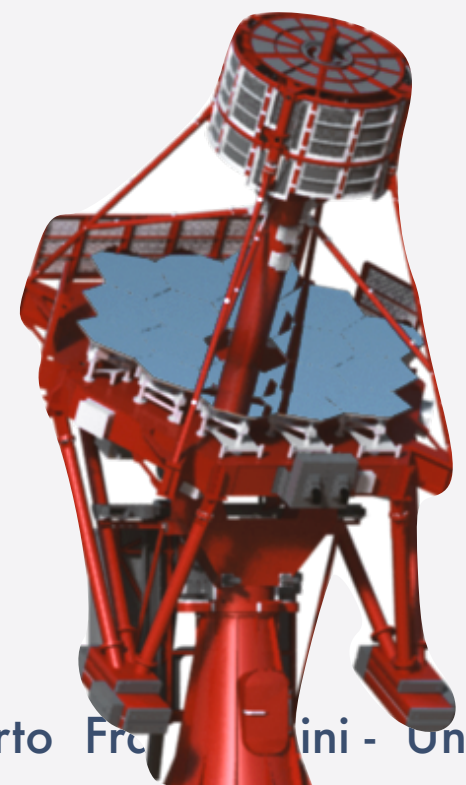
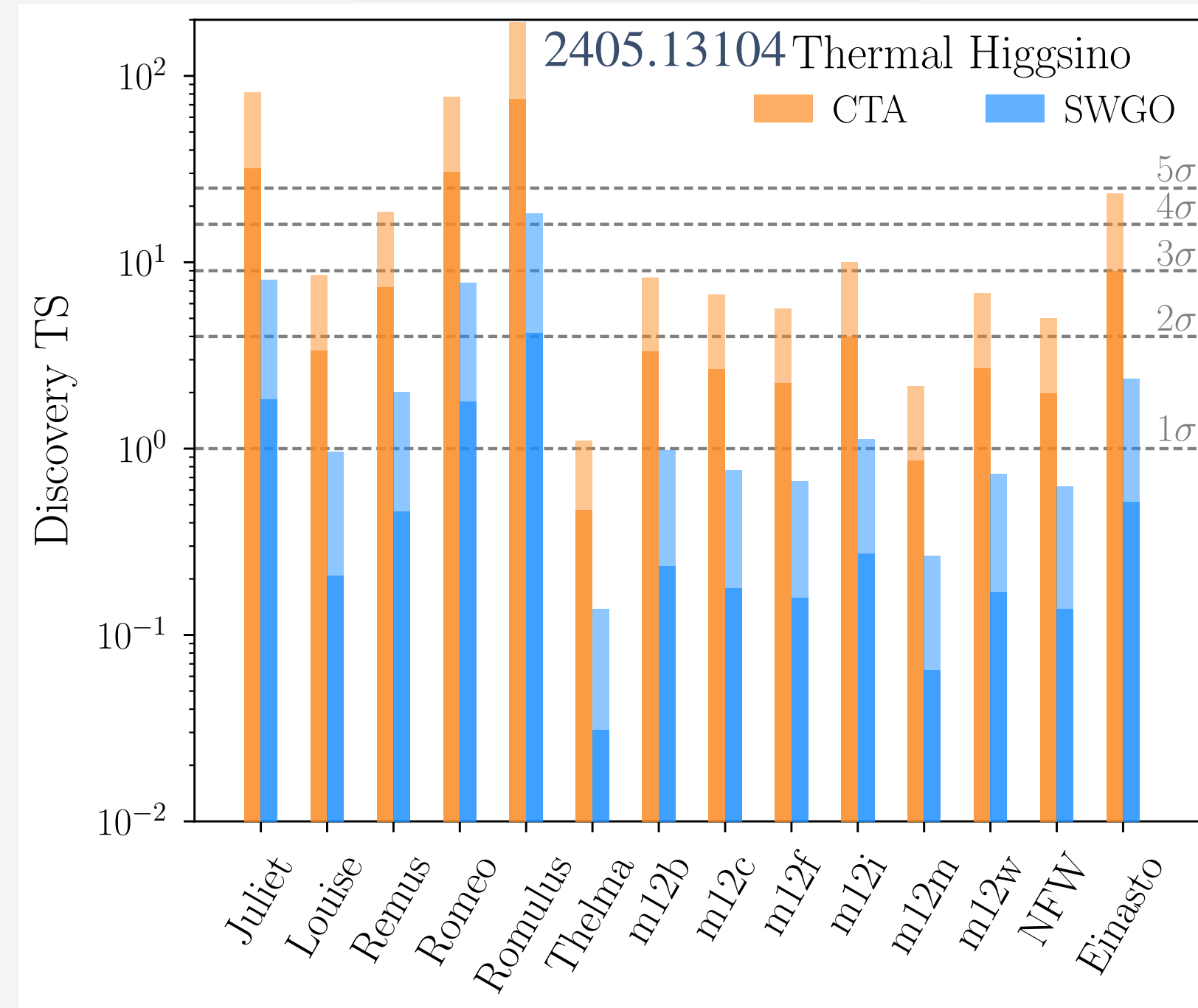
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$$J \equiv \int ds \rho_{\text{DM}}^2(s, \Omega),$$



## Milky Way analogs



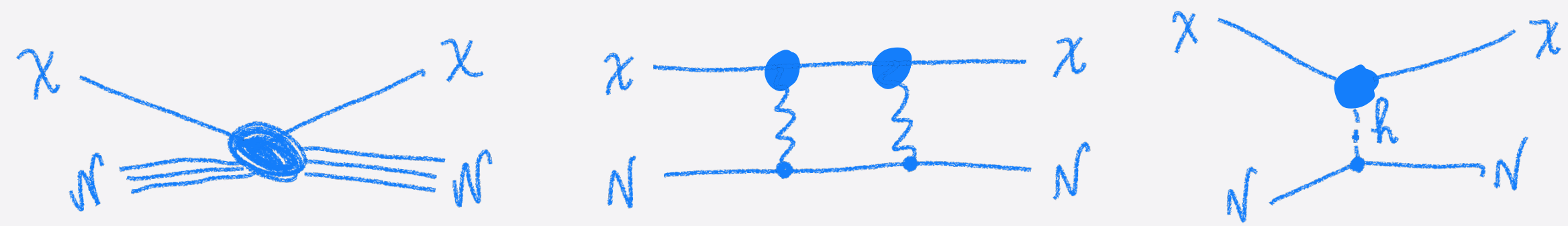
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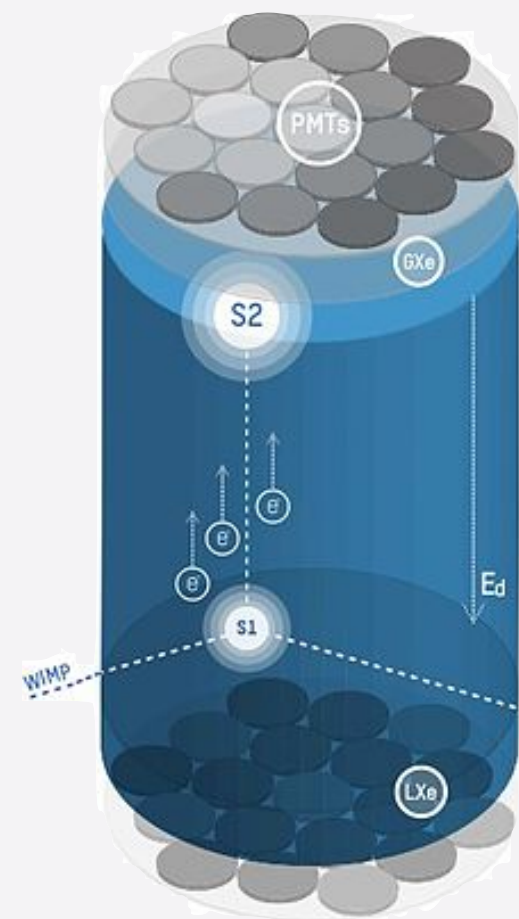
# DIRECT DETECTION



Scattering on SM materials can be detected in ultra-low background experiments

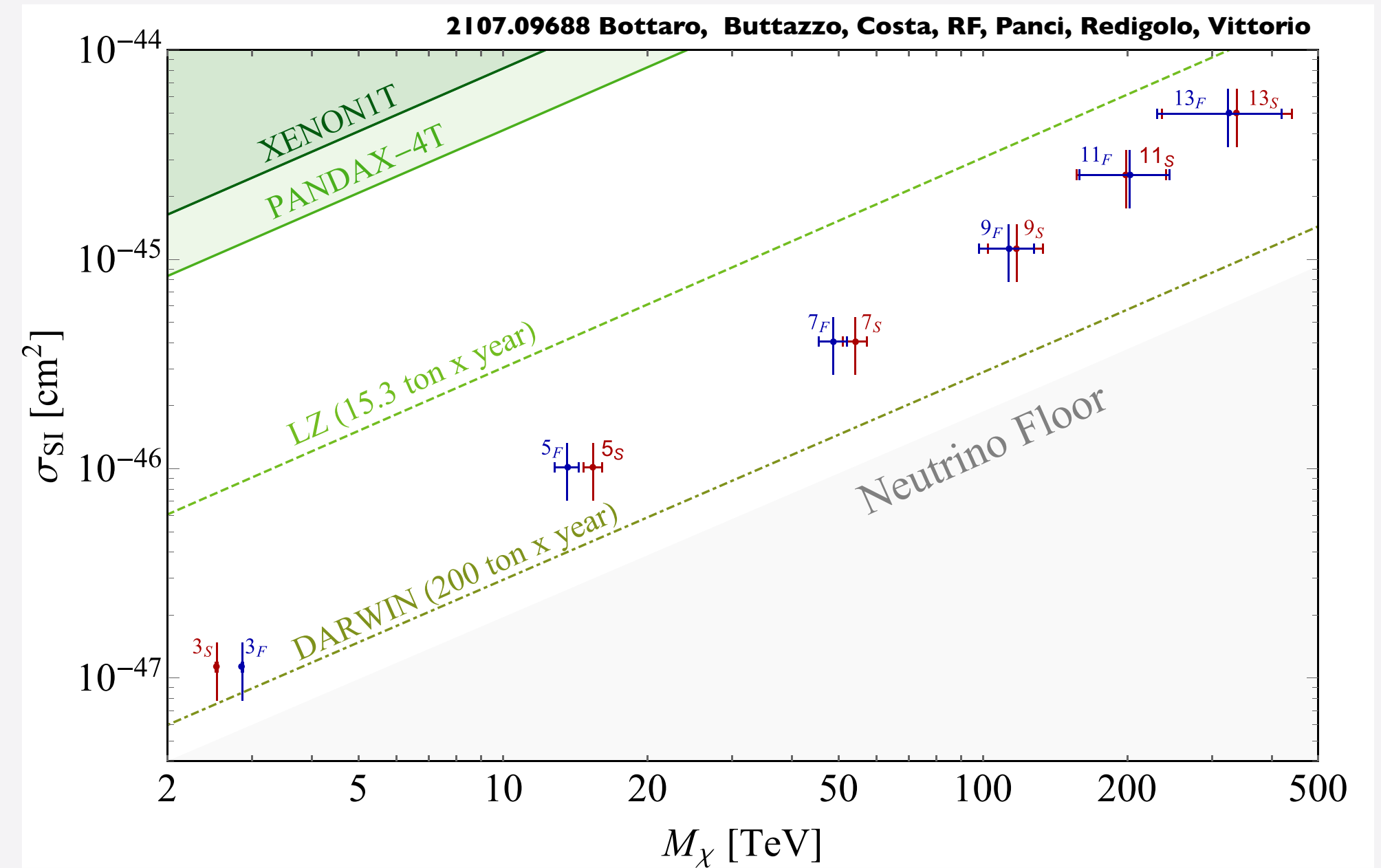
Larger rates for the larger  $n$ -plets keep them visible

For such large DM mass the signature does not depend on the DM mass.

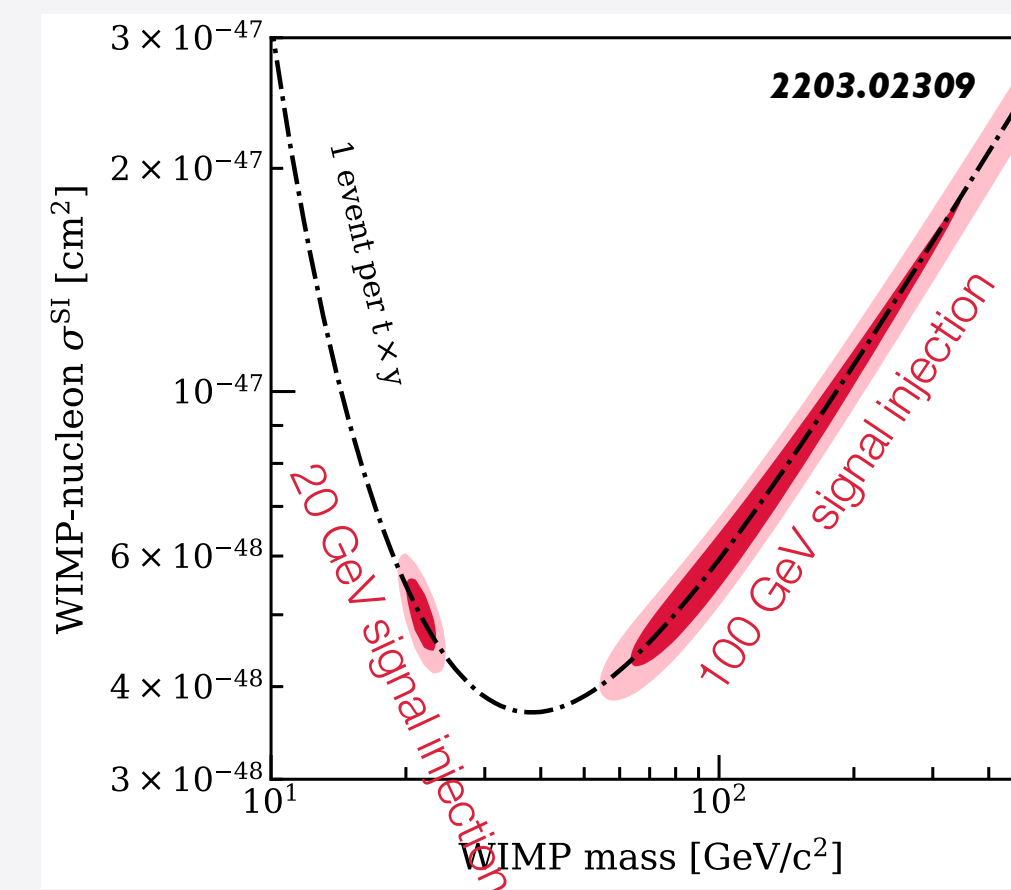


## 2030s

up to  $O(\text{PeV})$

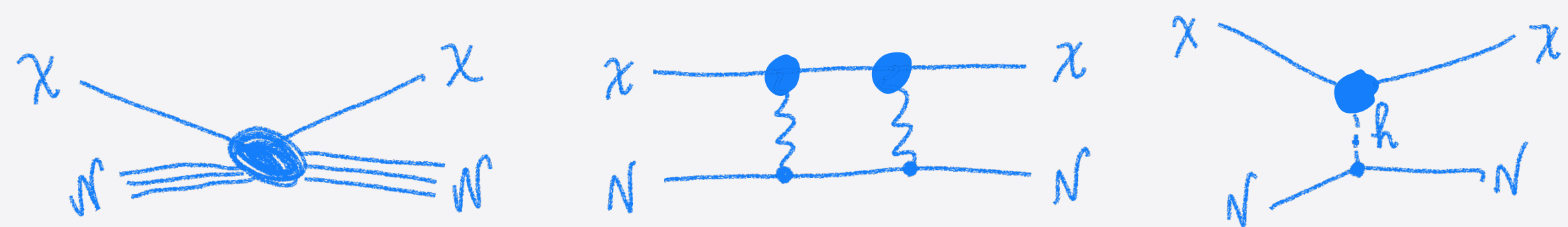


An excess would require a "seasonality" check and maybe independent confirmation (many excesses in the past in this type of experiments, though most were at the lowest accessible masses)



insensitive to  $\chi$  mass, urgent need for high-energy colliders

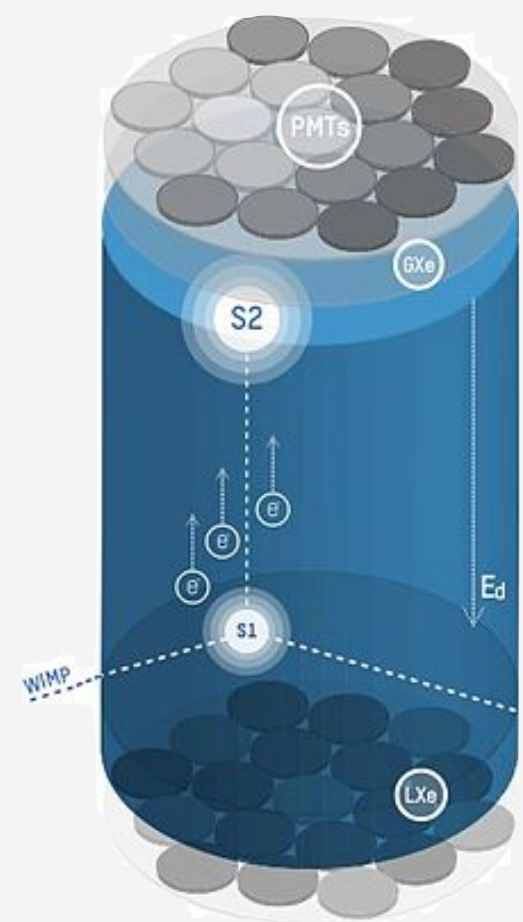
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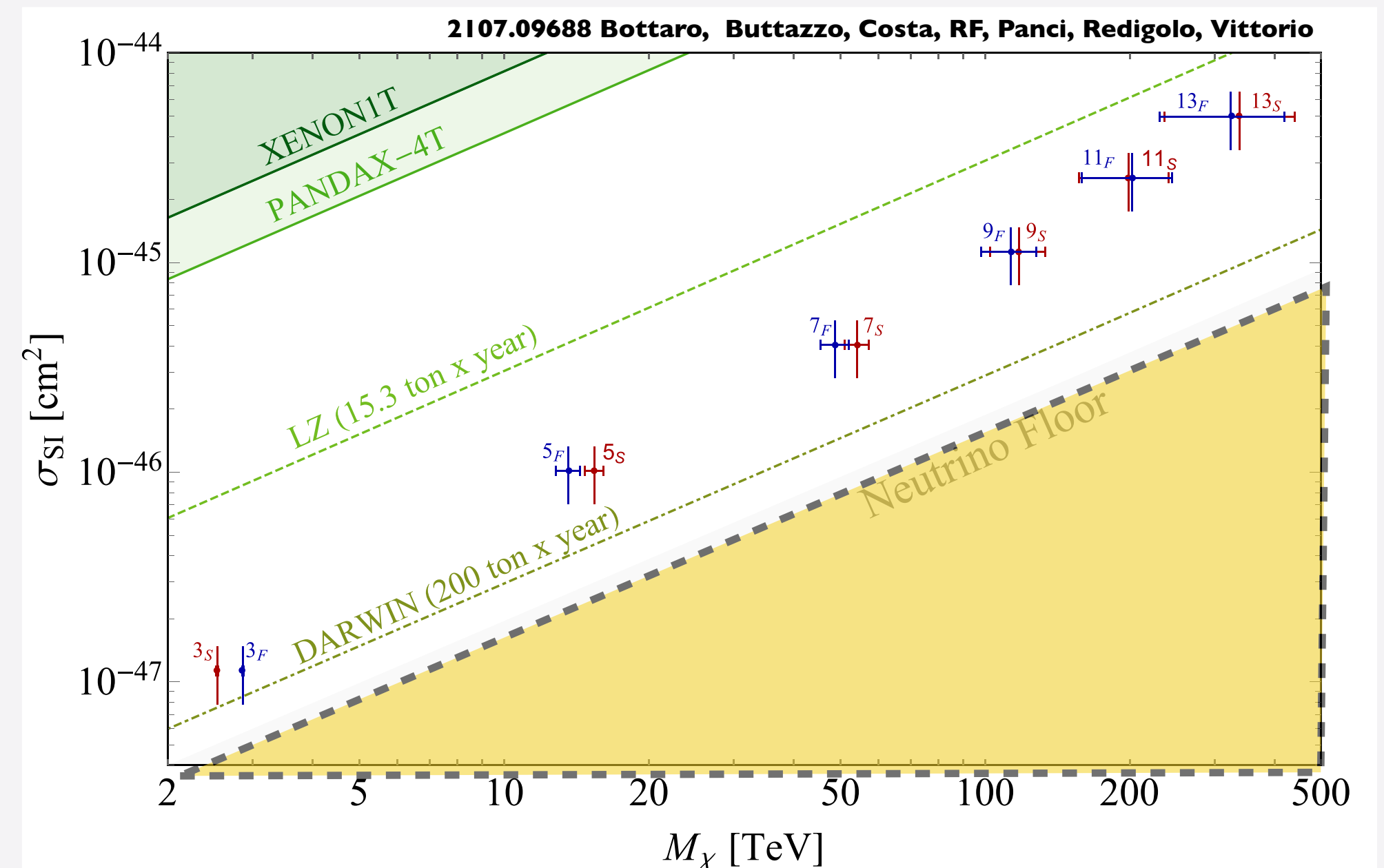
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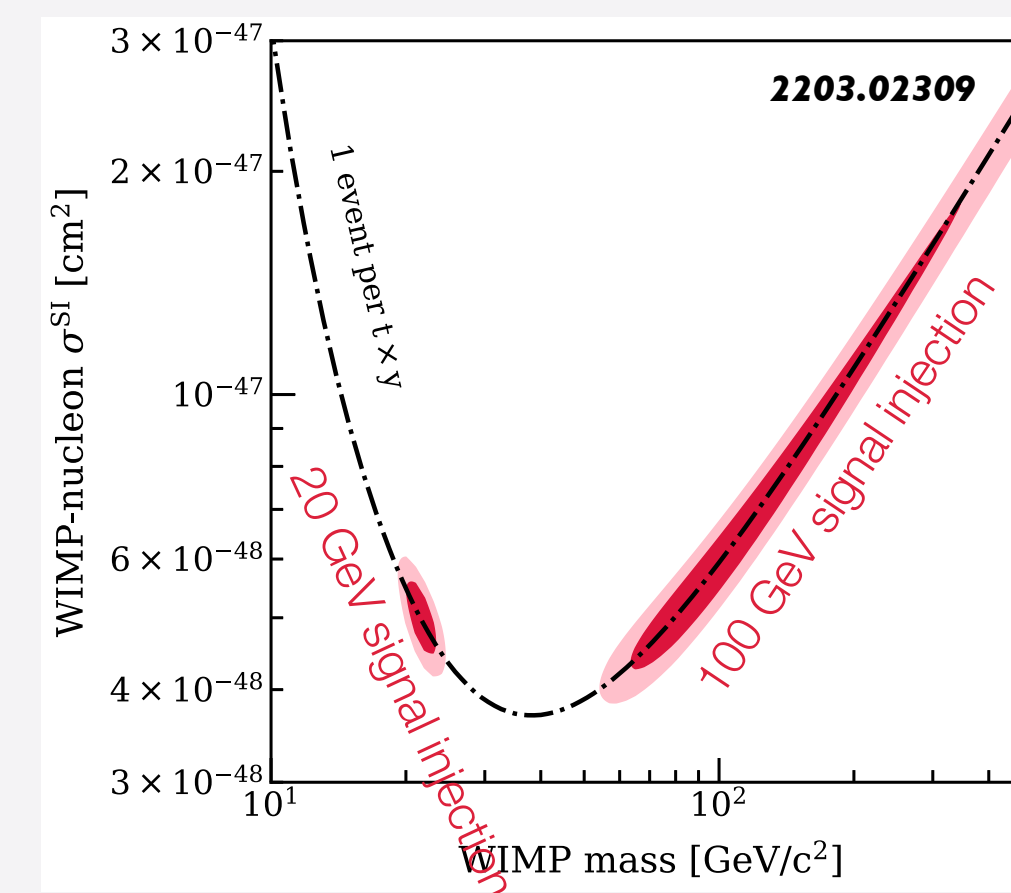


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# (IN)DIRECT DETECTION CIRCA 2030s

- Within 10 years we may have a detection of a WIMPs from natural source (big-bang)
- No detection at Darwin may kill the most minimal case ("odd-plet"  $Y = 0$ )
- Within 10 years we may get indirect observation of WIMPs annihilation
- "No detection" would be harder to interpret, because of possible missing pheno bits (e.g. expected SNR in the astrophysical objects for the actual detector resolution)

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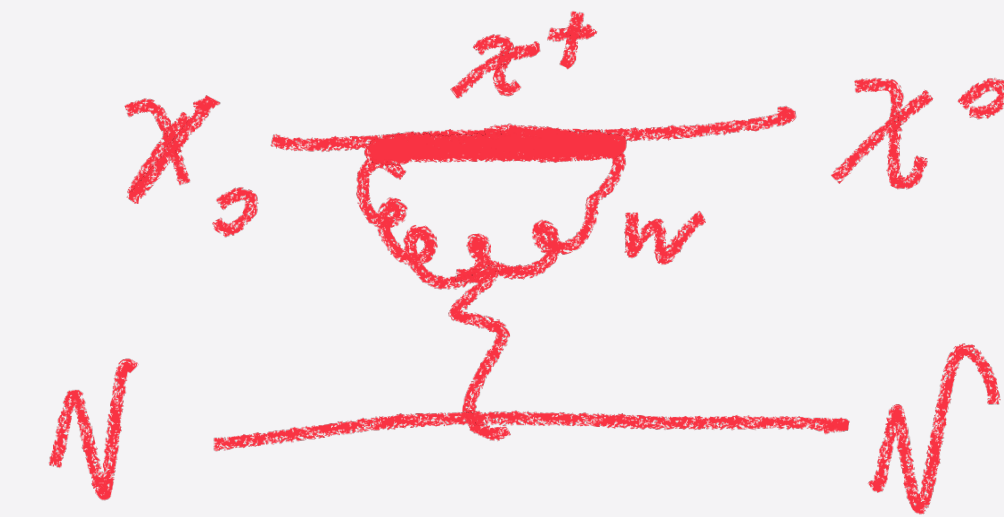
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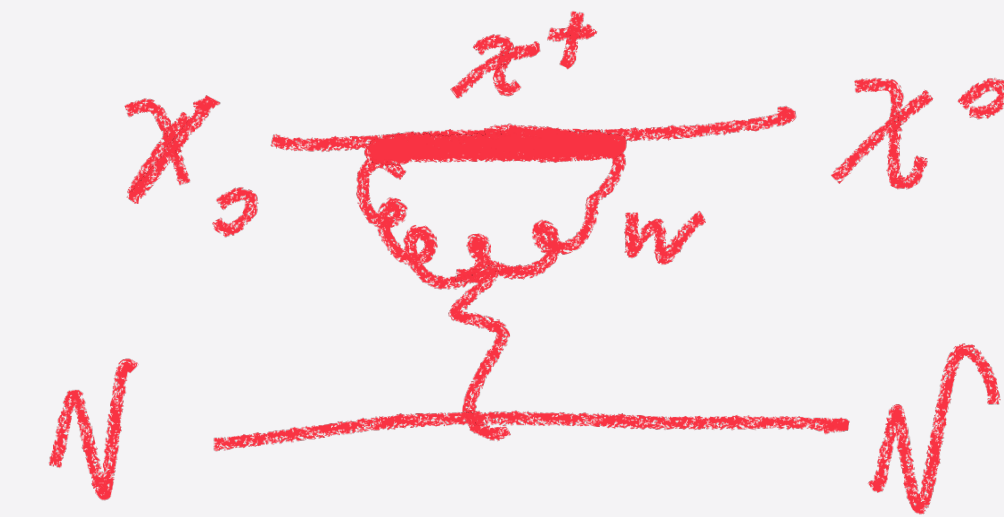
INELASTIC WIMP SCATTERING

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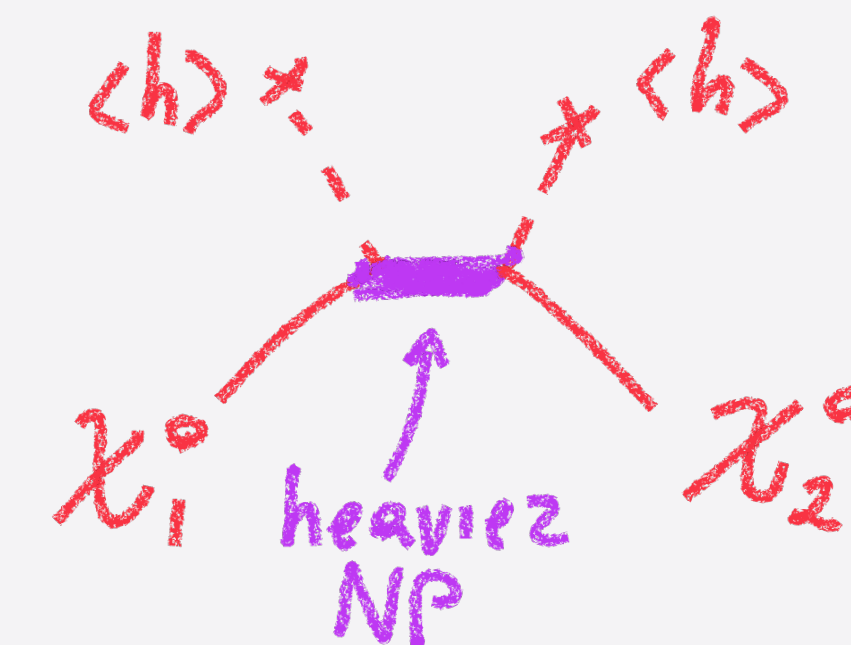
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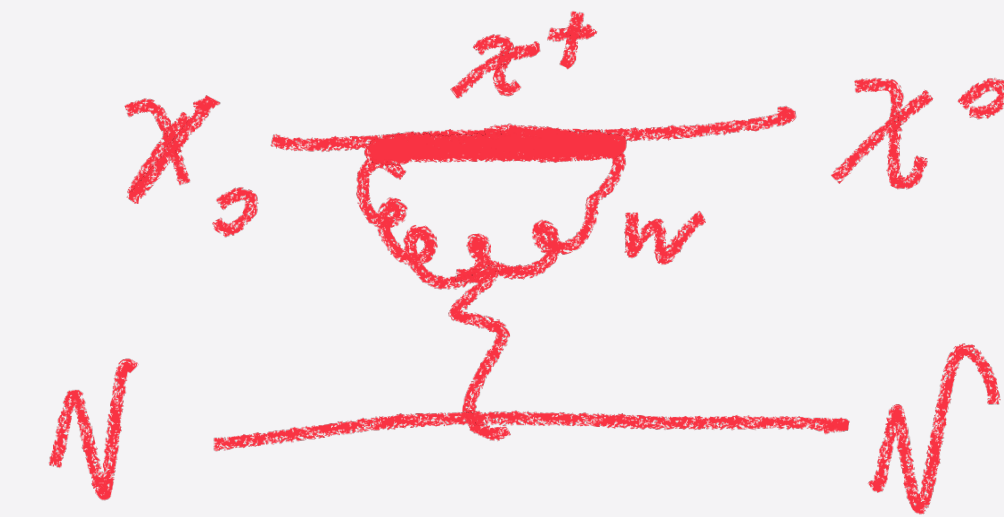




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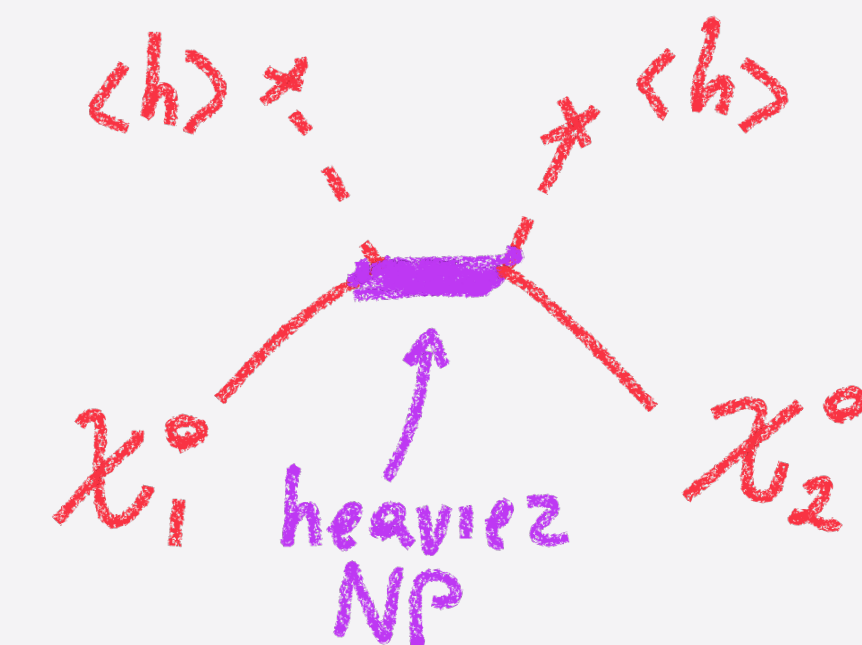
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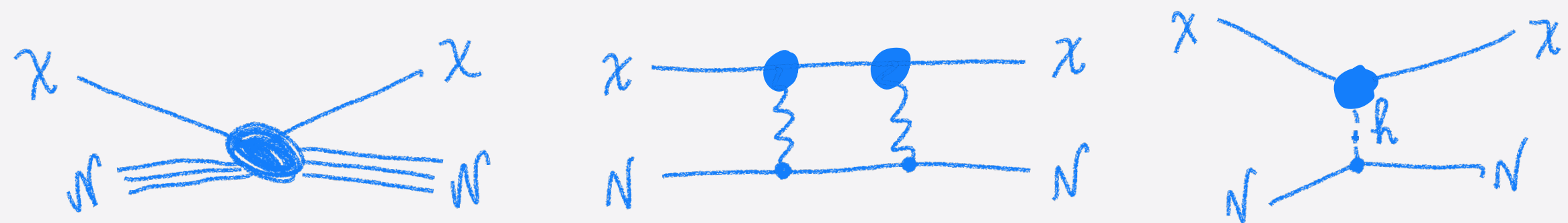
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hypercharge offers one extra handle on the mass splitting

# DIRECT DETECTION

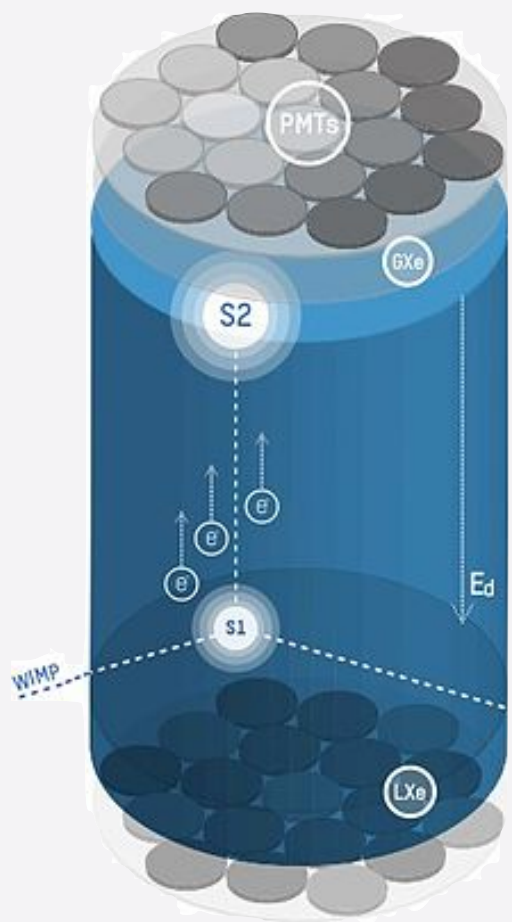
$Y \neq 0$ , pure EW Mass-Splitting



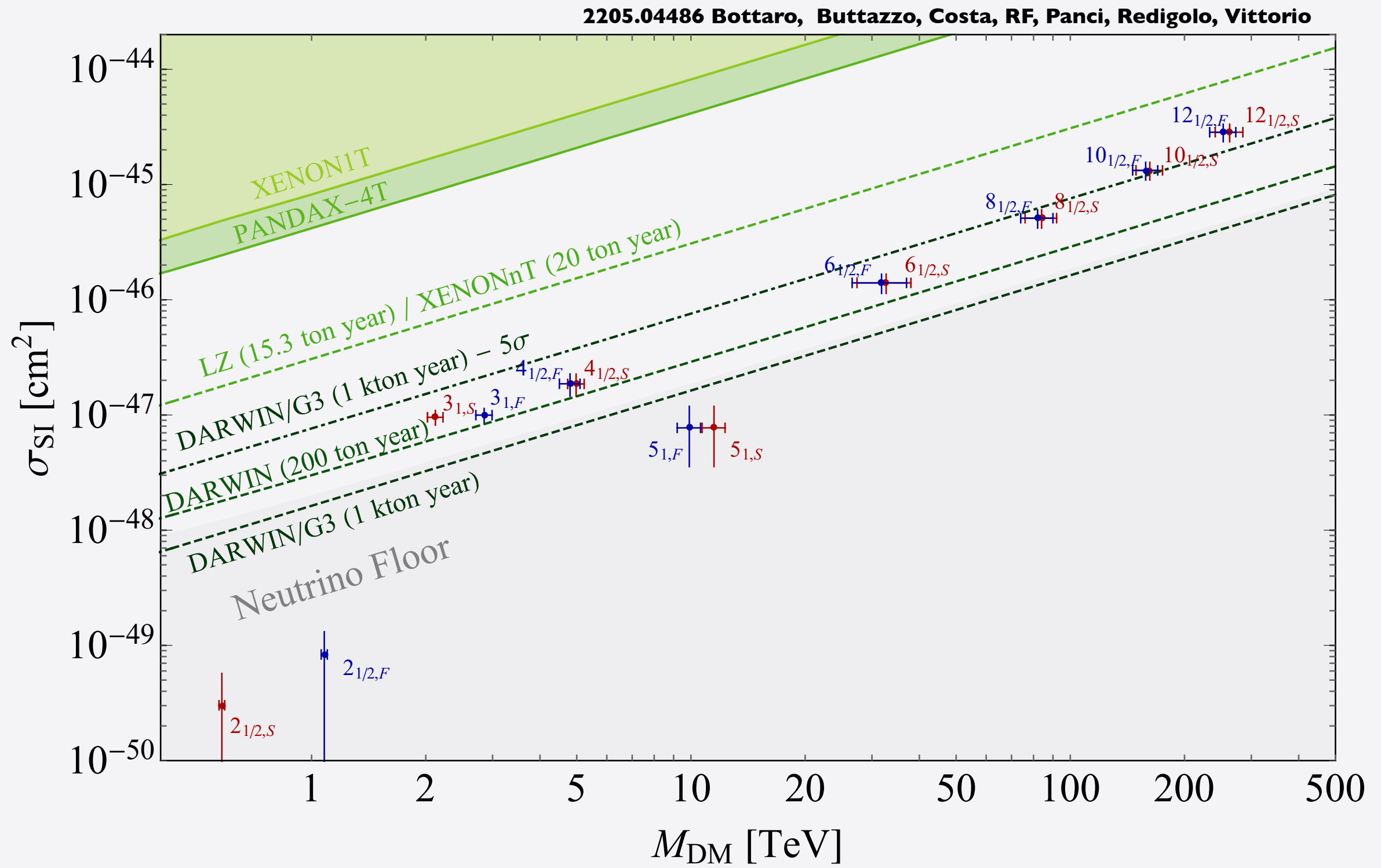
Scattering on SM materials can be detected in ultra-low background experiments

Larger rates for the larger  $n$ -plets keep them visible

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**2030s**  
up to  $O(\text{PeV})$



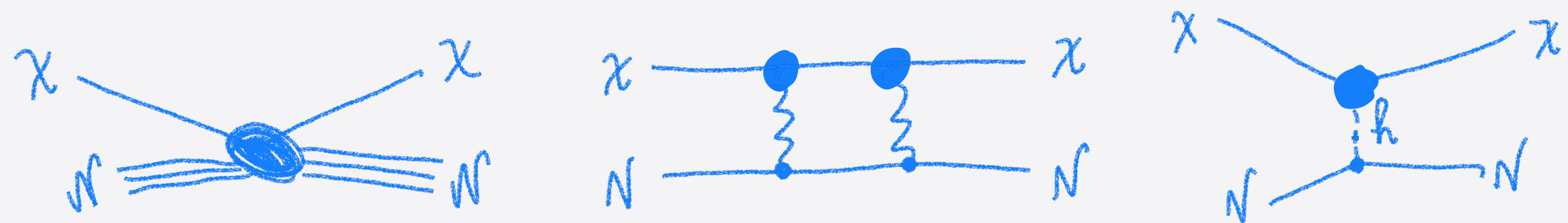
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simple  $2n$ -plet scenarios can evade Direct Detection

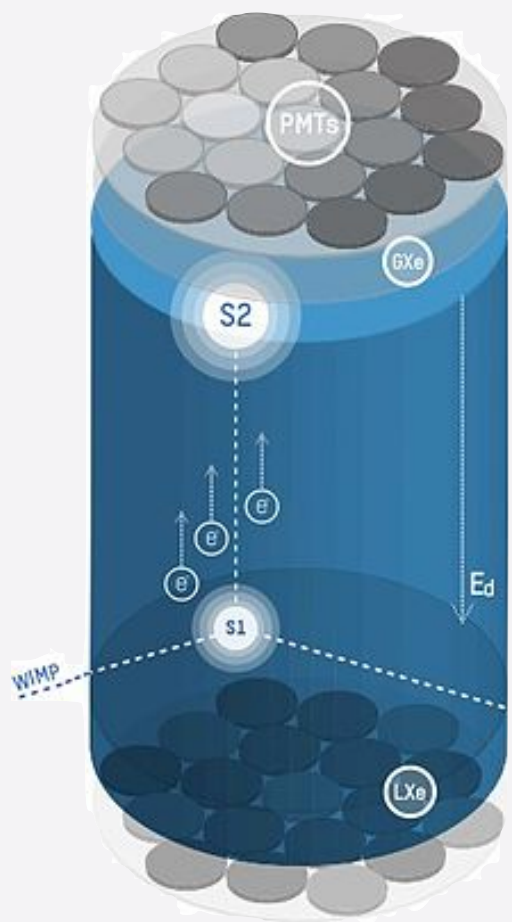


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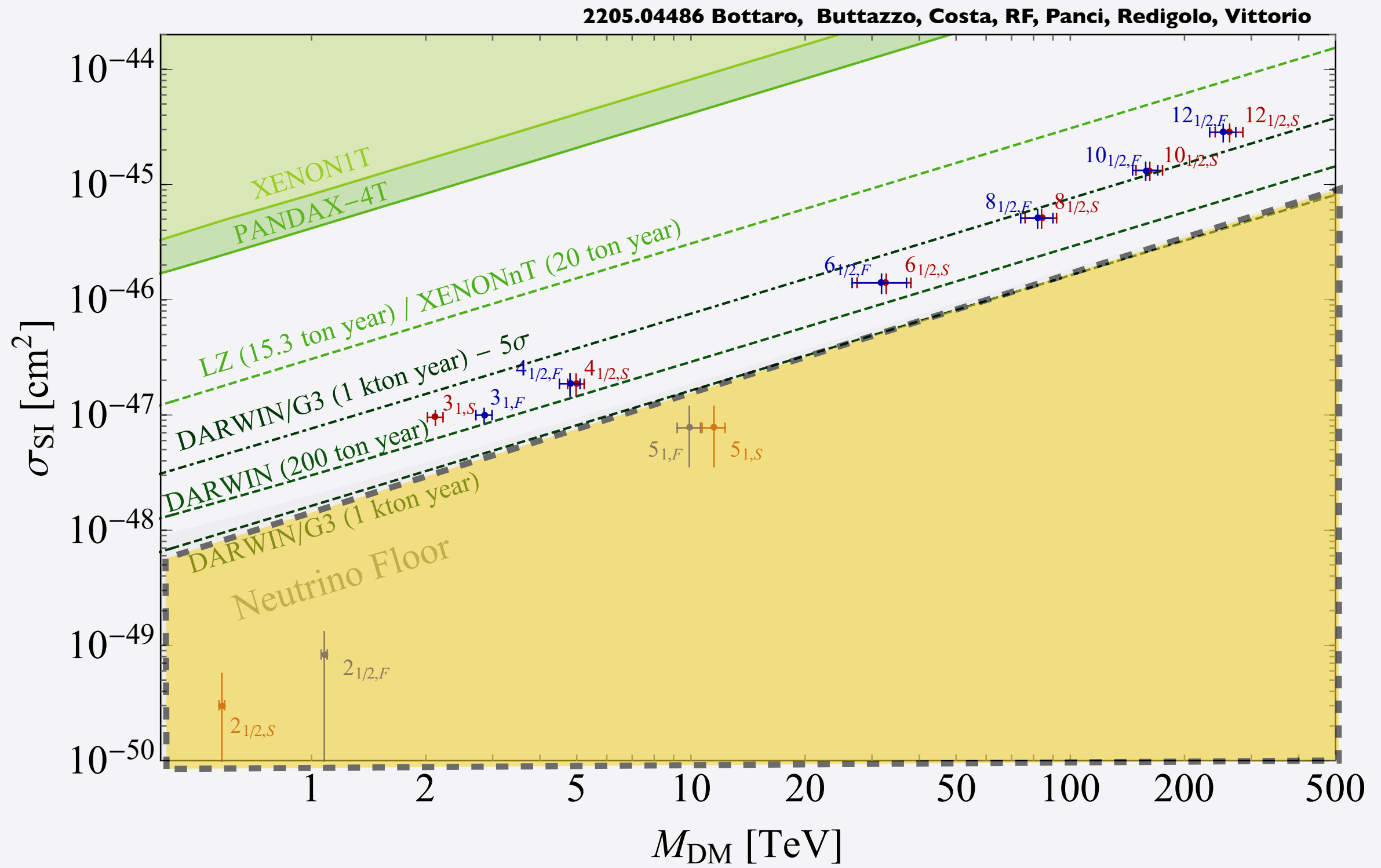
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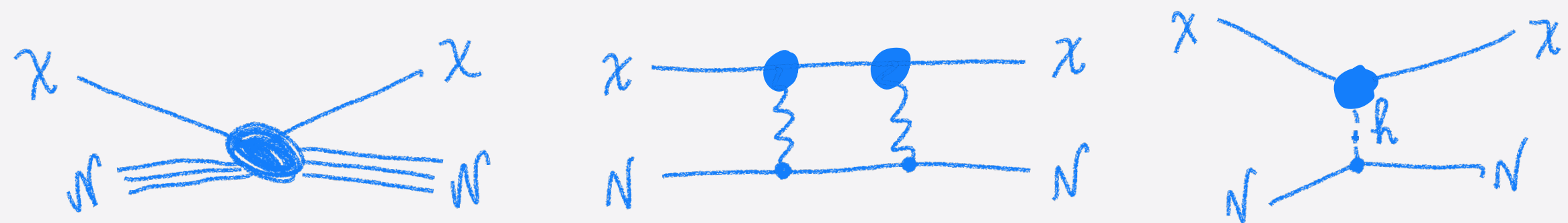


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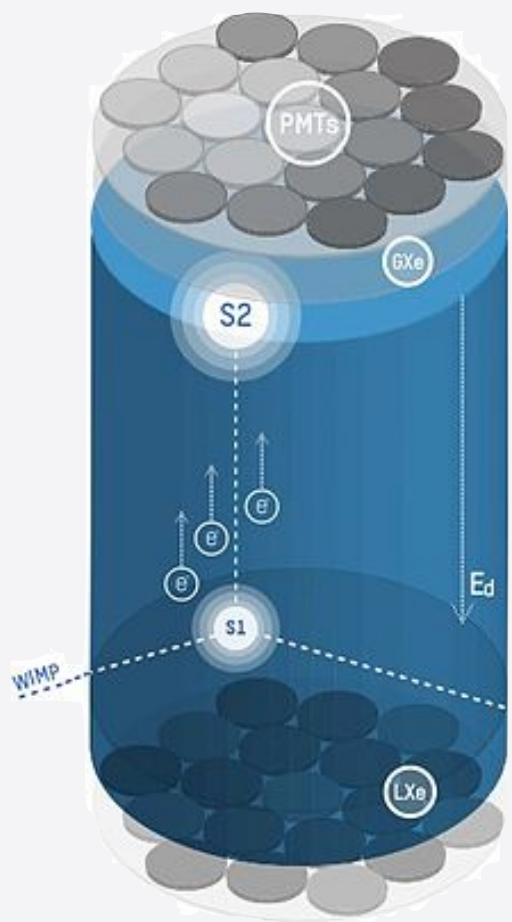
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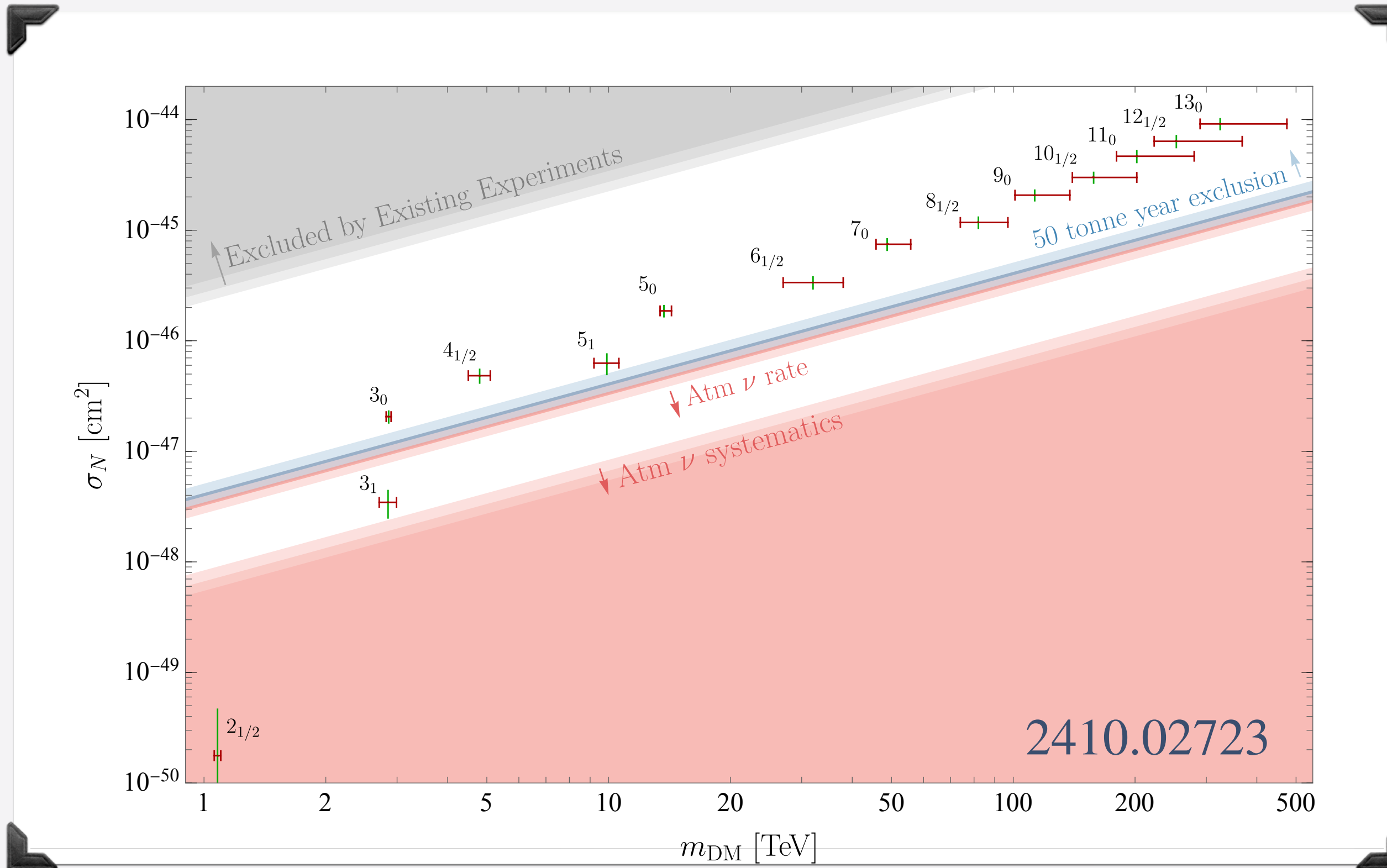
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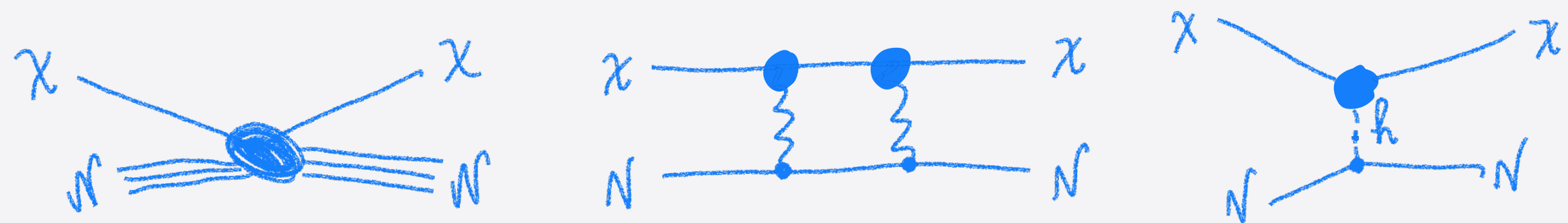
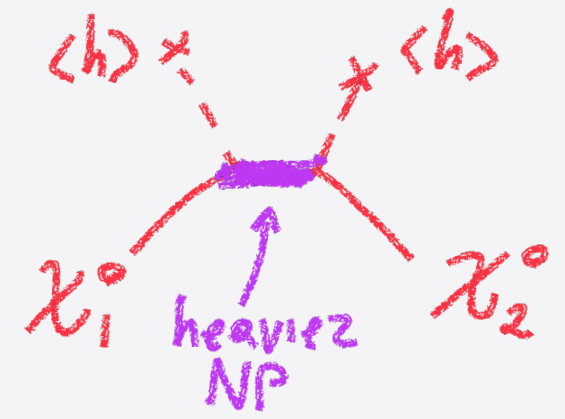
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# DIRECT DETECTION

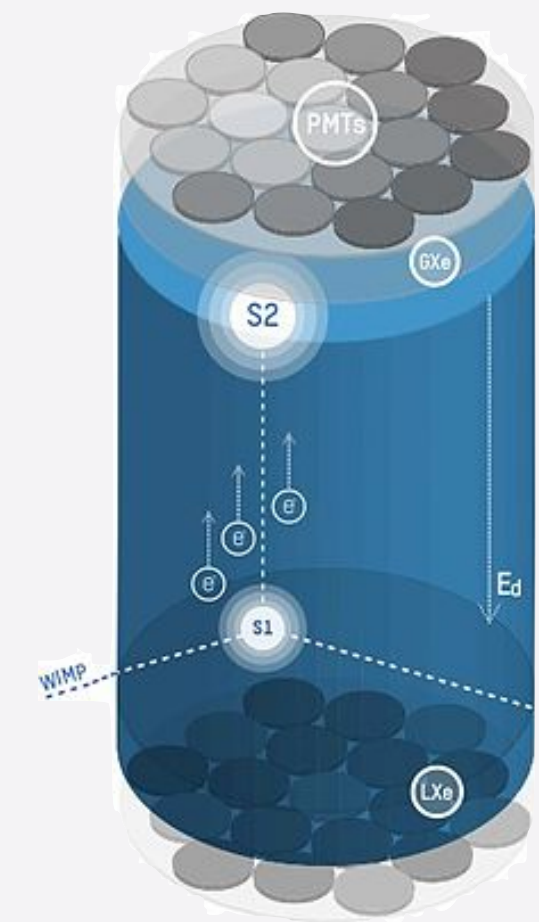
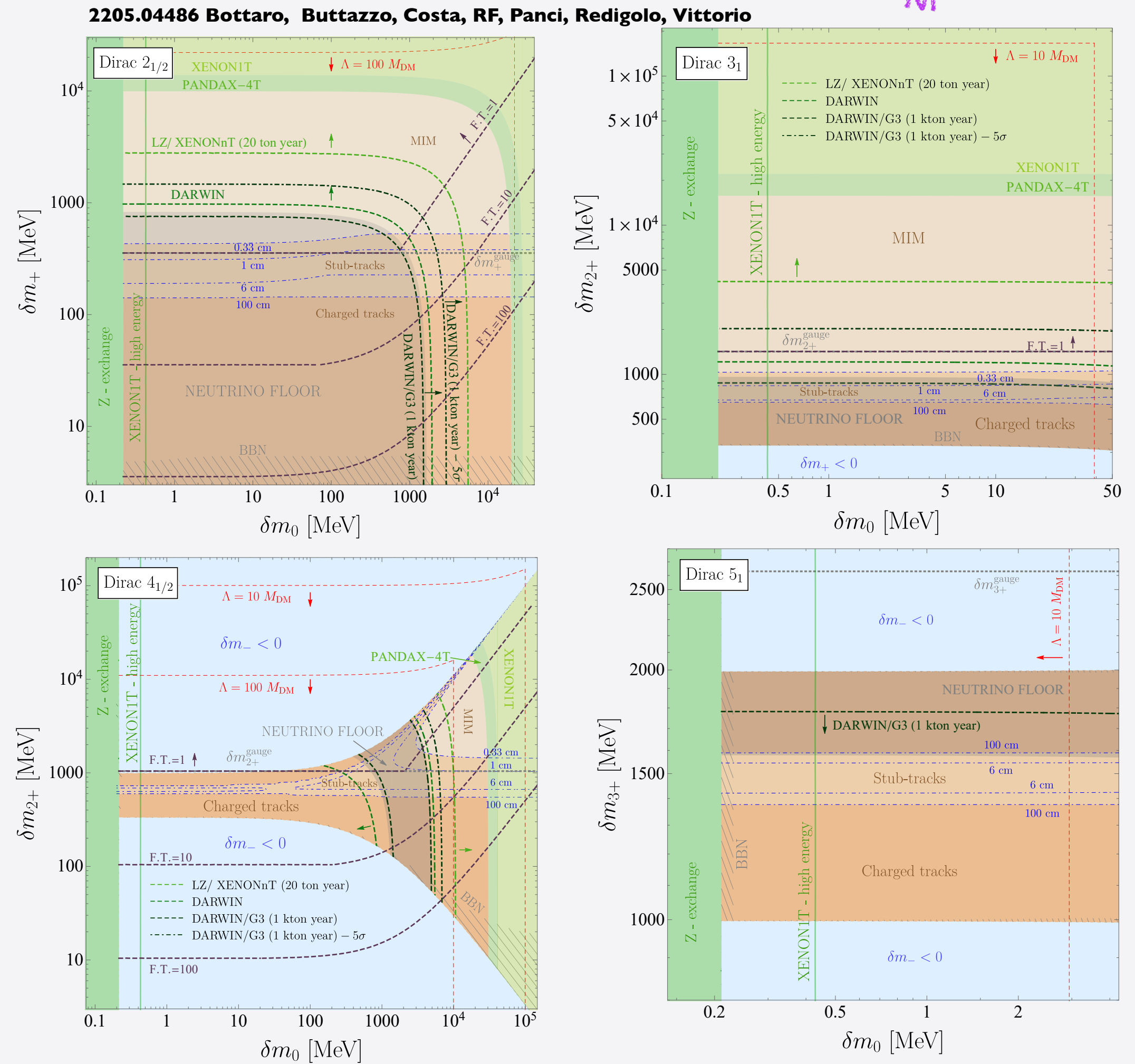
$Y \neq 0$ , Mass-Splitting from DIM>4



Scattering on SM materials can be detected in ultra-low background experiments

Larger rates for the larger  $n$ -plets keep them visible

For such large DM mass the signature does not depend on the DM mass.



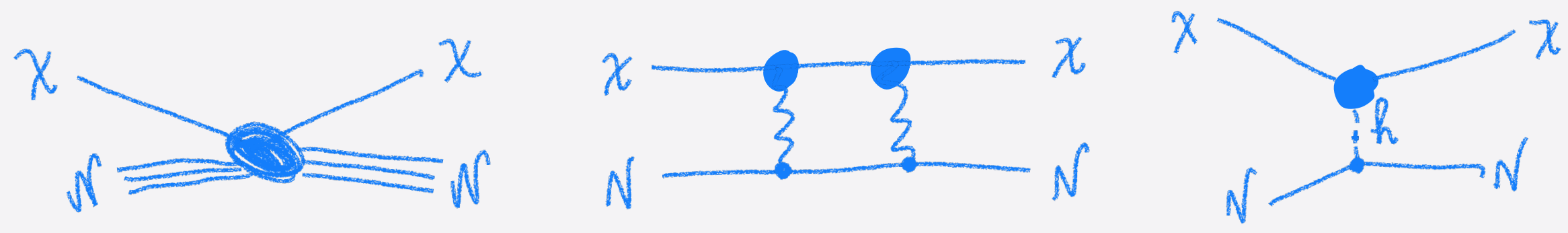
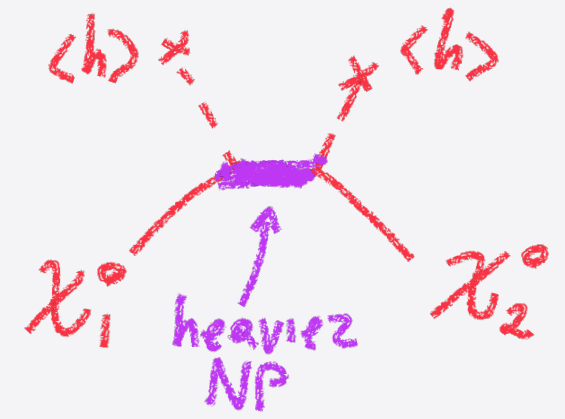
# 2030s

up to  $O(\text{PeV})$

all next-to-simple  $2n$ -plet scenarios can evade Direct Detection

# DIRECT DETECTION

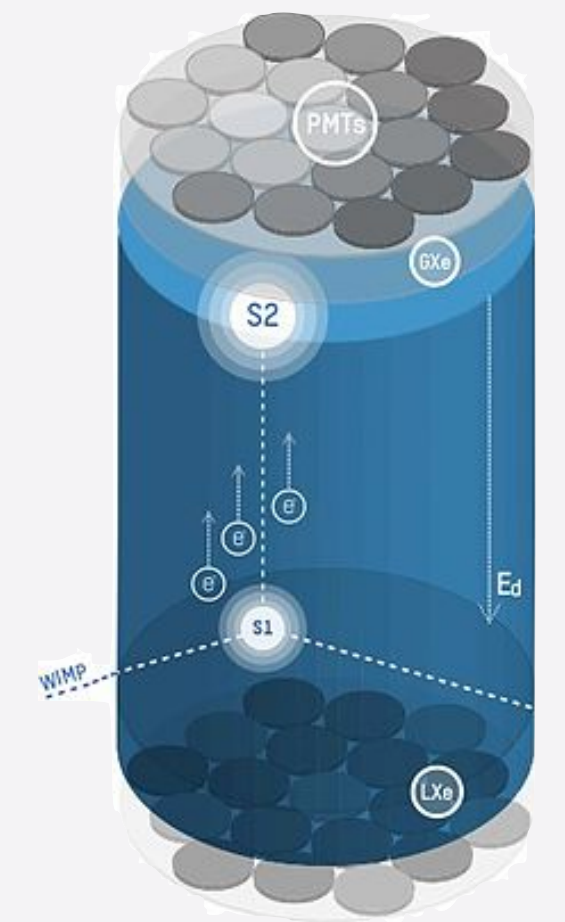
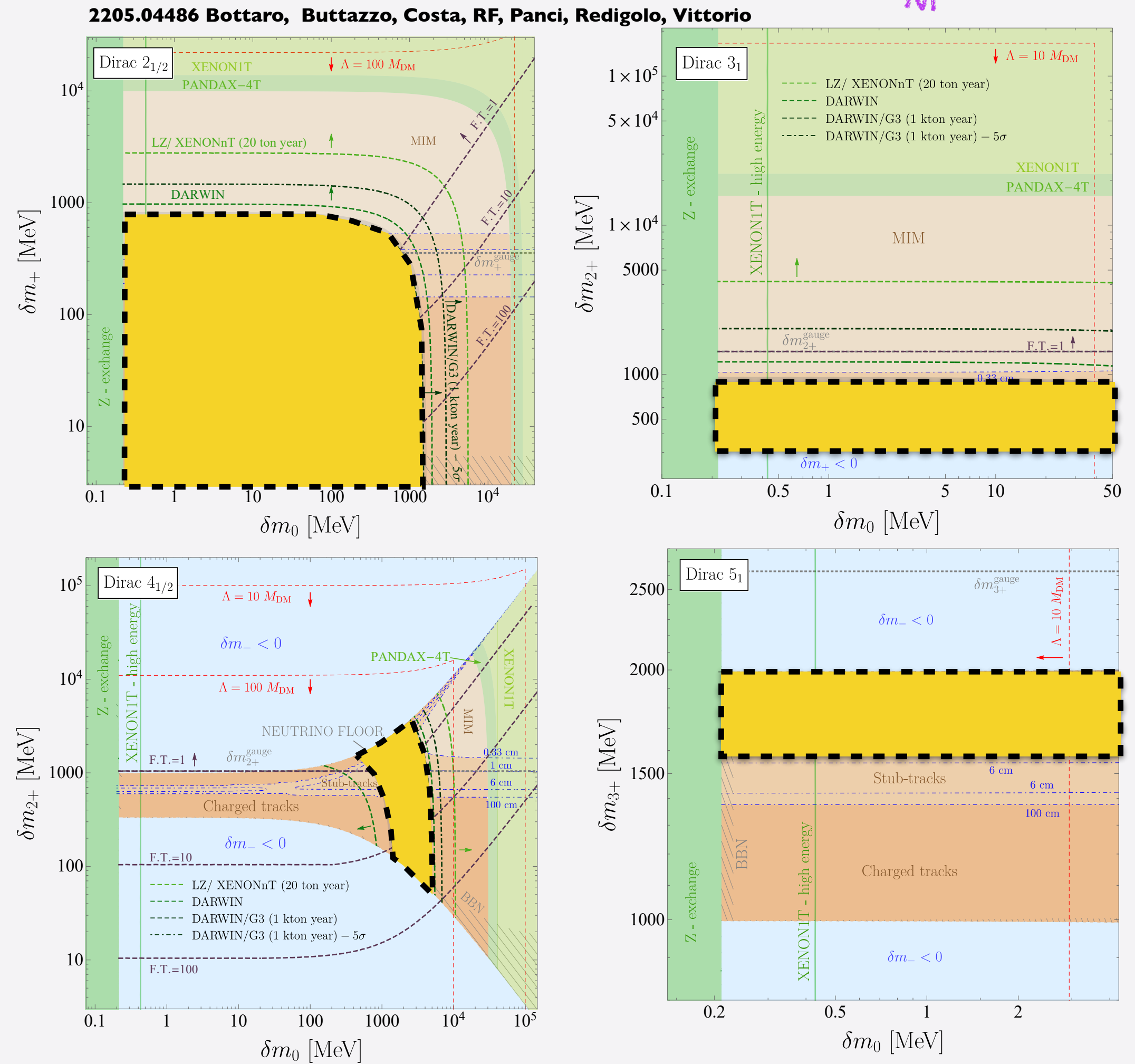
$Y \neq 0$ , Mass-Splitting from DIM>4



Scattering on SM materials can be detected in ultra-low background experiments

Larger rates for the larger  $n$ -plets keep them visible

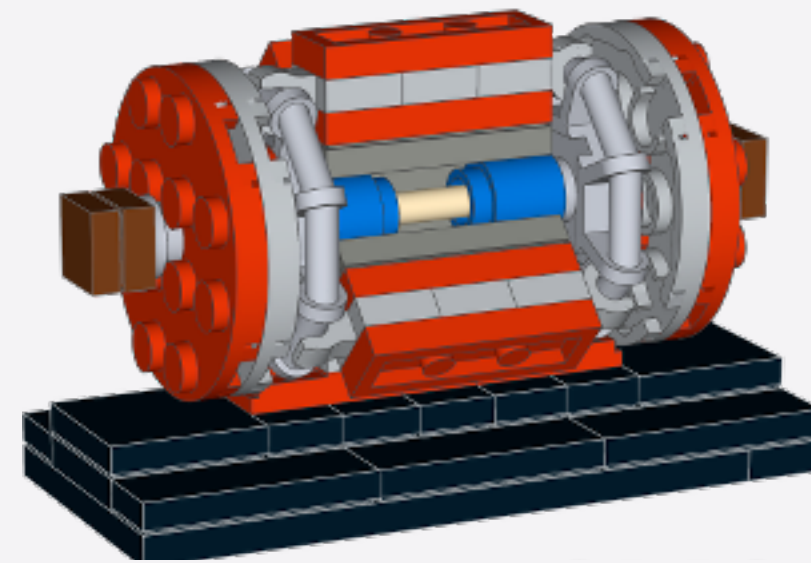
For such large DM mass the signature does not depend on the DM mass.



**2030s**  
up to  $O(\text{PeV})$

all next-to-simple  $2n$ -plet scenarios can evade Direct Detection

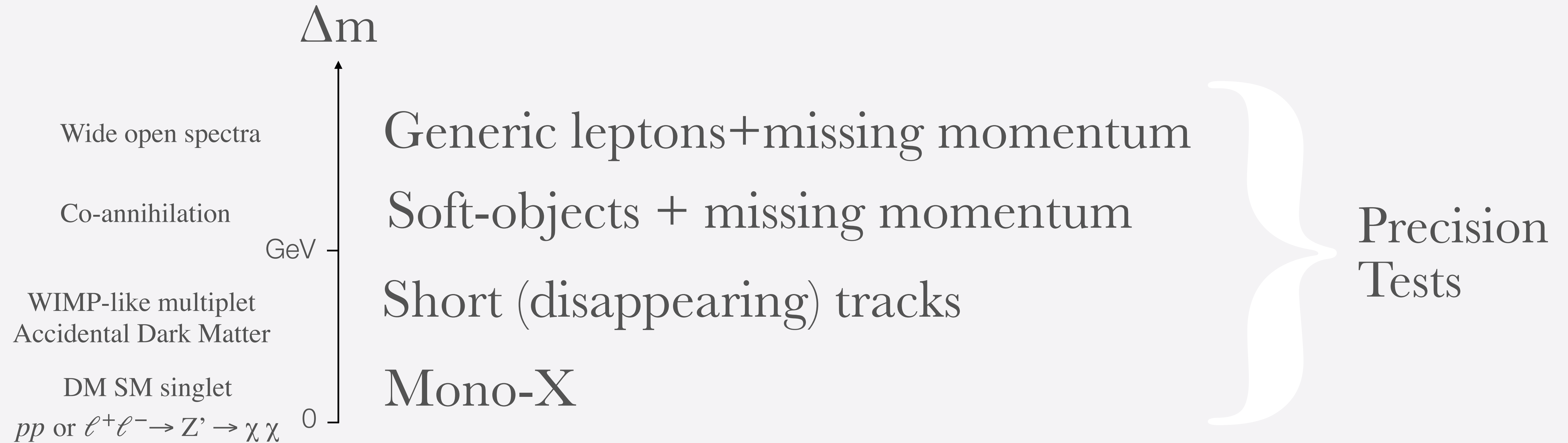
# DIRECT PRODUCTION AT COLLIDERS



2040s

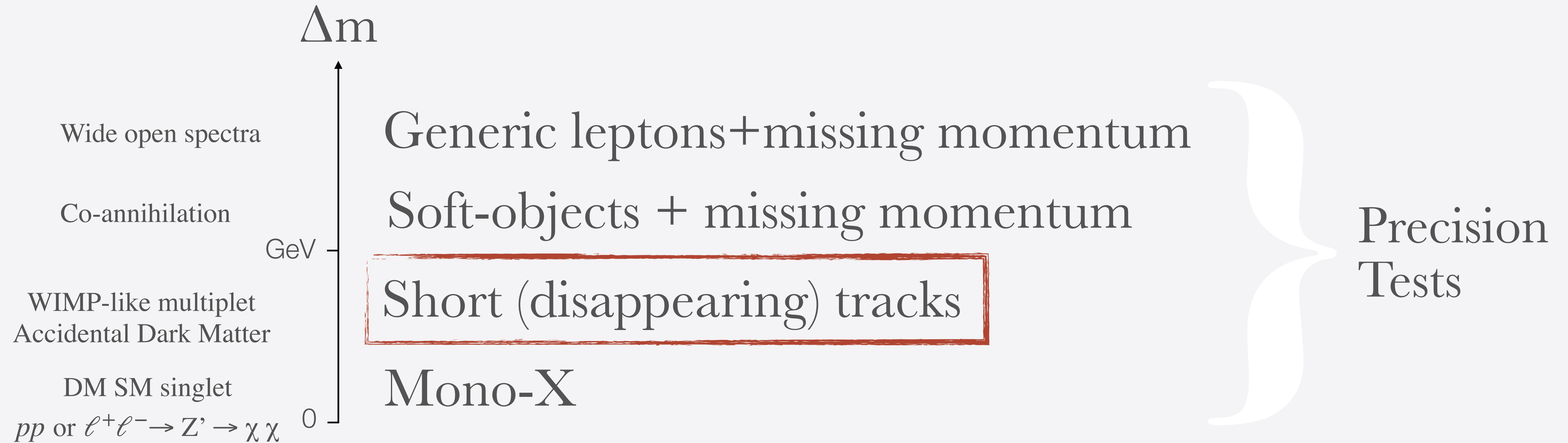


# DIRECT SIGNALS AT COLLIDERS





# DIRECT SIGNALS AT COLLIDERS



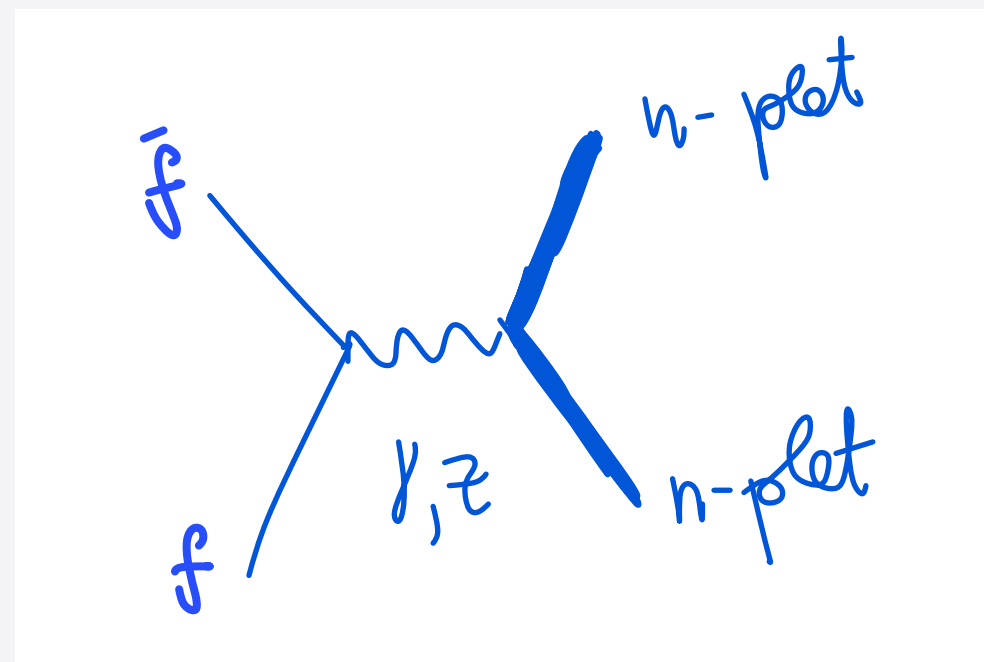
# PURE $\tilde{h}$ AND $\tilde{W}$ DM

stub track and soft tracks

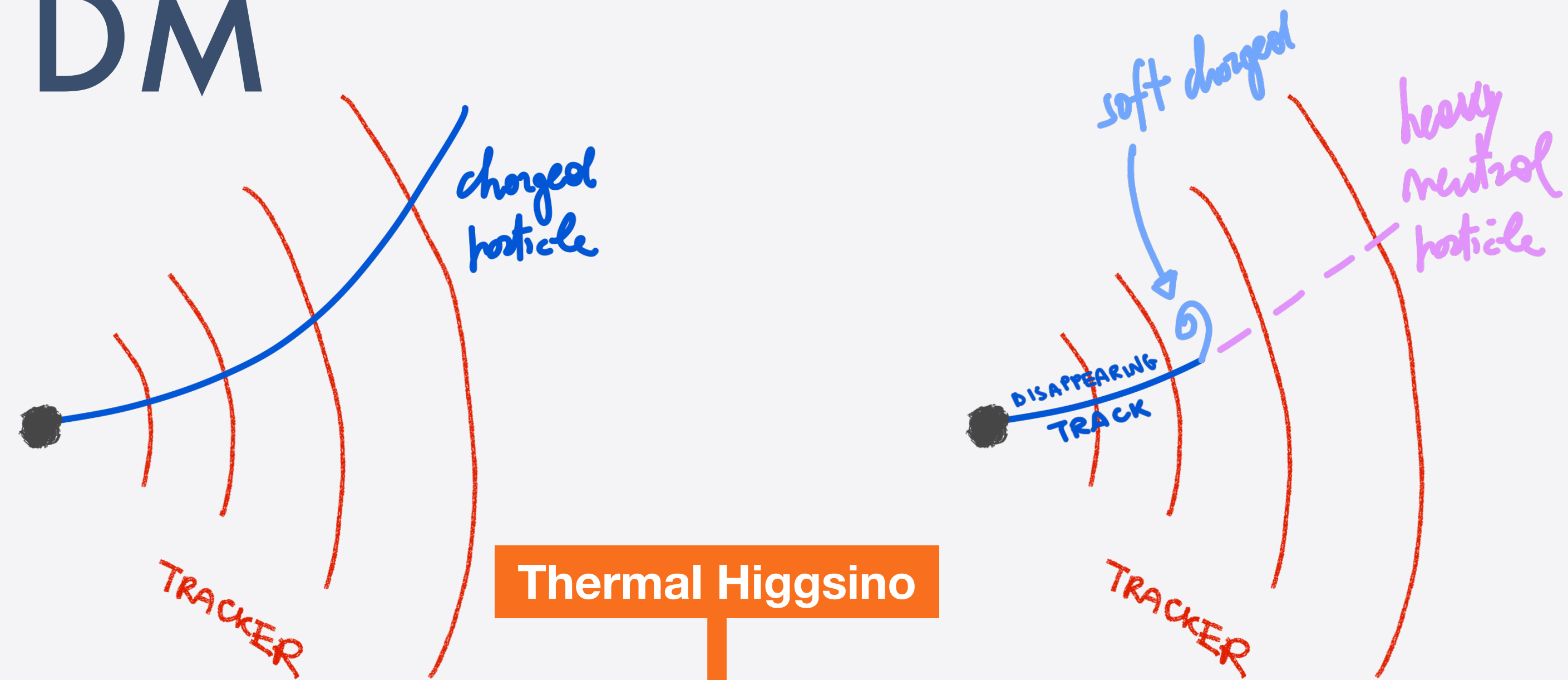
## 2040s

up to  $\mu\mu$  3-10 TeV

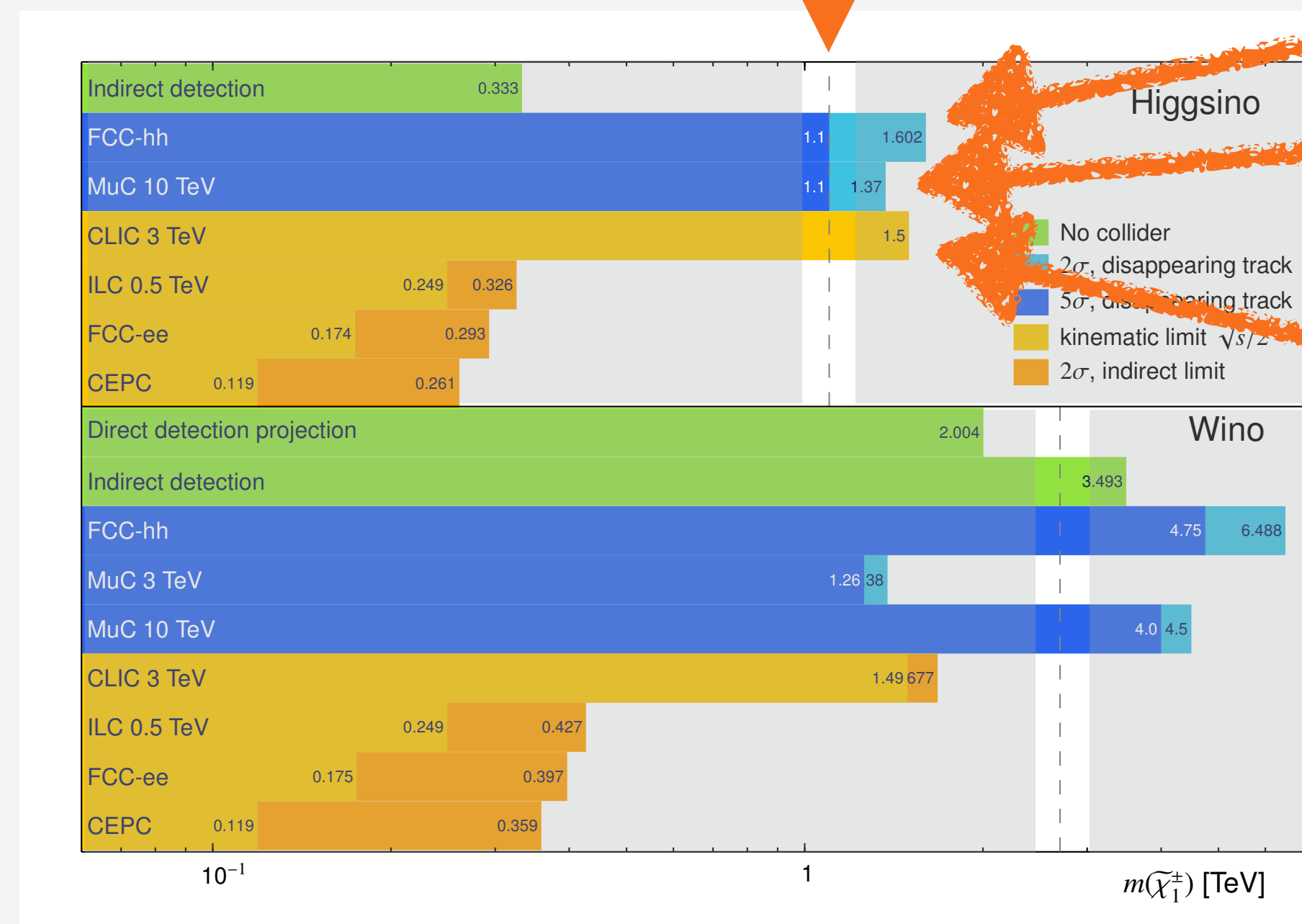
- Heavy  $n$ -plet of SU(2)
- Mass splitting  $\sim \alpha_W m_W \sim 0.1\text{GeV} - 1\text{GeV}$



Large rates, but needs to light up the detector in a discernible way



Thermal Higgsino



$pp$  100 TeV 30  $\text{ab}^{-1}$   
 $\mu^+\mu^-$  10 TeV 10  $\text{ab}^{-1}$   
 $e^+e^-$  3 TeV 5  $\text{ab}^{-1}$

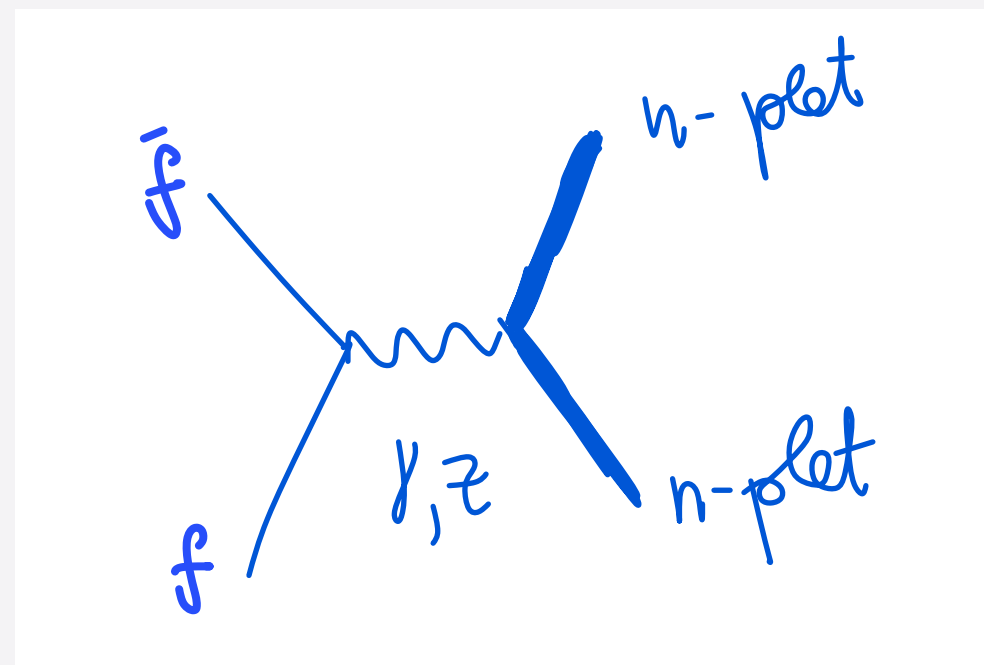
# PURE $\tilde{h}$ AND $\tilde{W}$ DM

stub track and soft tracks

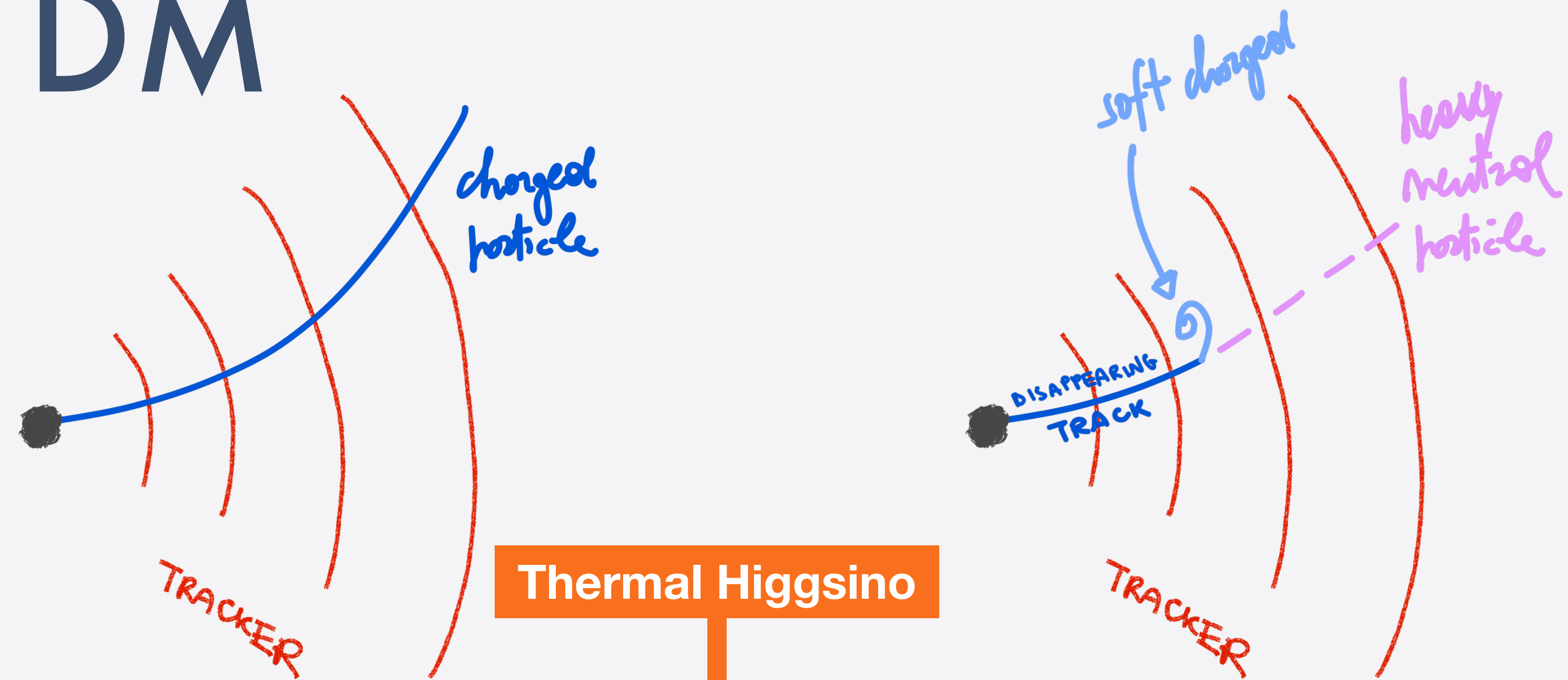
## 2040s

up to  $\mu\mu$  3-10 TeV

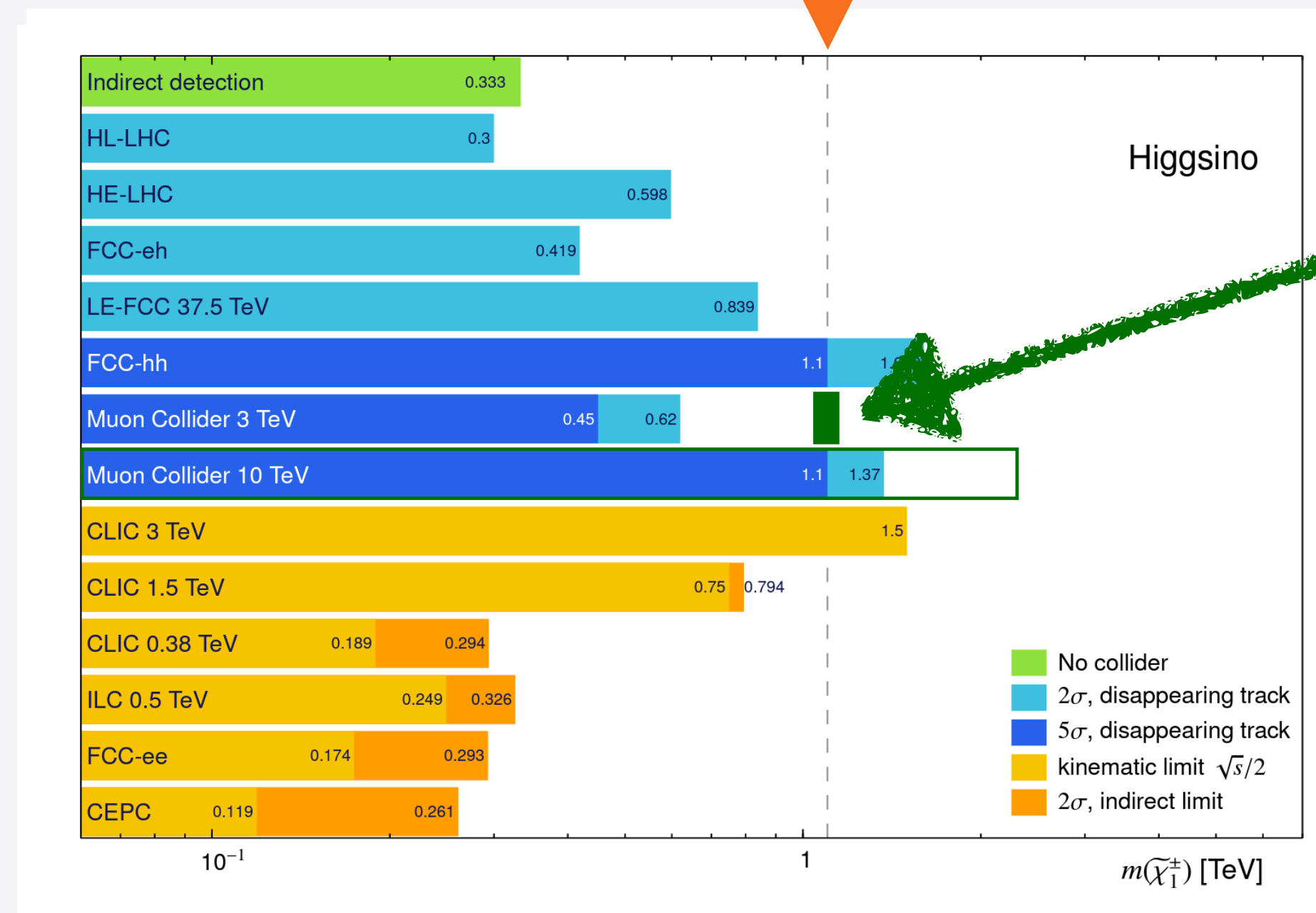
- Heavy  $n$ -plet of SU(2)
- Mass splitting  $\sim \alpha_W m_W \sim 0.1\text{GeV} - 1\text{GeV}$



Large rates, but needs to light up the detector in a discernible way



Thermal Higgsino



$\mu^+\mu^-$  3 TeV 1 ab<sup>-1</sup>  
2405.08858

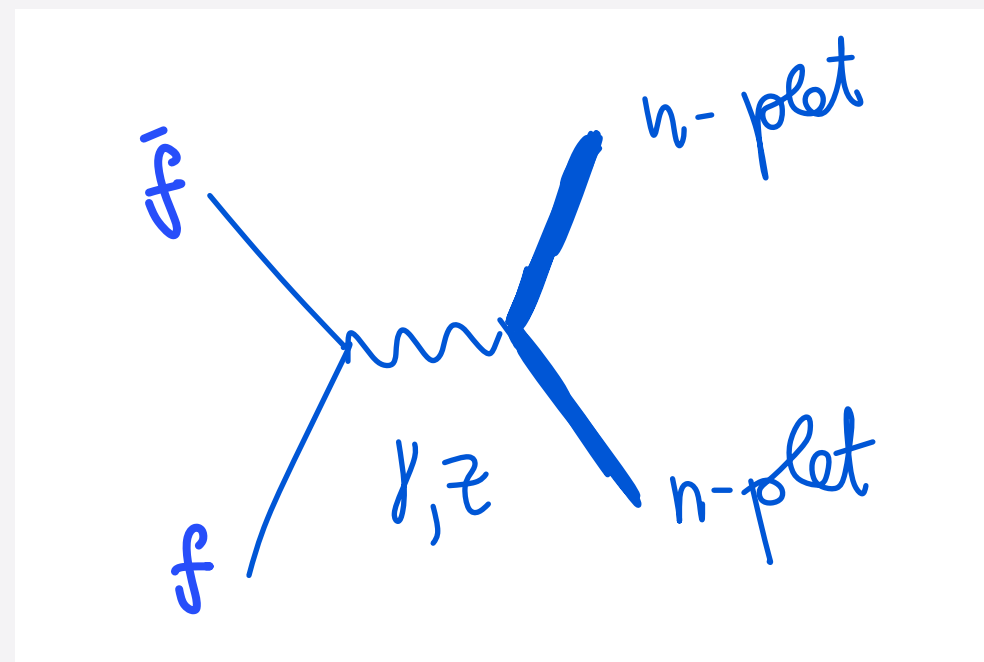
# PURE $\tilde{h}$ AND $\tilde{W}$ DM

stub track and soft tracks

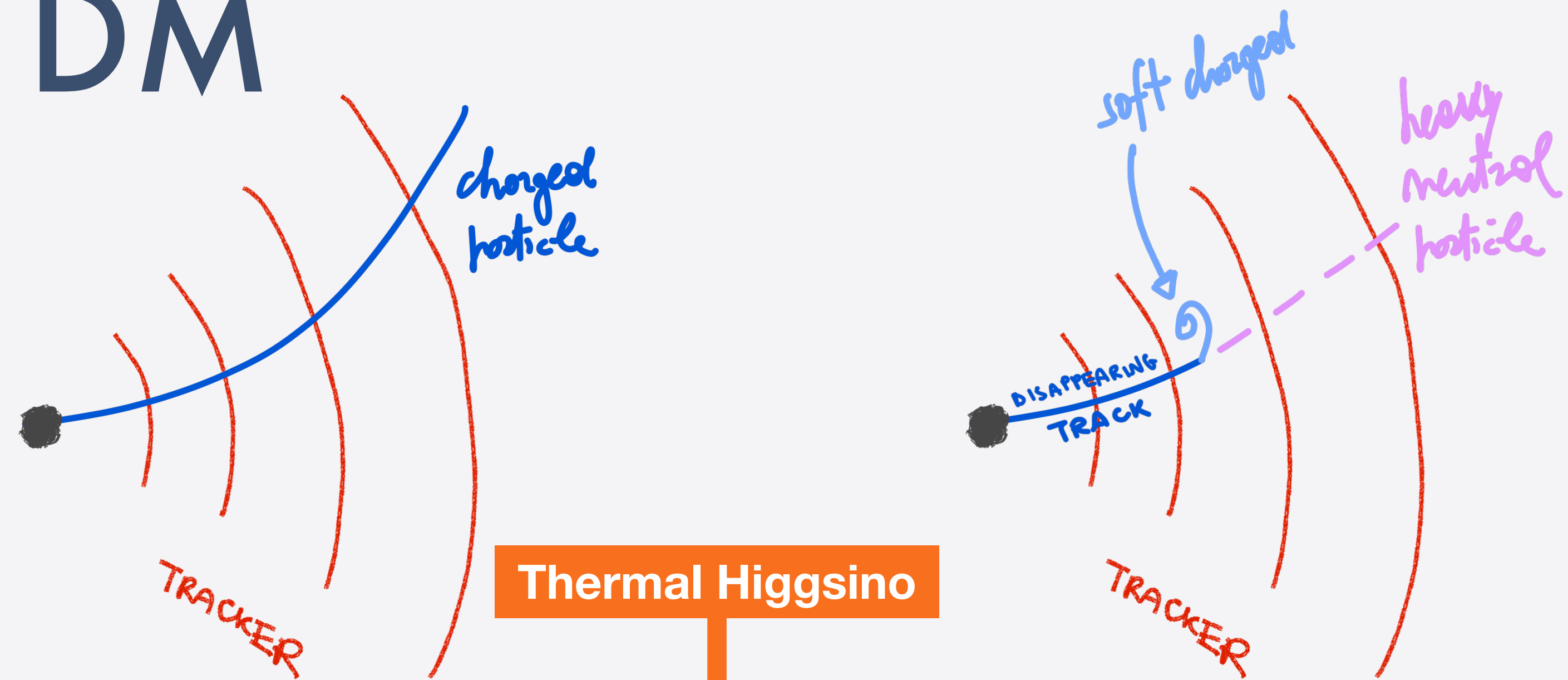
## 2040s

up to  $\mu\mu$  3-10 TeV

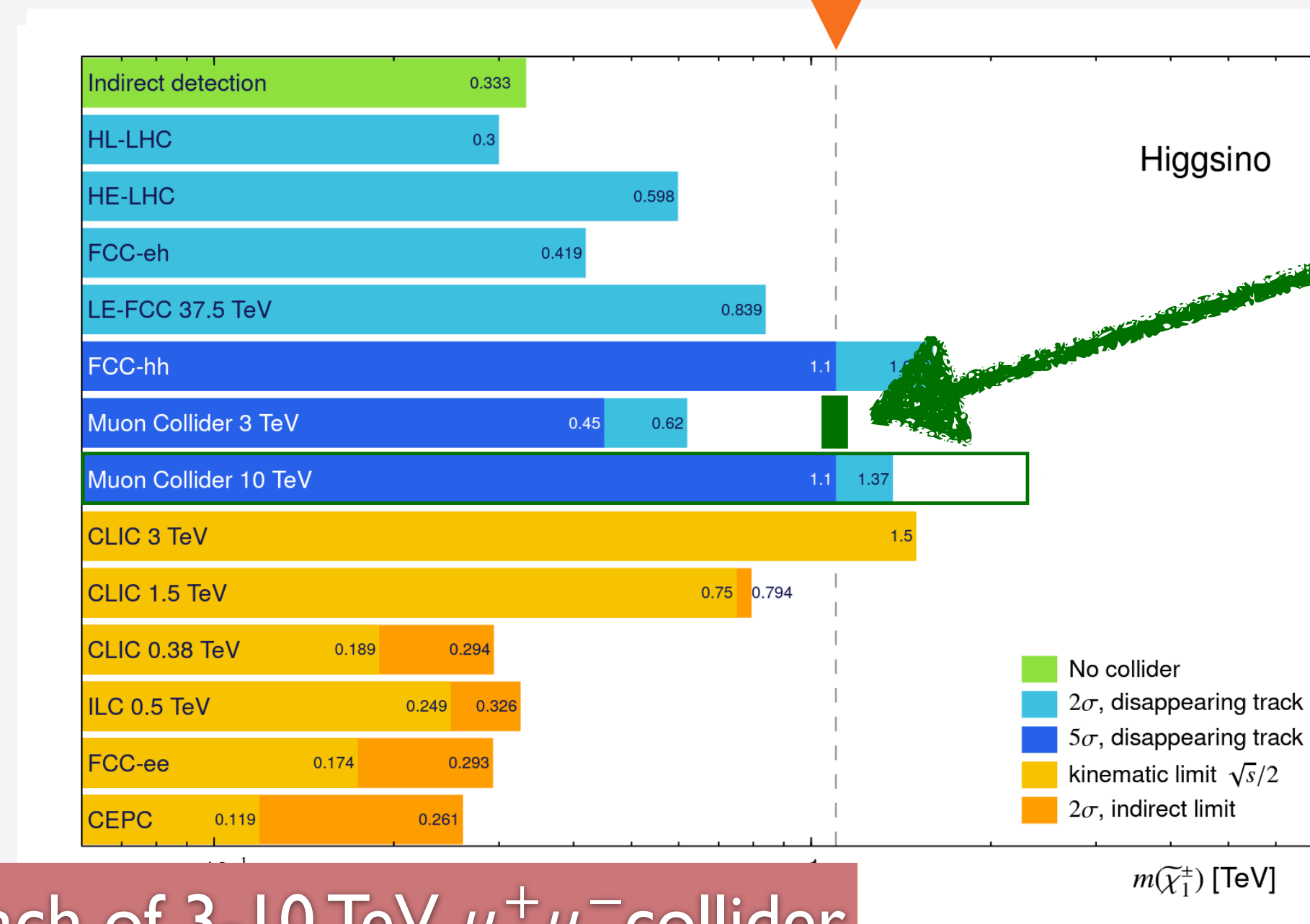
- Heavy  $n$ -plet of SU(2)
- Mass splitting  $\sim \alpha_W m_W \sim 0.1\text{GeV} - 1\text{GeV}$



Large rates, but needs to light up the detector in a discernible way



Thermal Higgsino

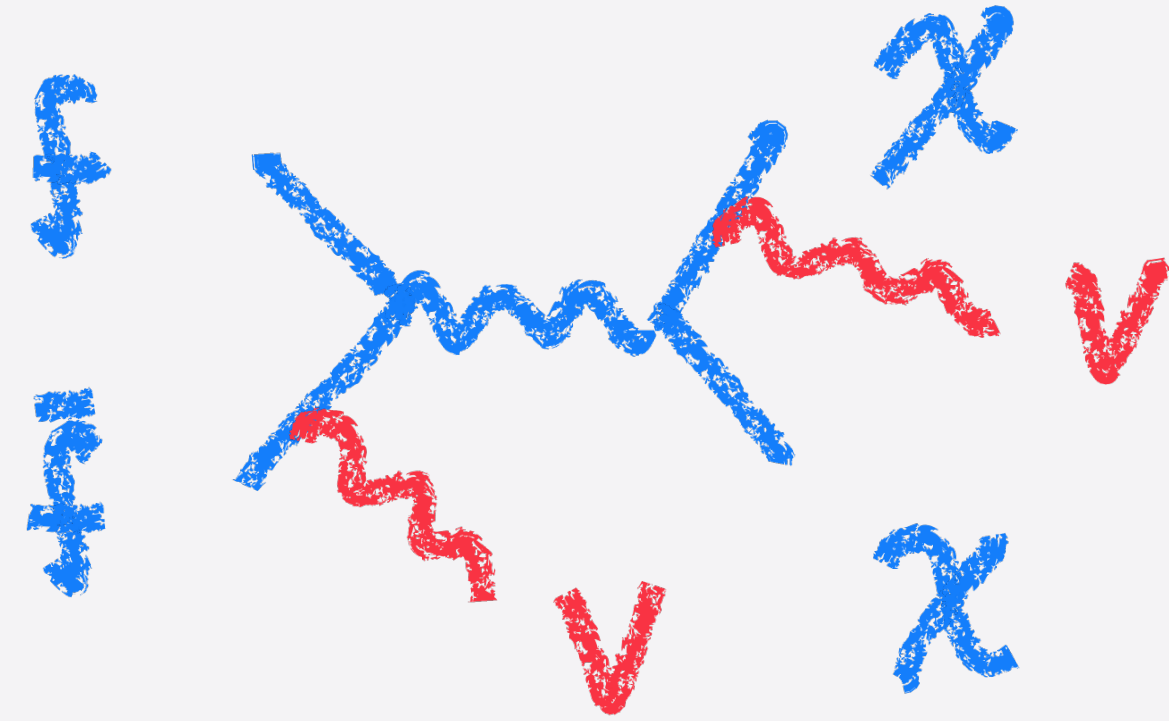


$\mu^+\mu^-$  3 TeV  $1\text{ab}^{-1}$   
2405.08858

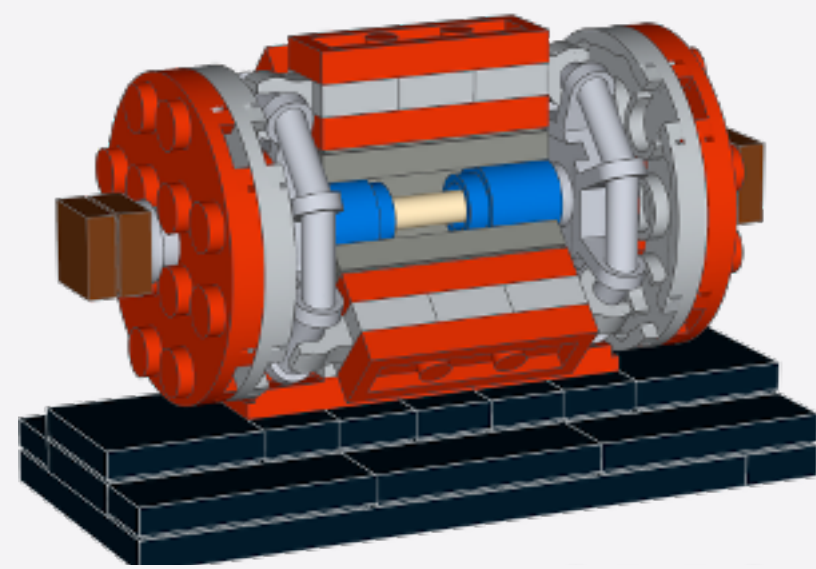


# PURE $\tilde{h}$ AND $\tilde{W}$ DM

## stub tracks

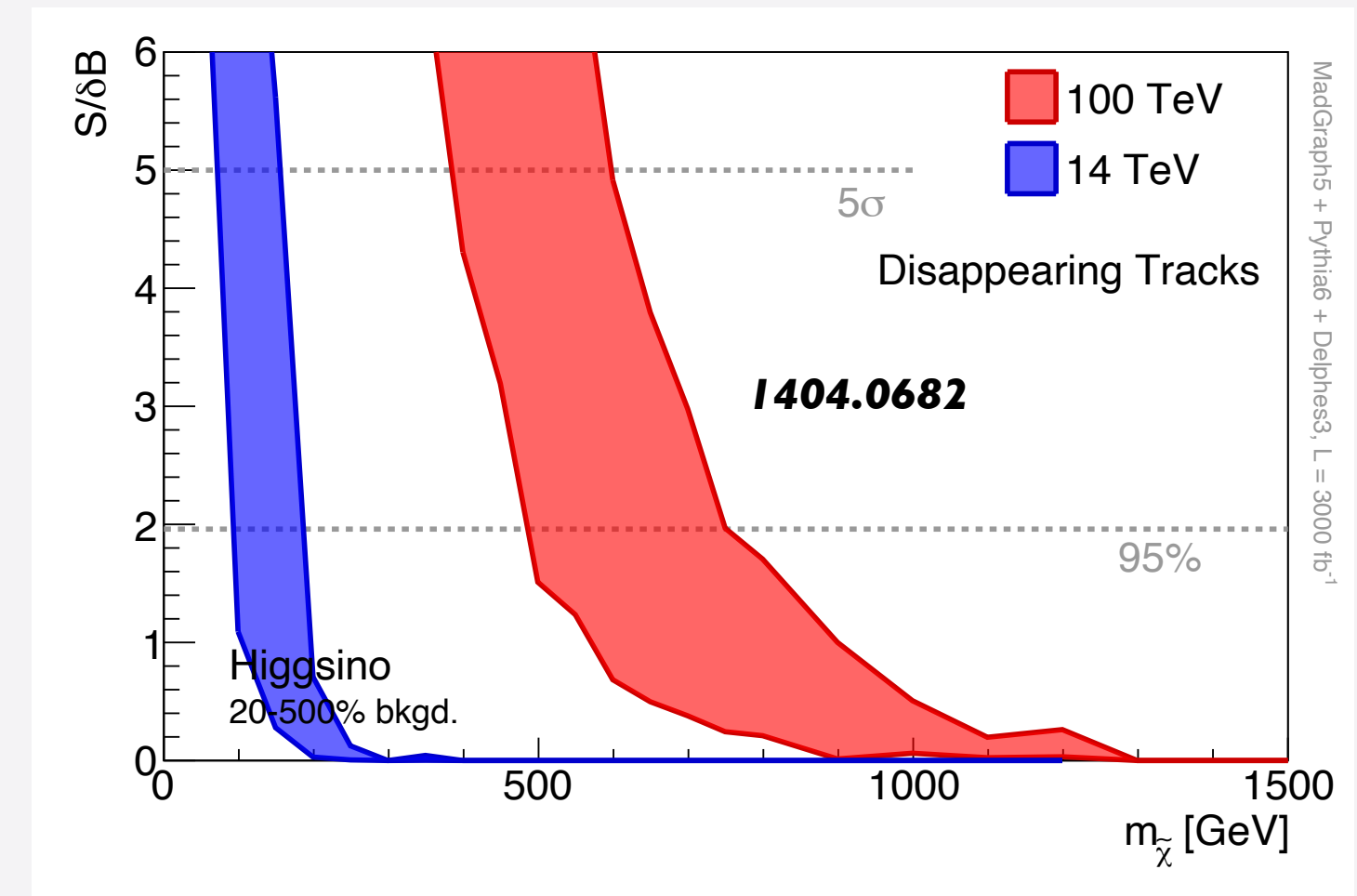
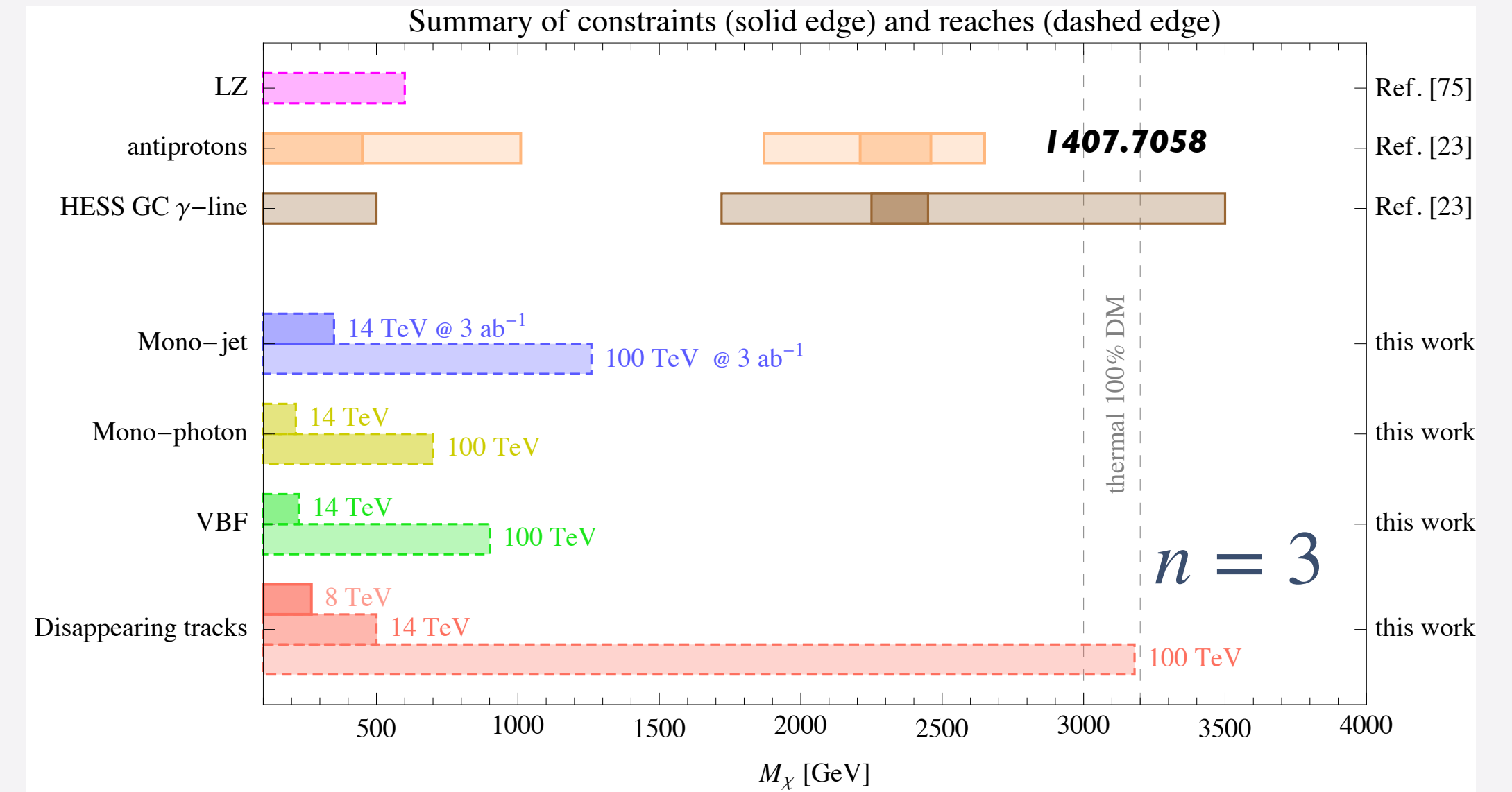


Production of Dark Matter weak multiplet states and observation of the decay products or associated productions

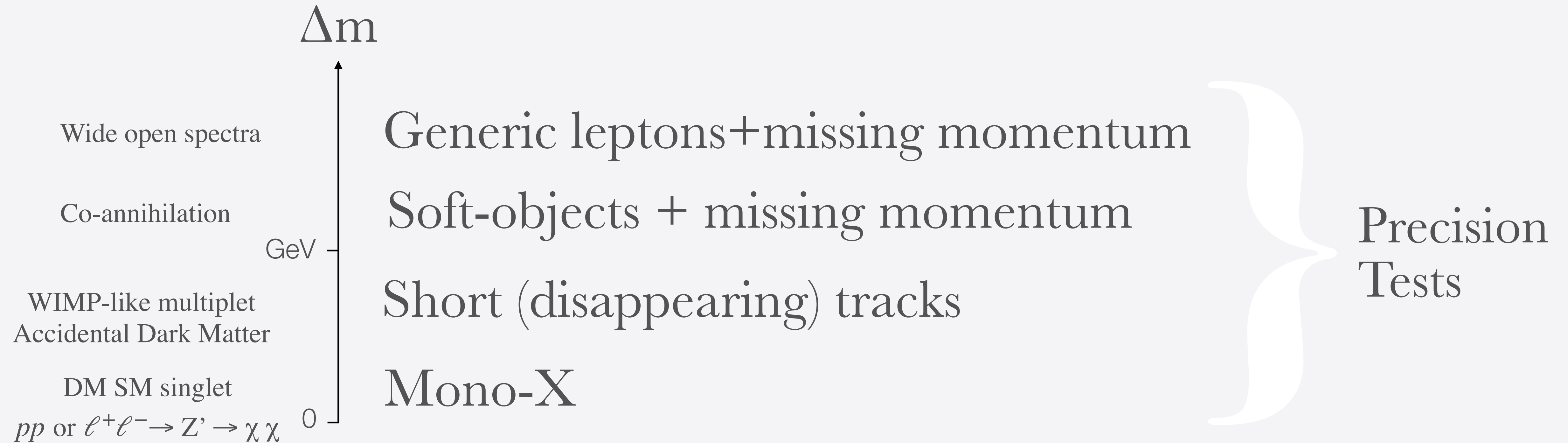


**2060s**  
up to  $pp$  100 TeV

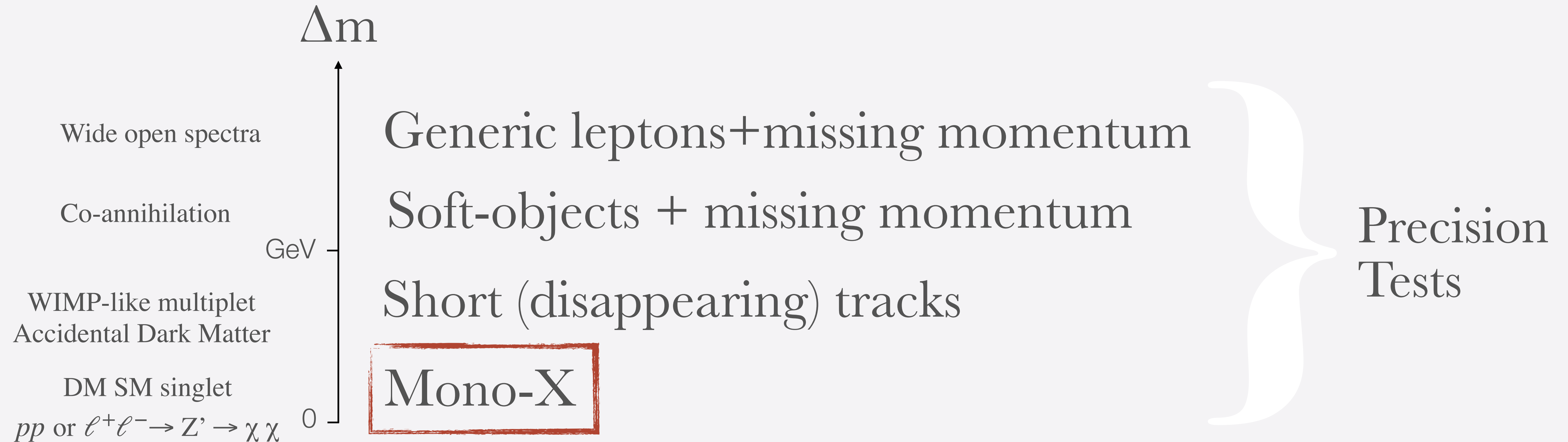
$n = 2$  and  $n = 3$  just inside reach of 100 TeV  $pp$  collider



# DIRECT SIGNALS AT COLLIDERS

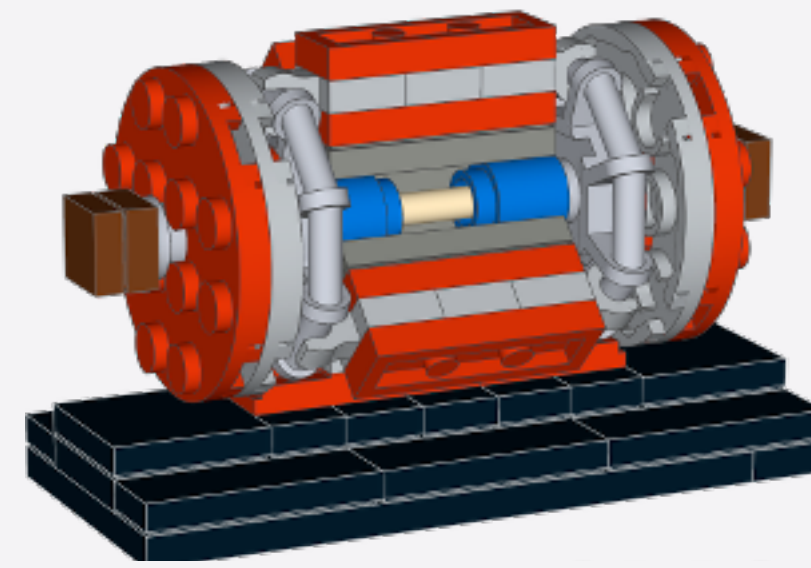


# DIRECT SIGNALS AT COLLIDERS





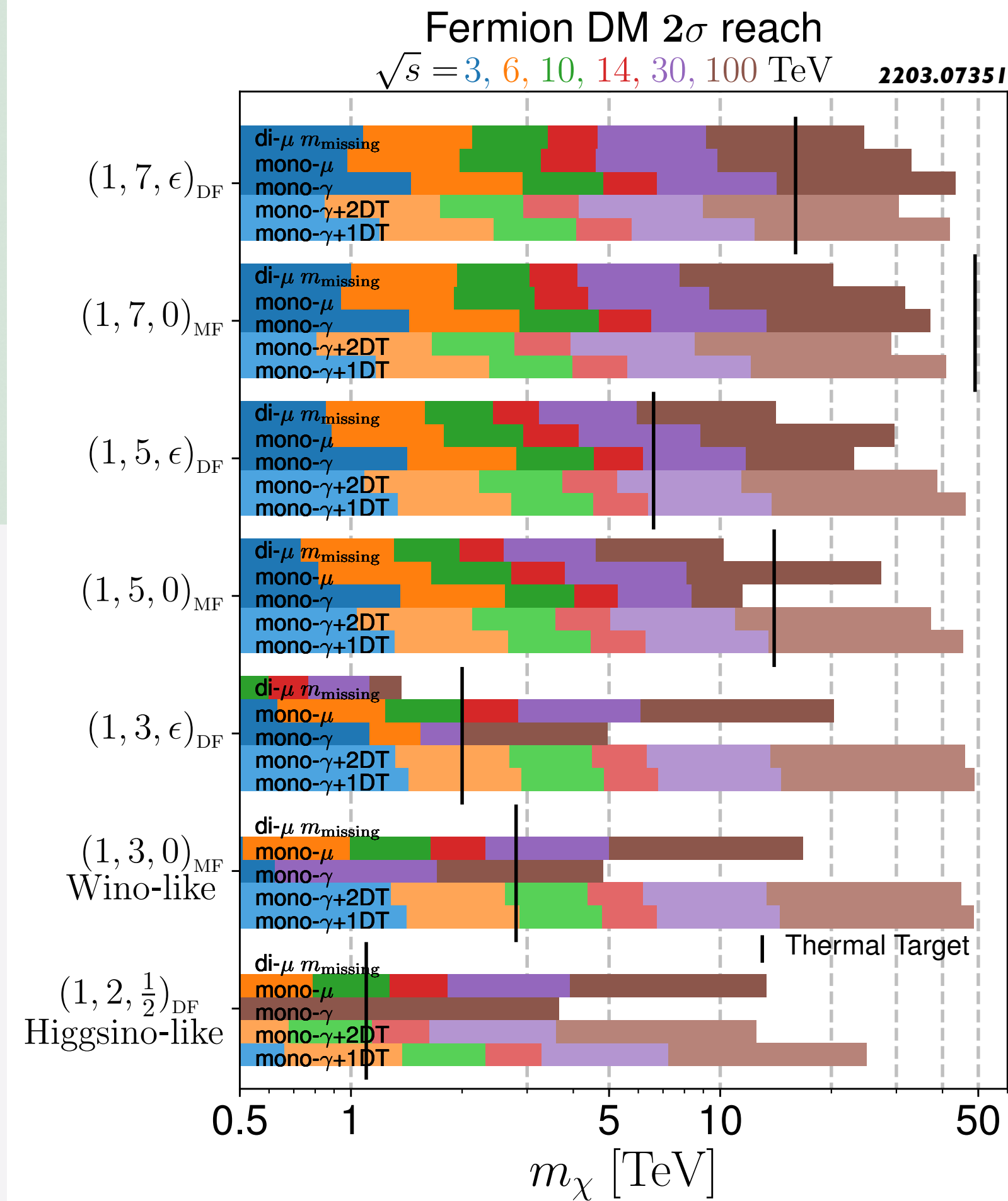
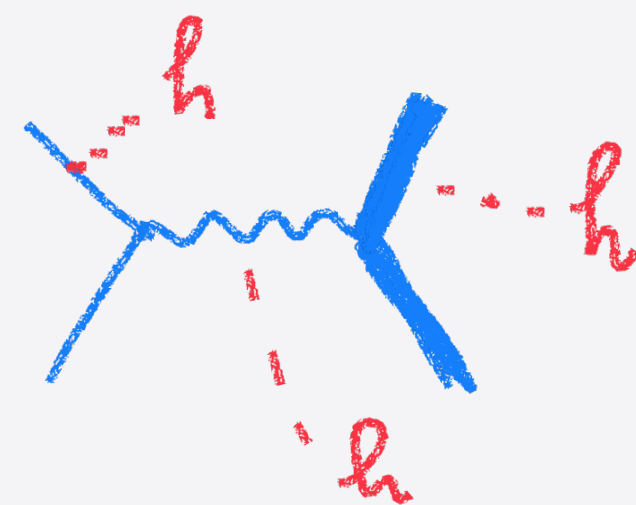
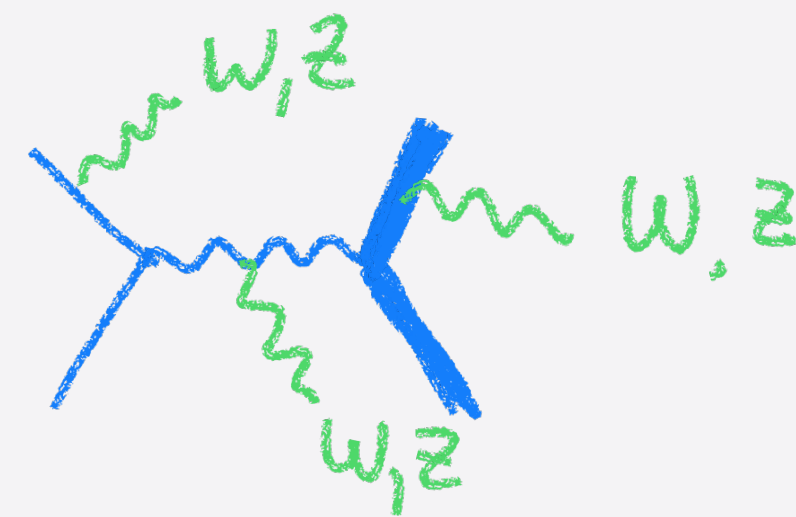
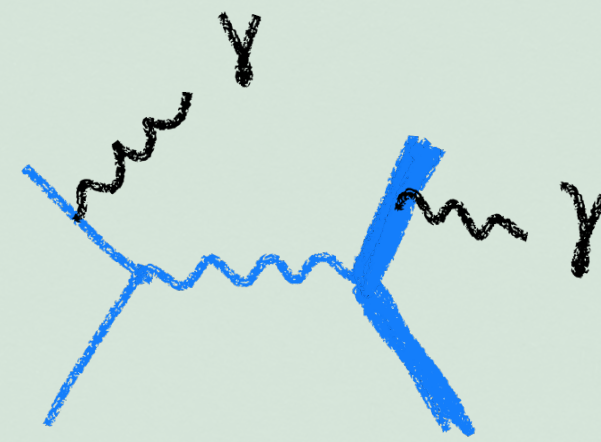
# MONO-X



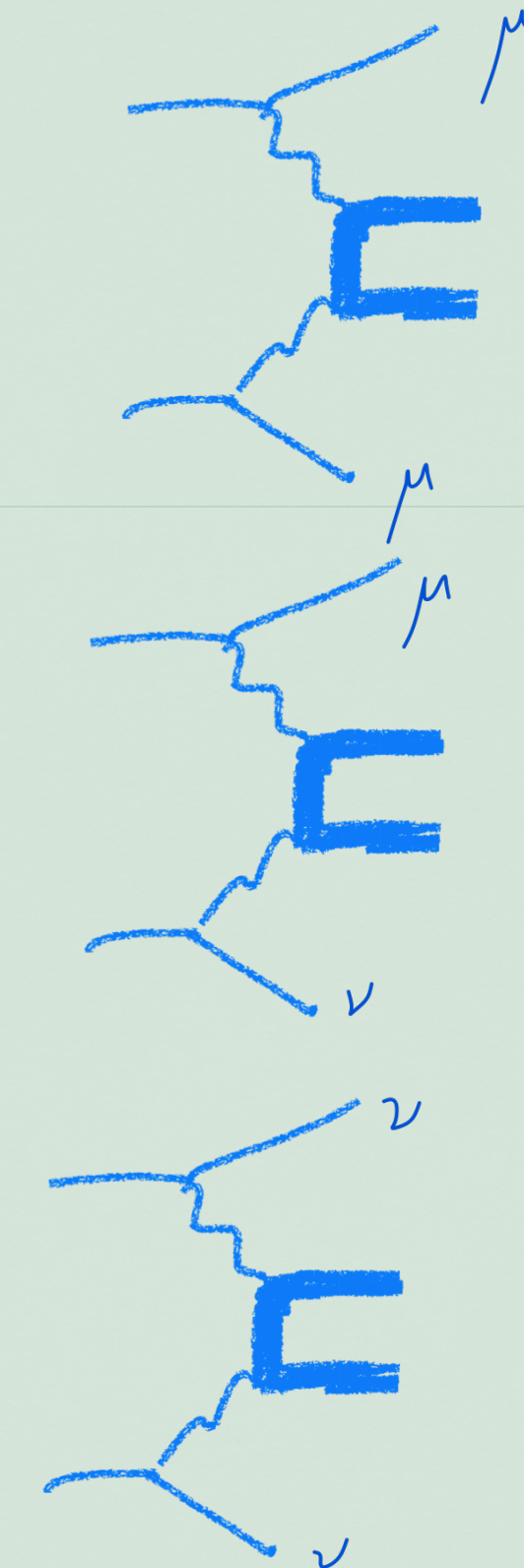
# 2040s

up to 10+ TeV

Sensitive up to mass comparable to the center of mass of  $\mu^+\mu^-$

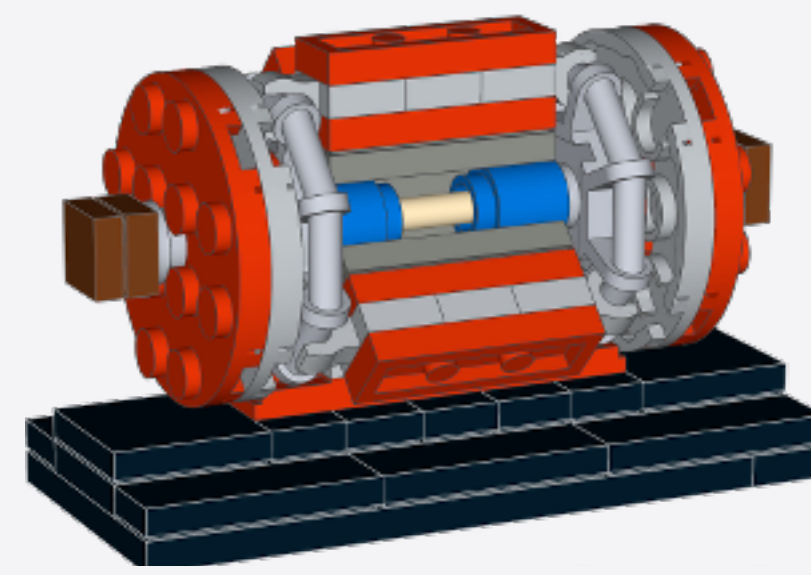


Excellent for low mass compared to the center of mass of  $\mu^+\mu^-$





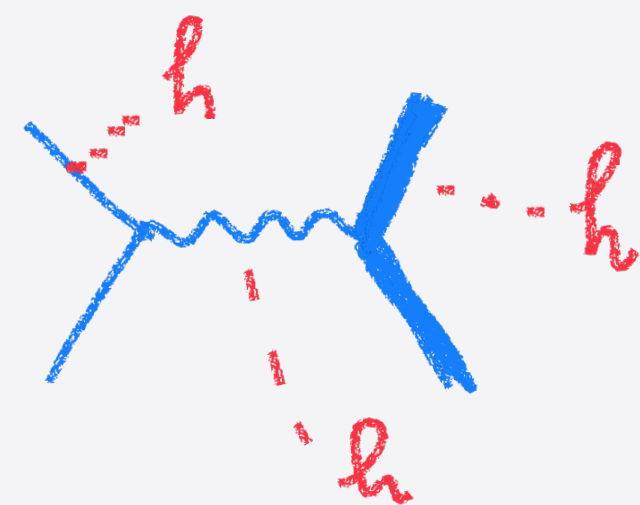
# MONO-X



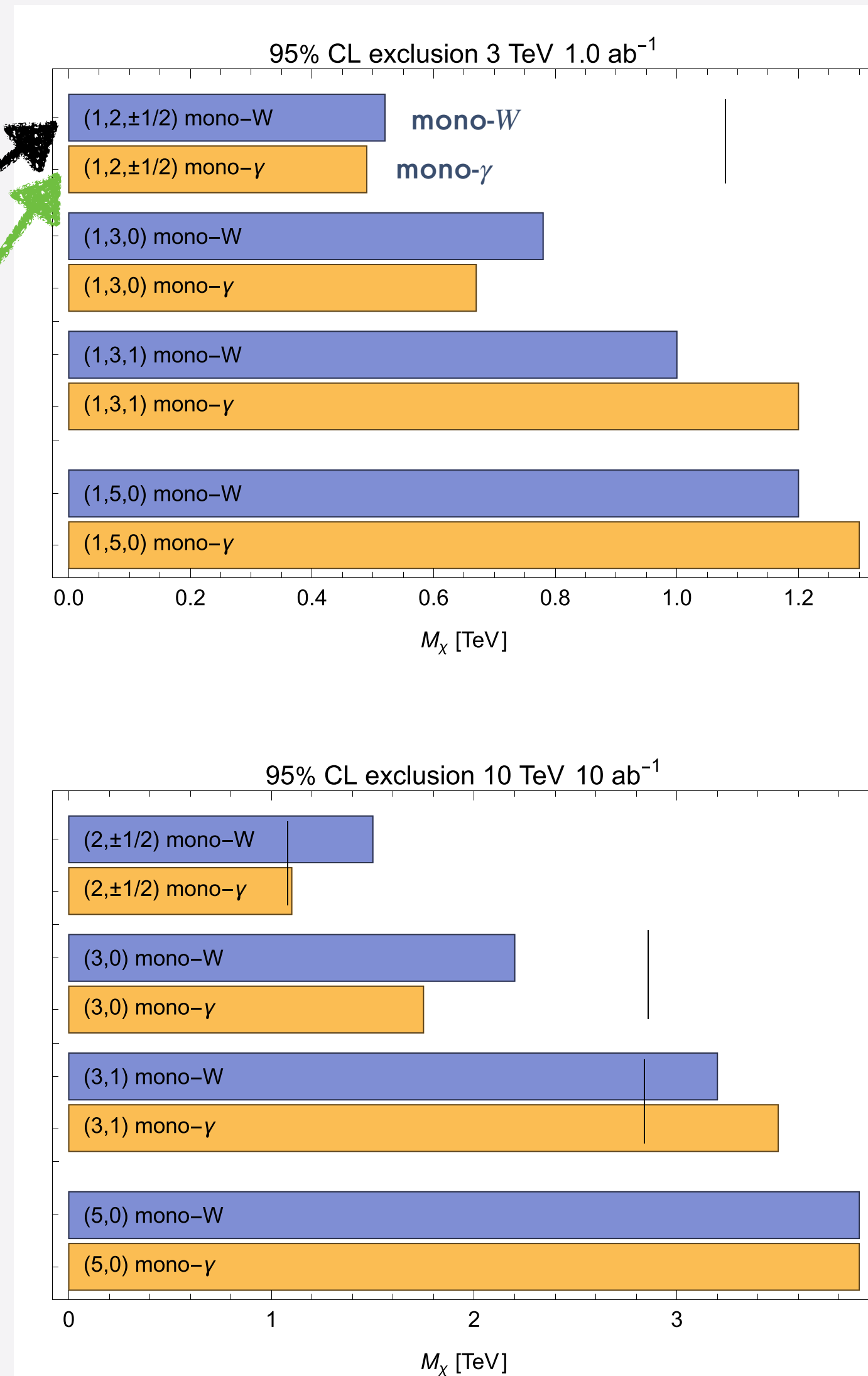
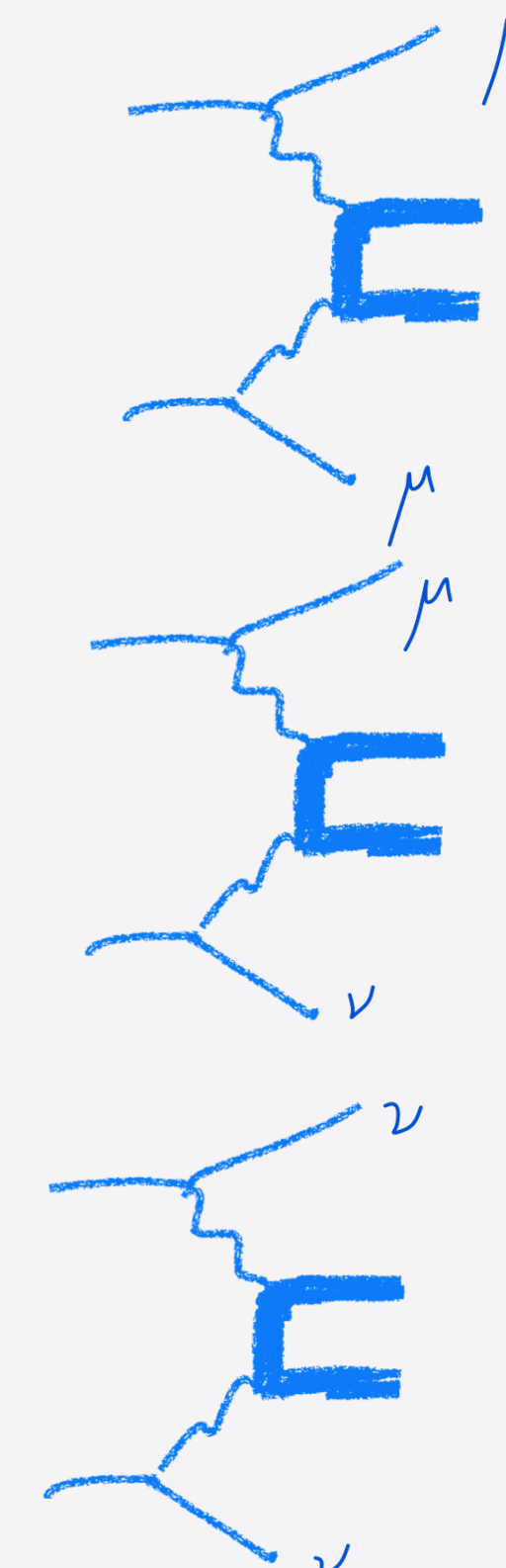
# 2040s

up to 10+ TeV

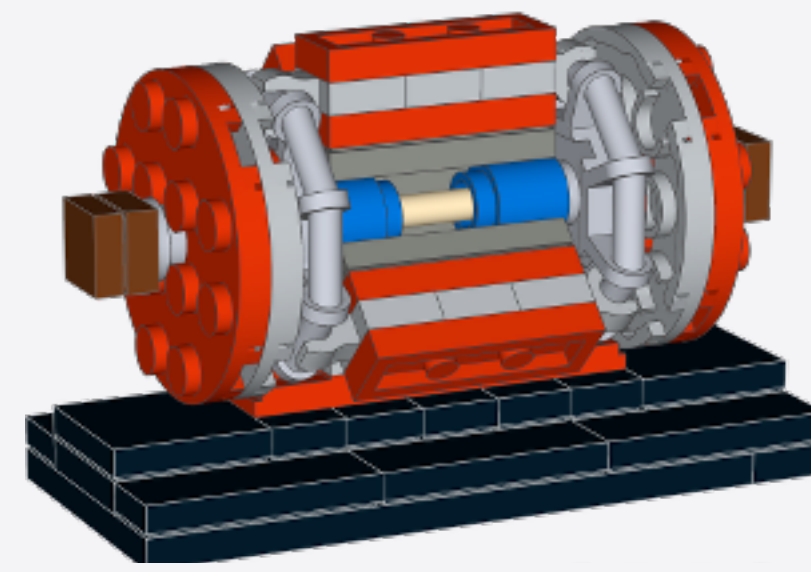
Sensitive up to mass comparable to the center of mass of  $\mu^+\mu^-$



Excellent for low mass compared to the center of mass of  $\mu^+\mu^-$



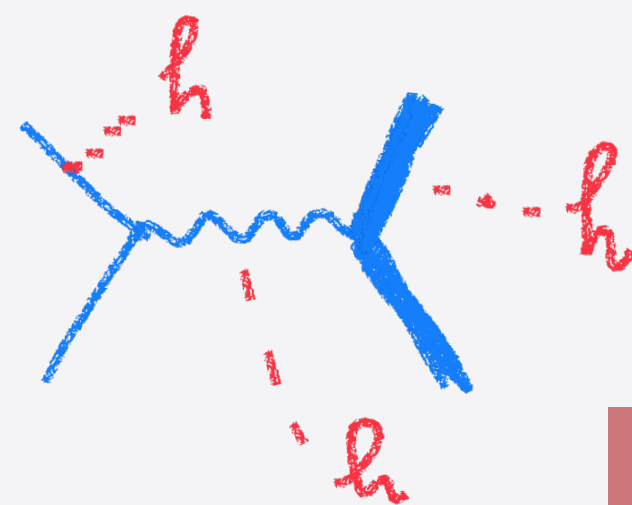
# MONO-X



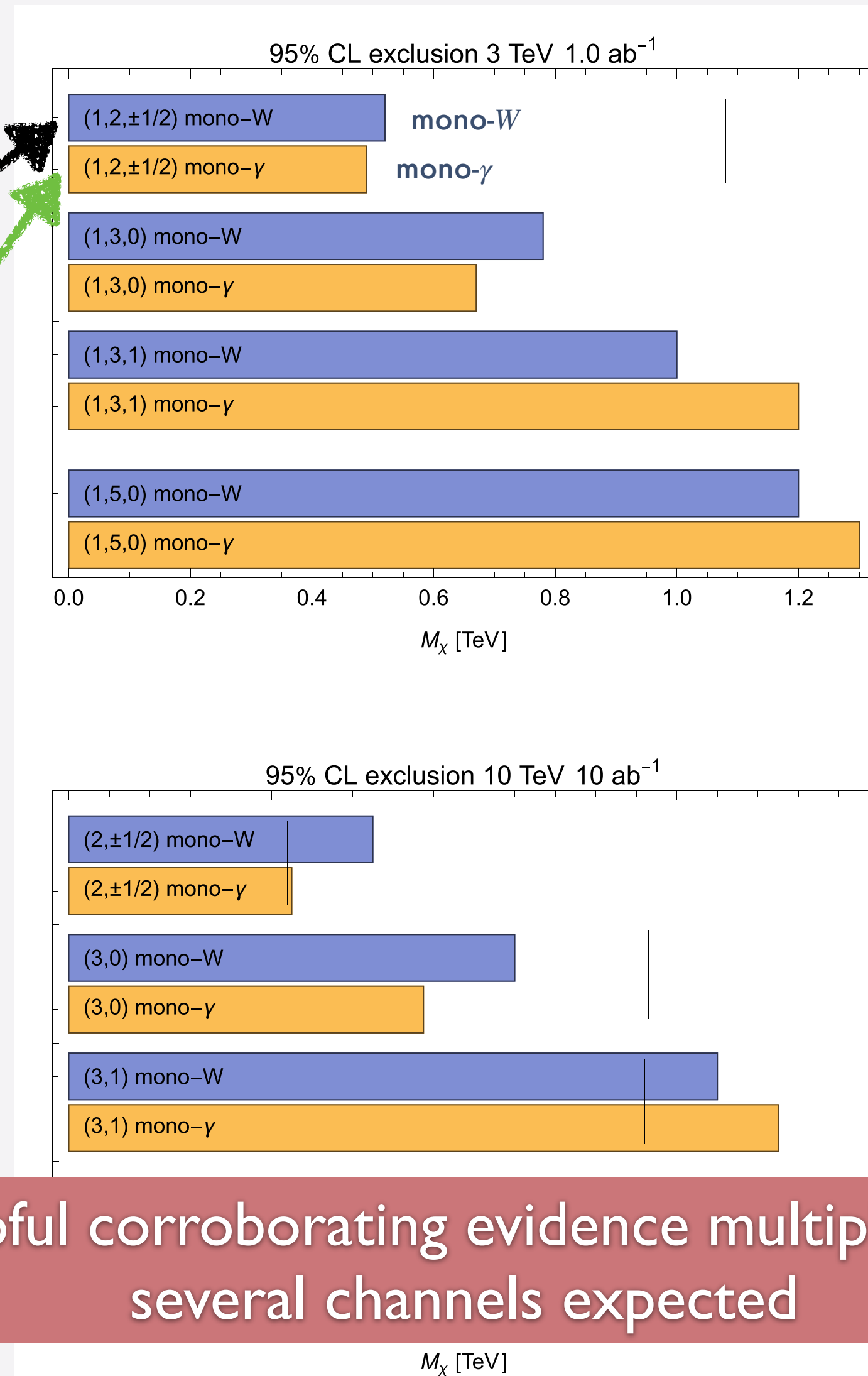
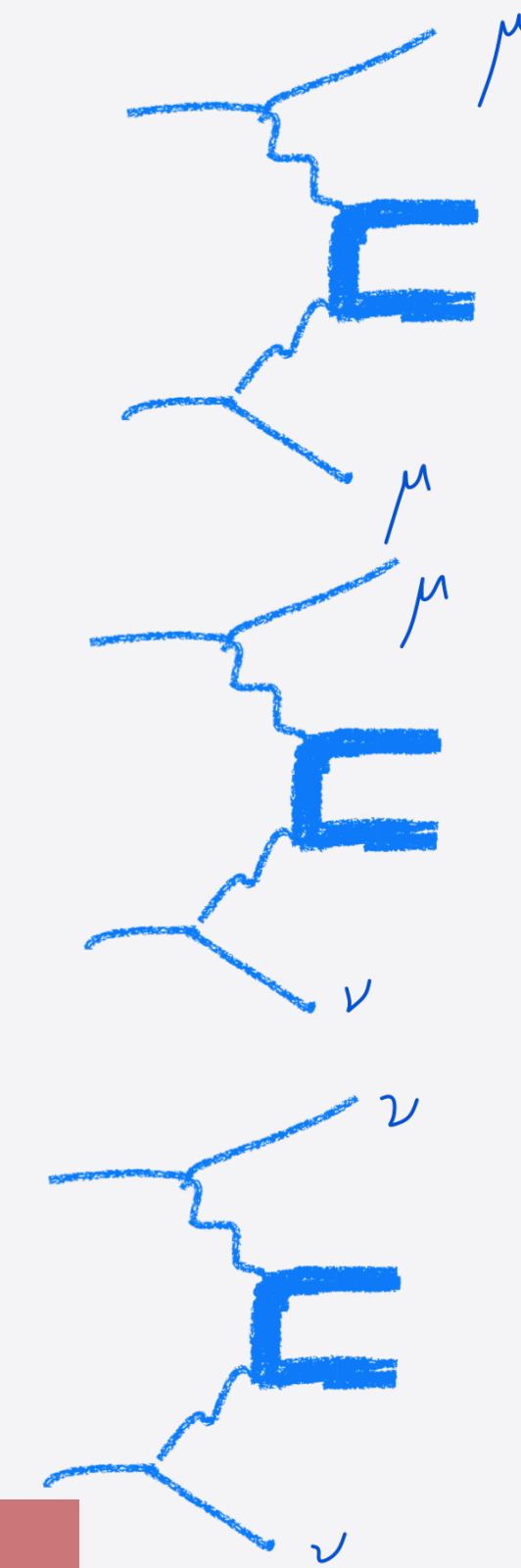
# 2040s

up to 10+ TeV

Sensitive up to mass comparable to the center of mass of  $\mu^+\mu^-$



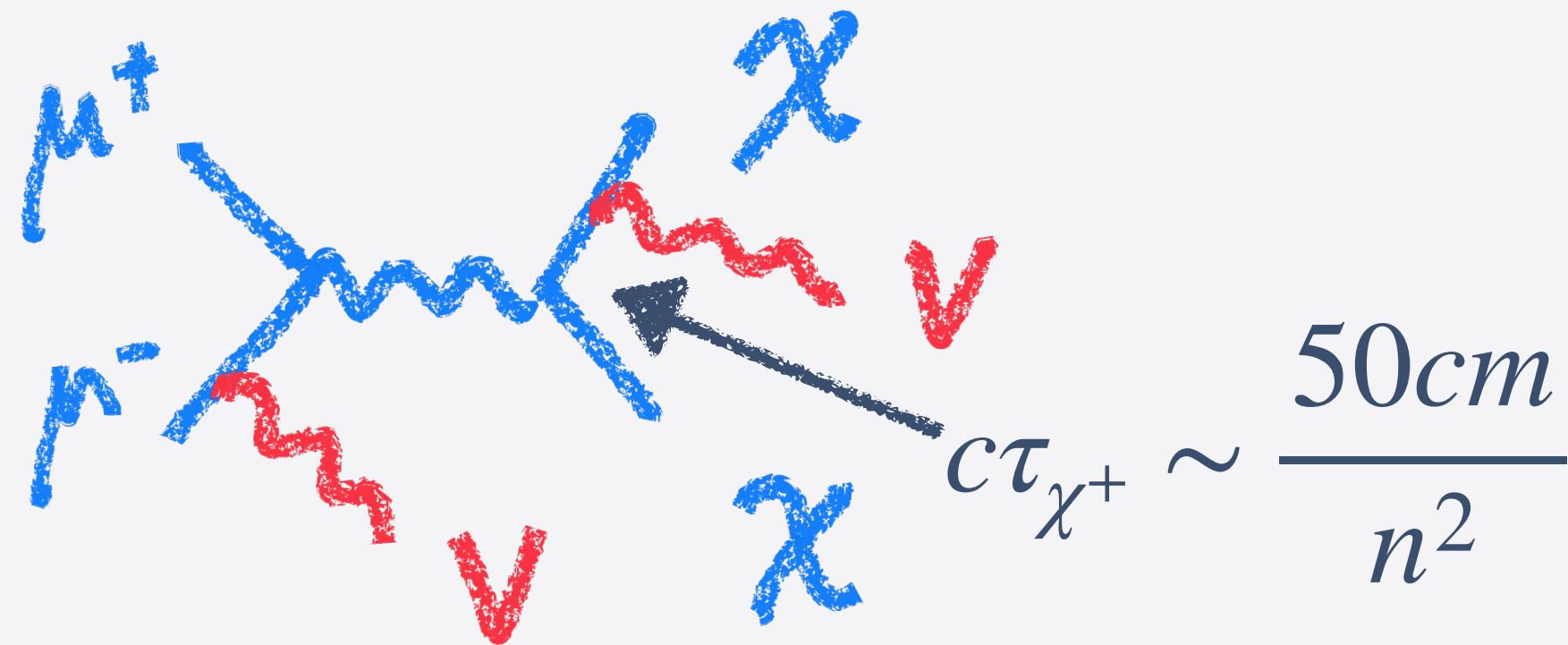
Excellent for low mass compared to the center of mass of  $\mu^+\mu^-$



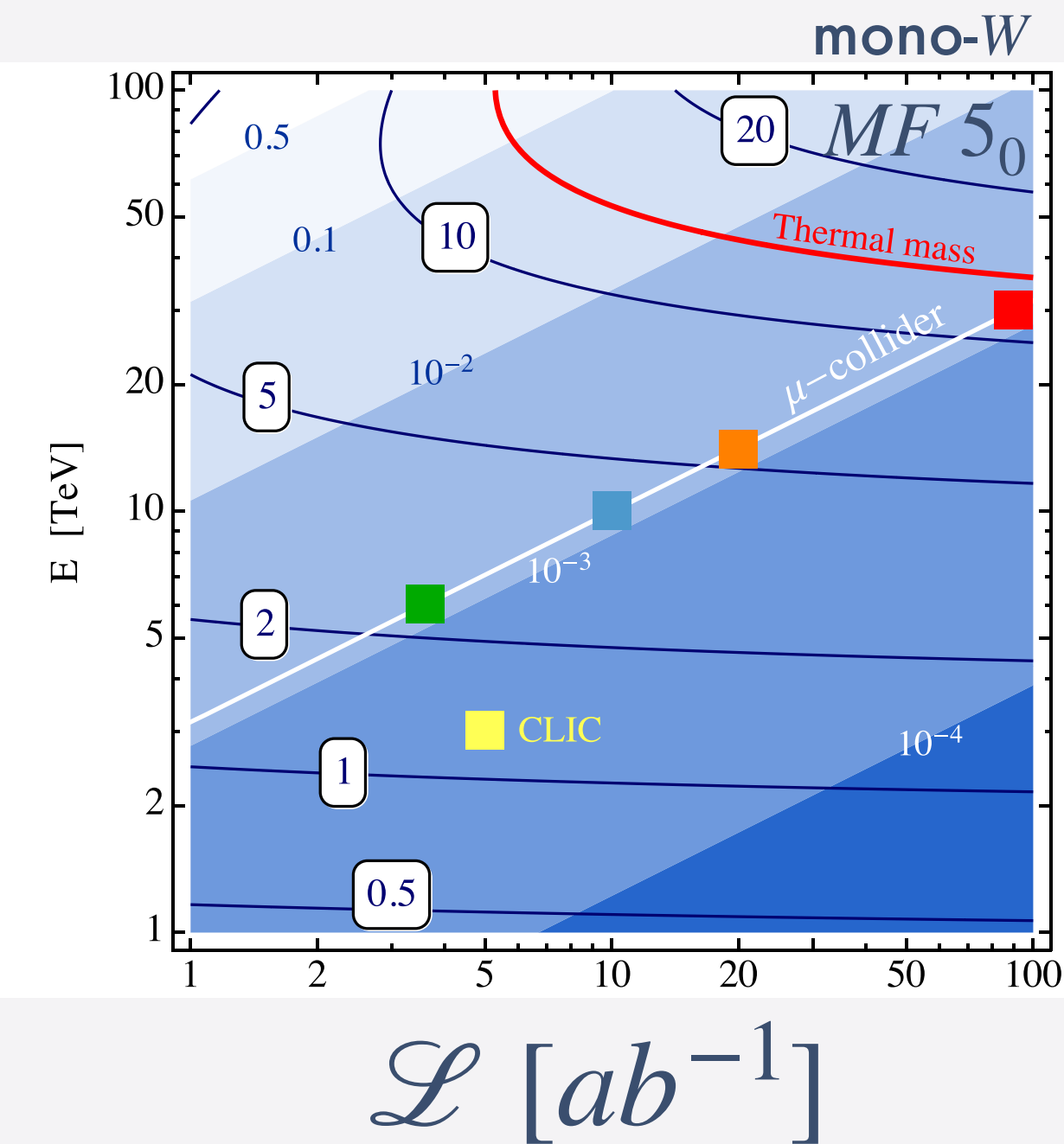
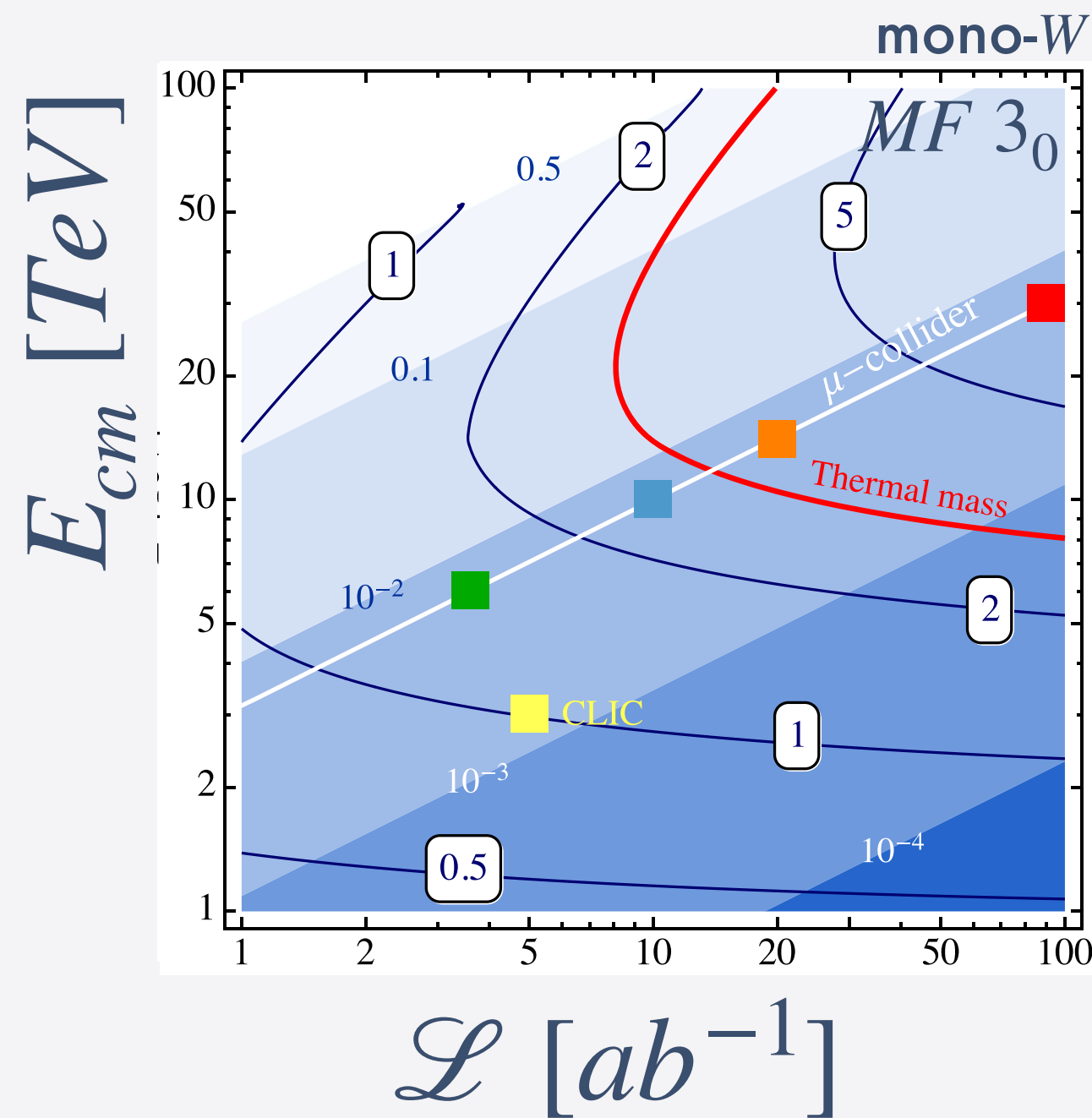
very helpful corroborating evidence multiple signals in several channels expected



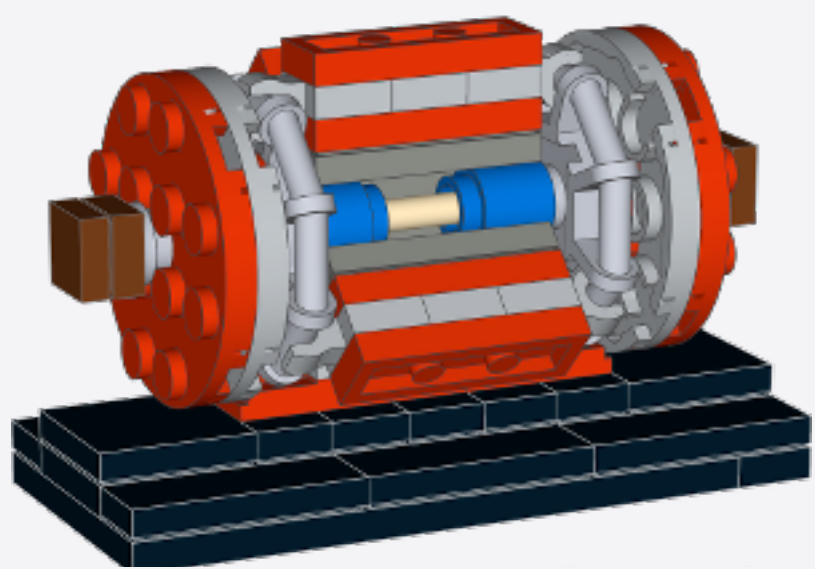
# DIRECT PRODUCTION



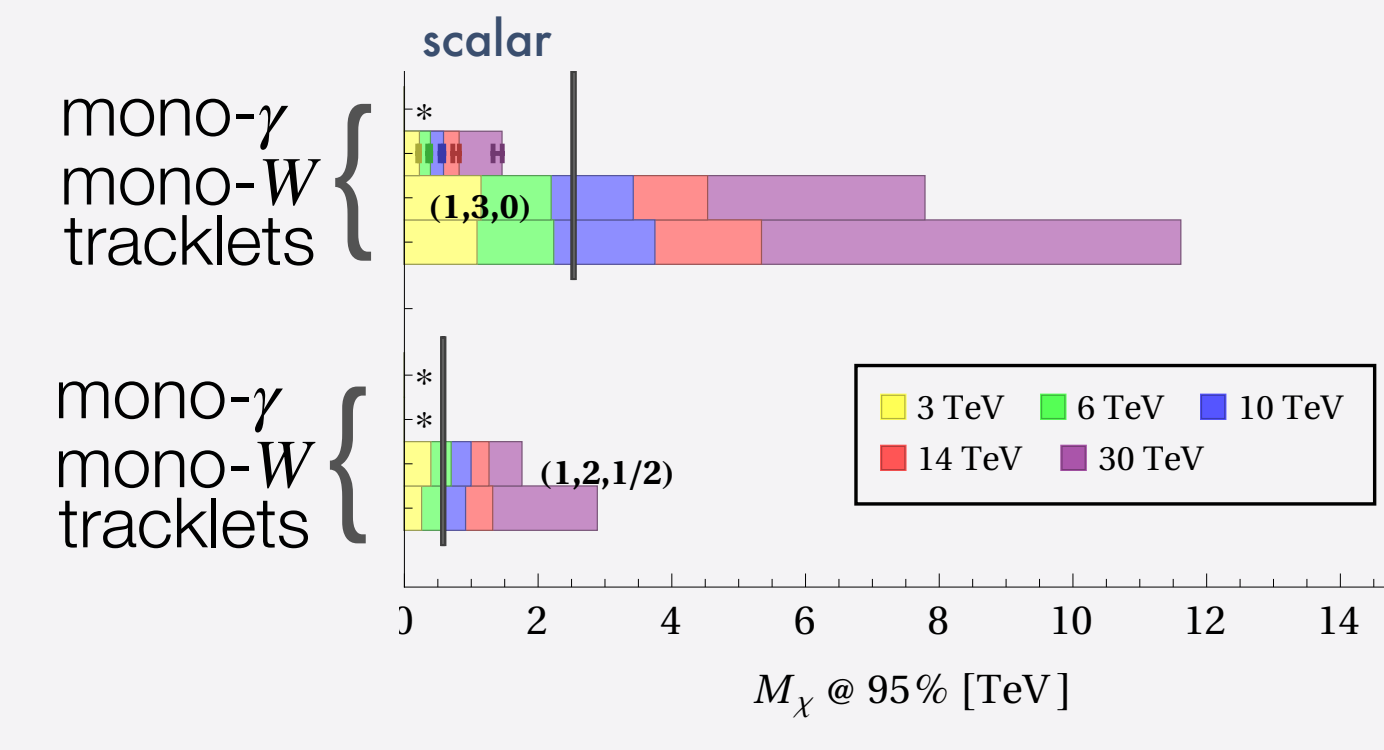
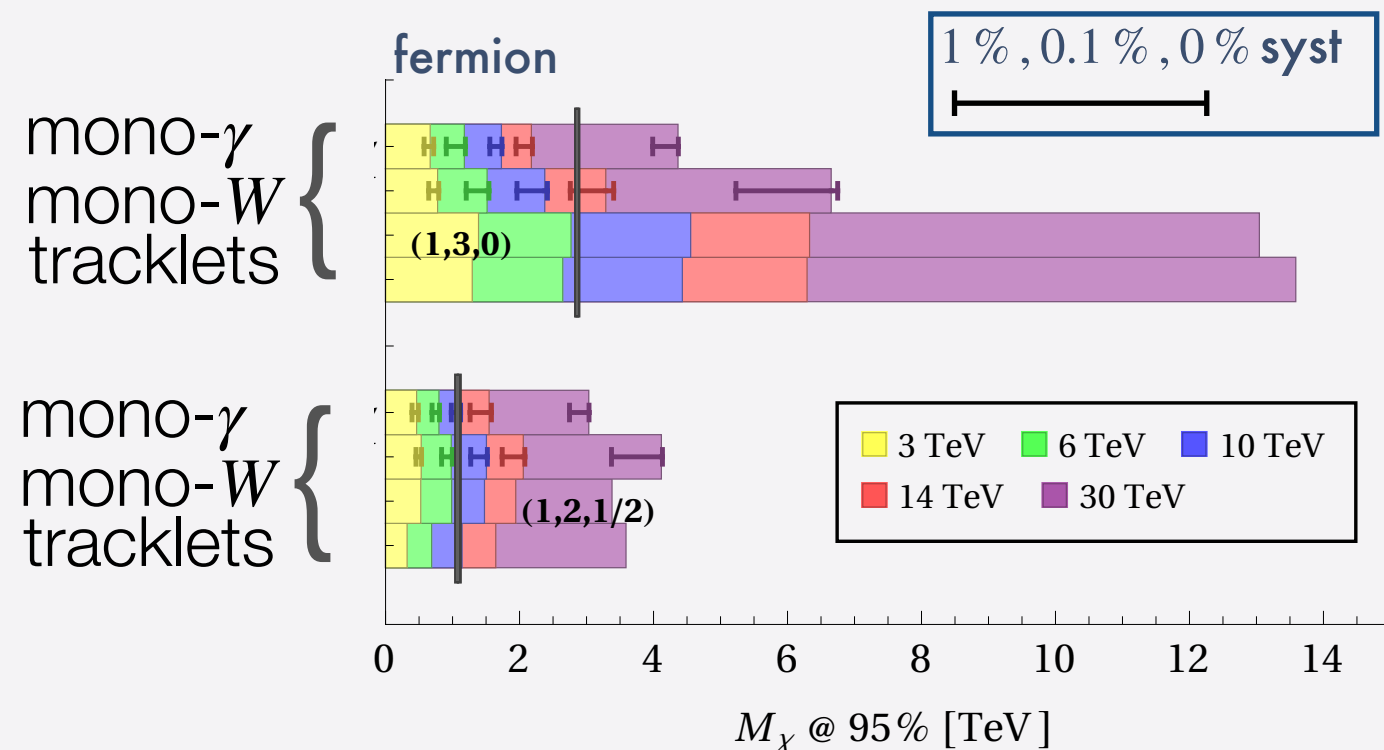
Production of Dark Matter weak multiplet states and observation of the decay products or associated productions



very helpful corroborating evidence multiple signals in several channels expected

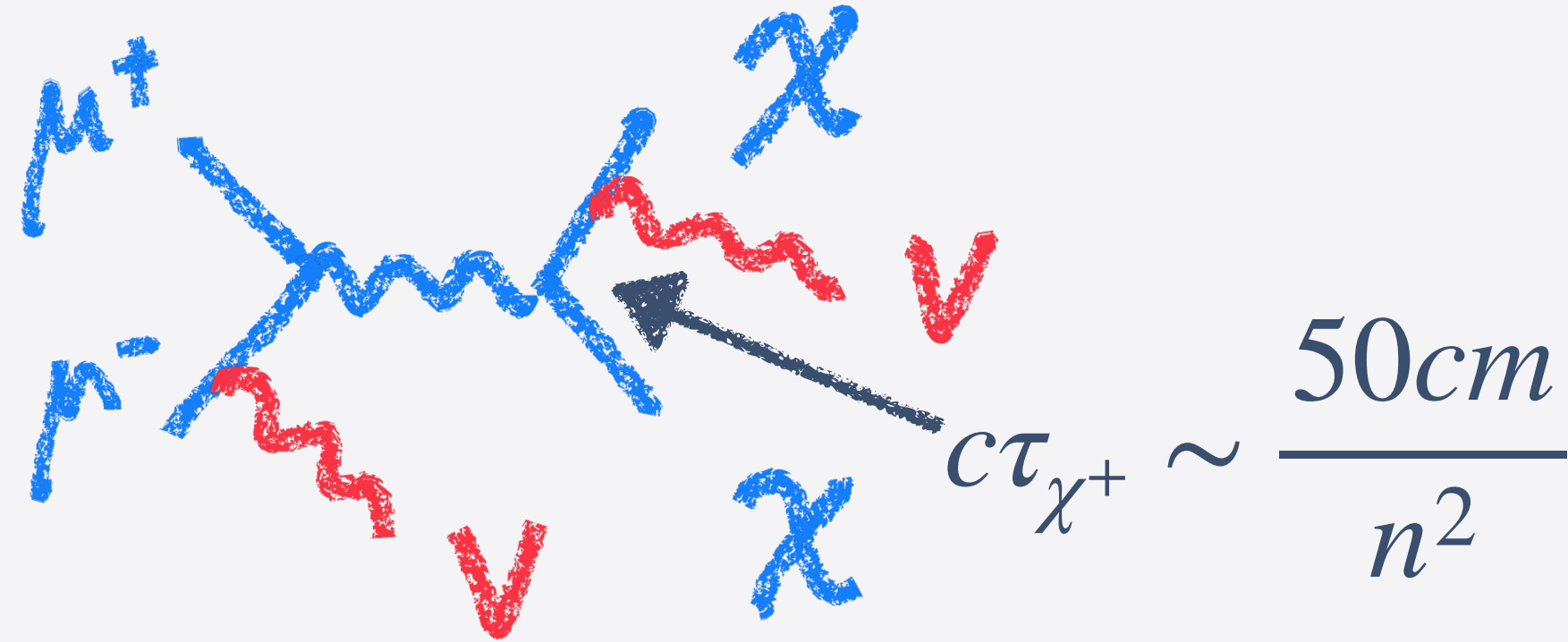


**2040s**  
up to 10+ TeV

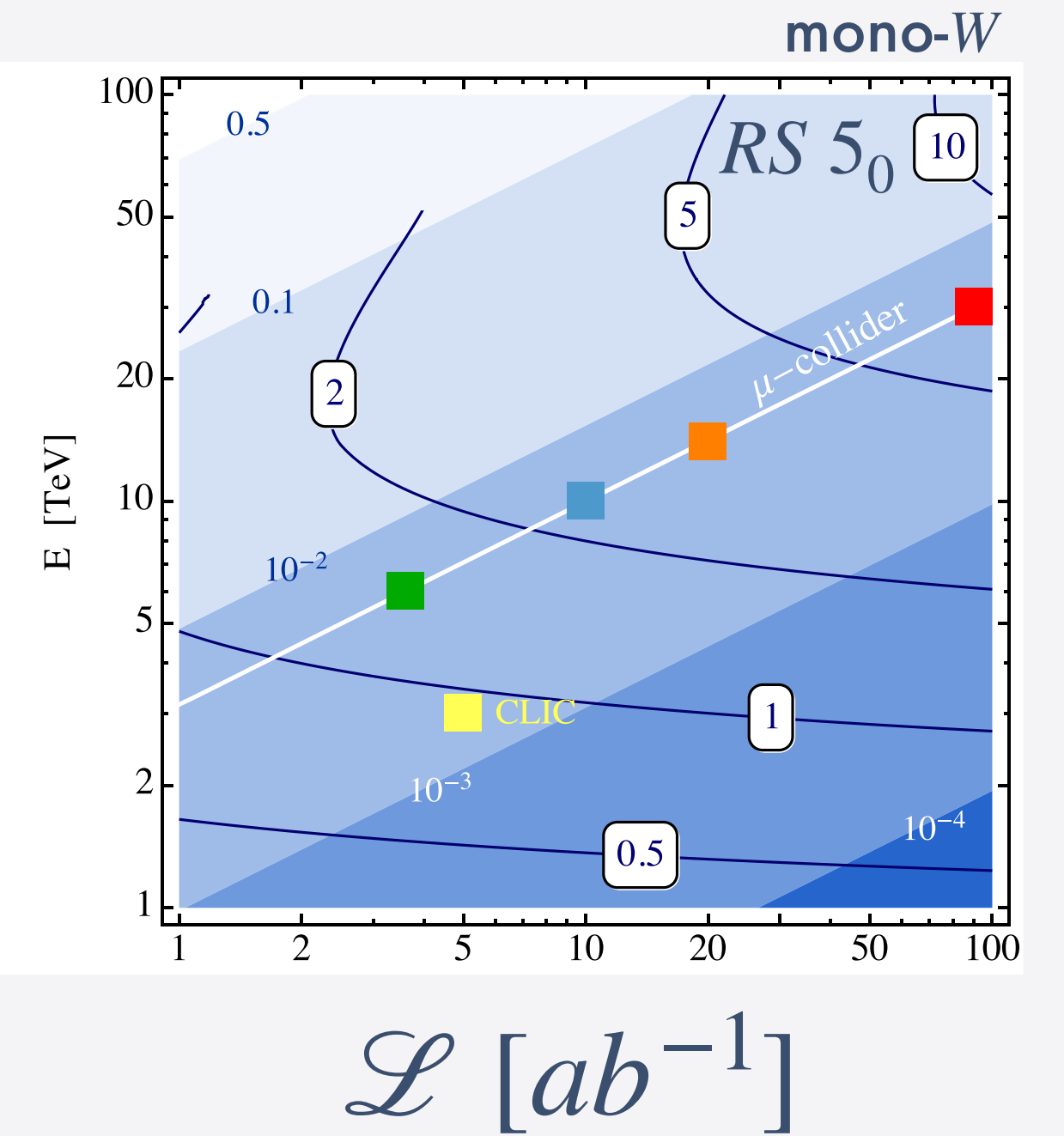
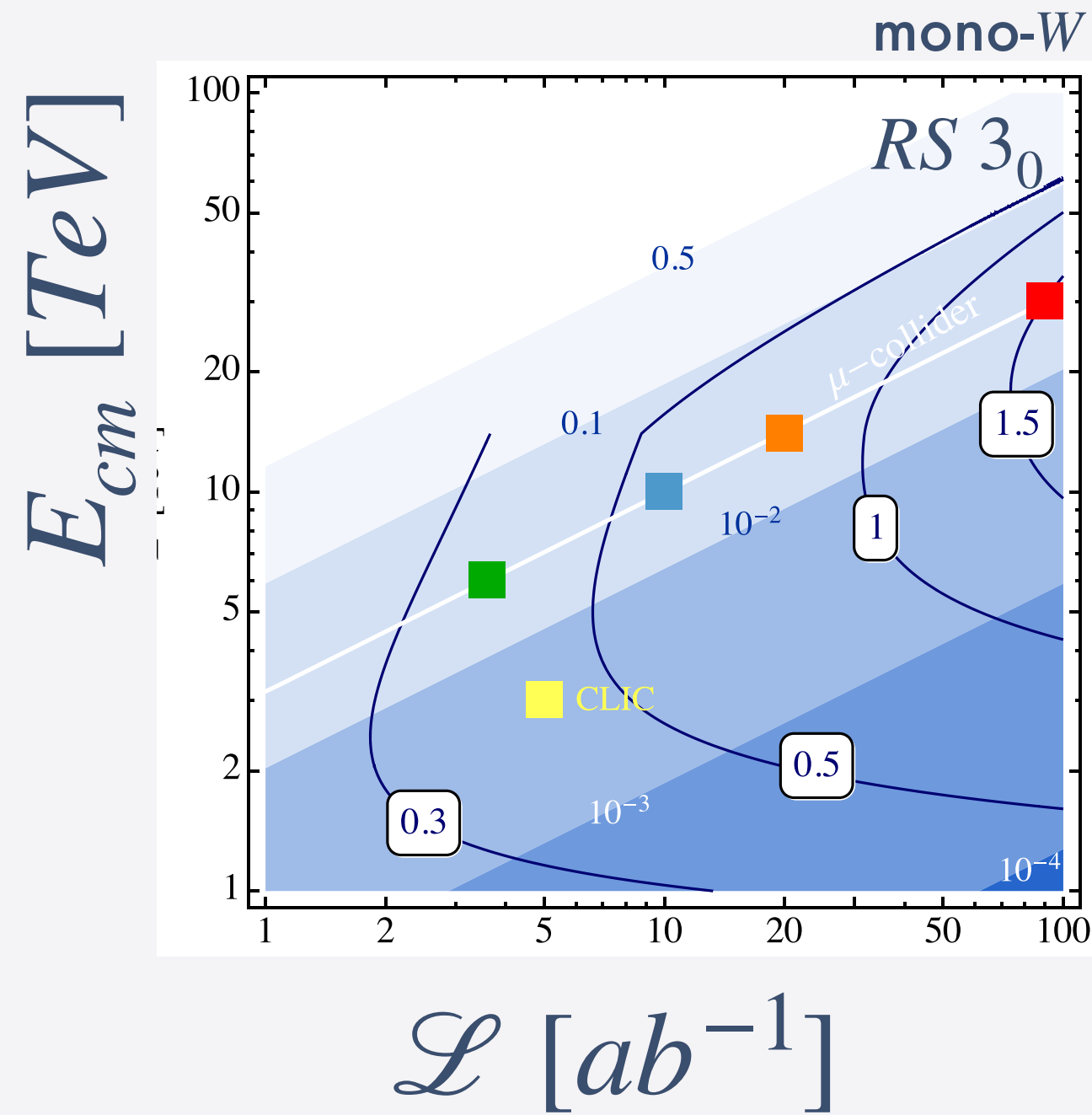




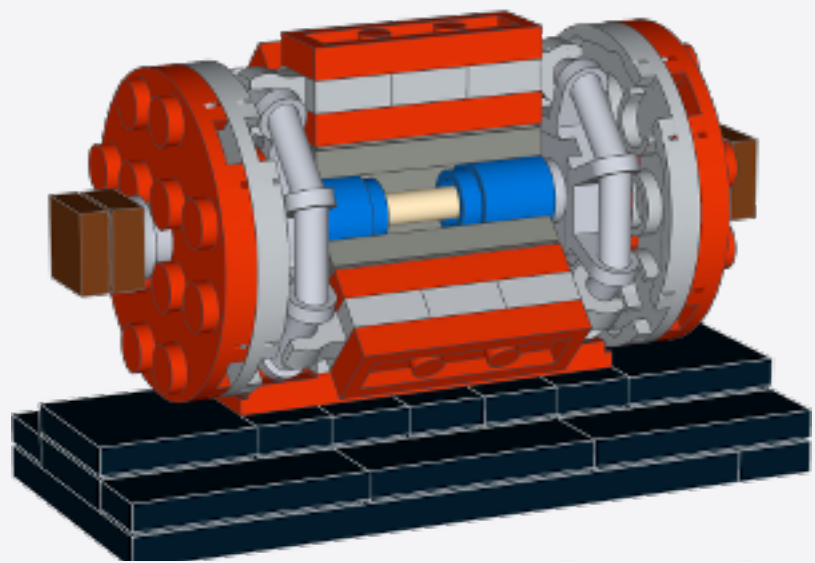
# DIRECT PRODUCTION



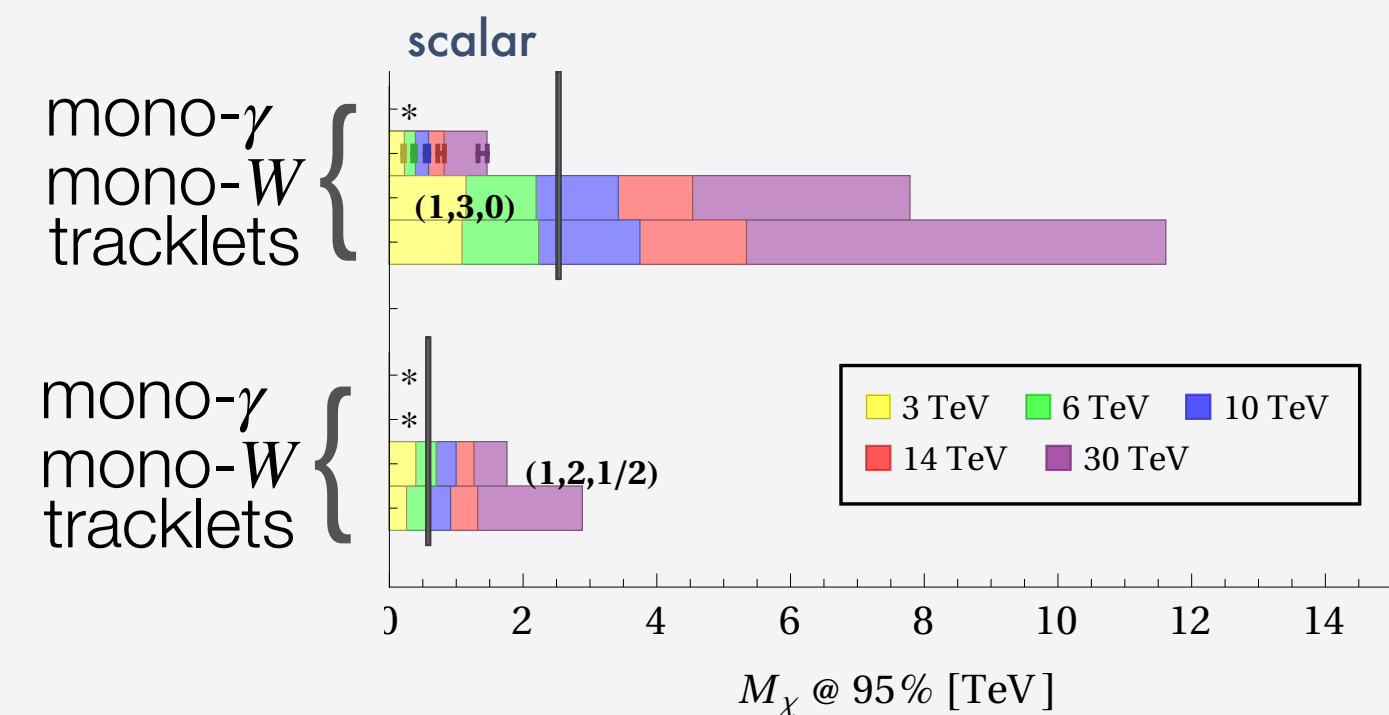
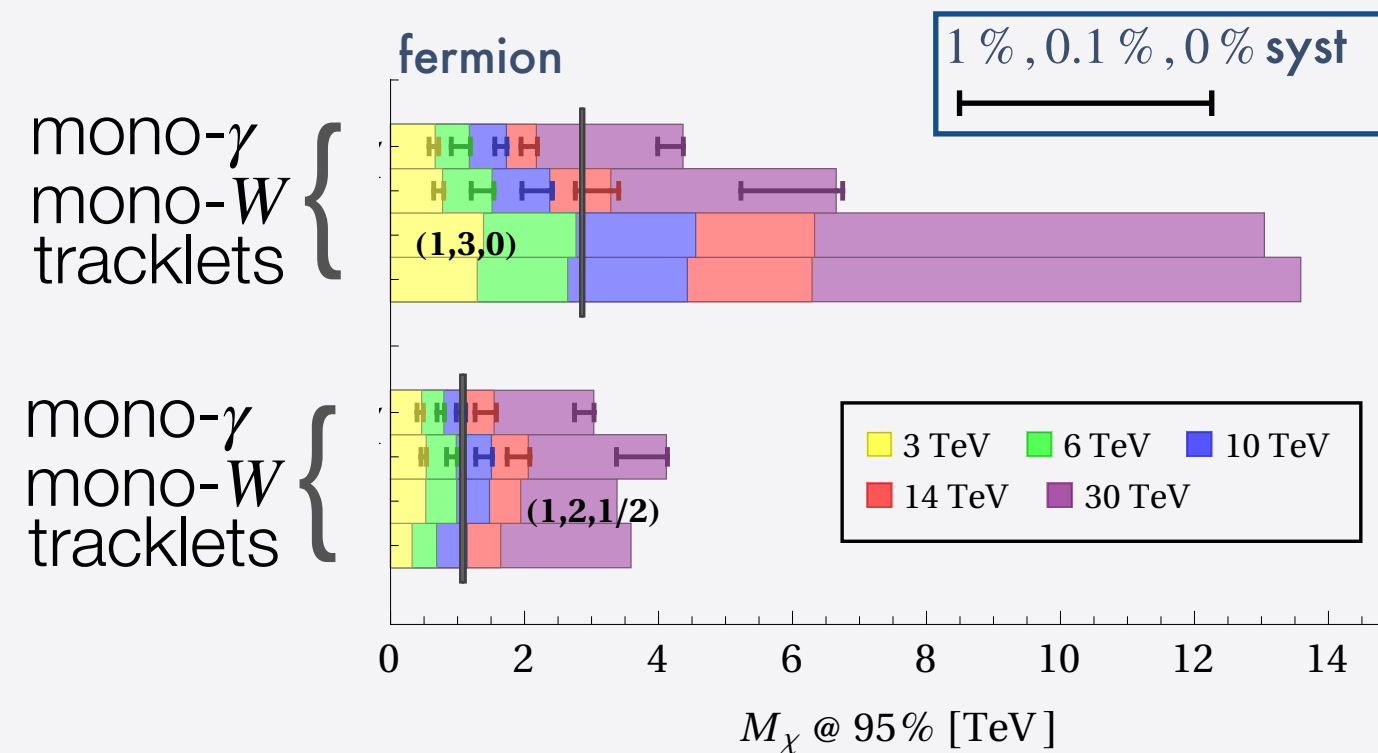
Production of Dark Matter weak multiplet states and observation of the decay products or associated productions



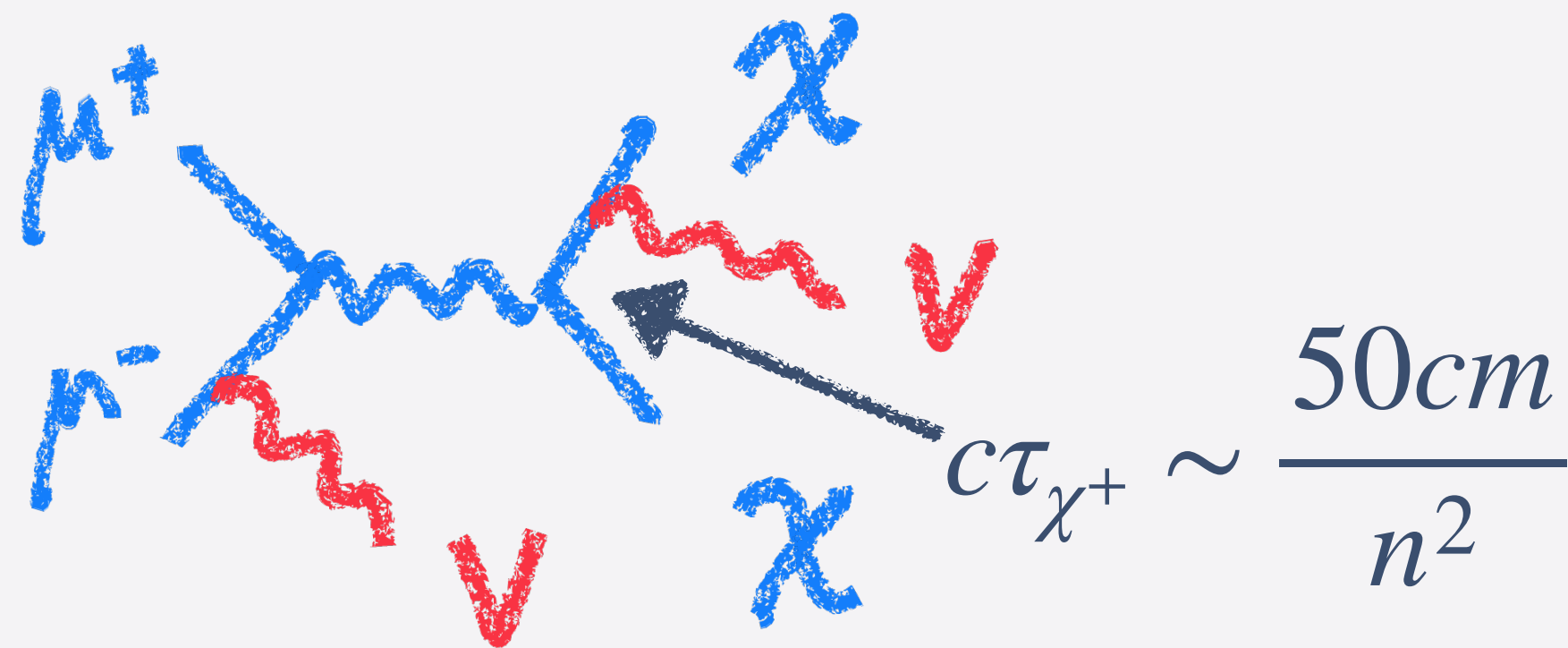
very helpful corroborating evidence multiple signals in several channels expected



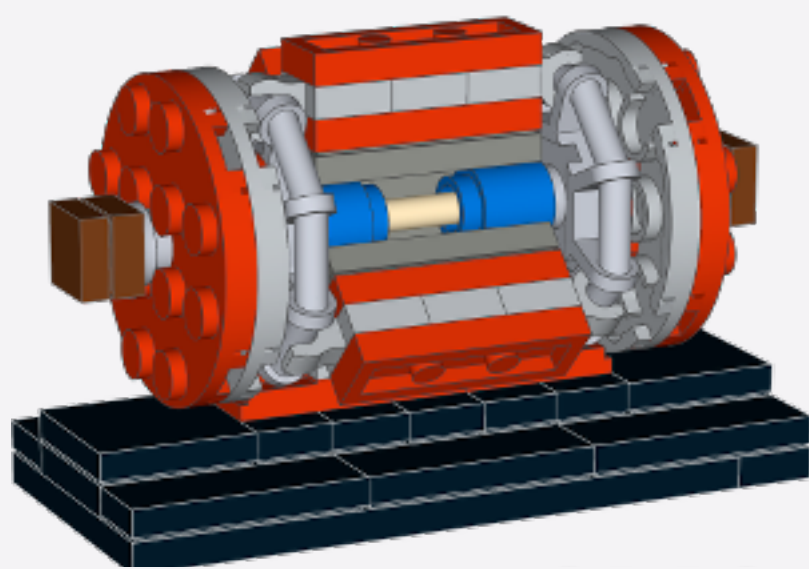
2040s  
up to 10+ TeV



# DIRECT PRODUCTION



Production of Dark Matter weak multiplet states and observation of the decay products or associated productions

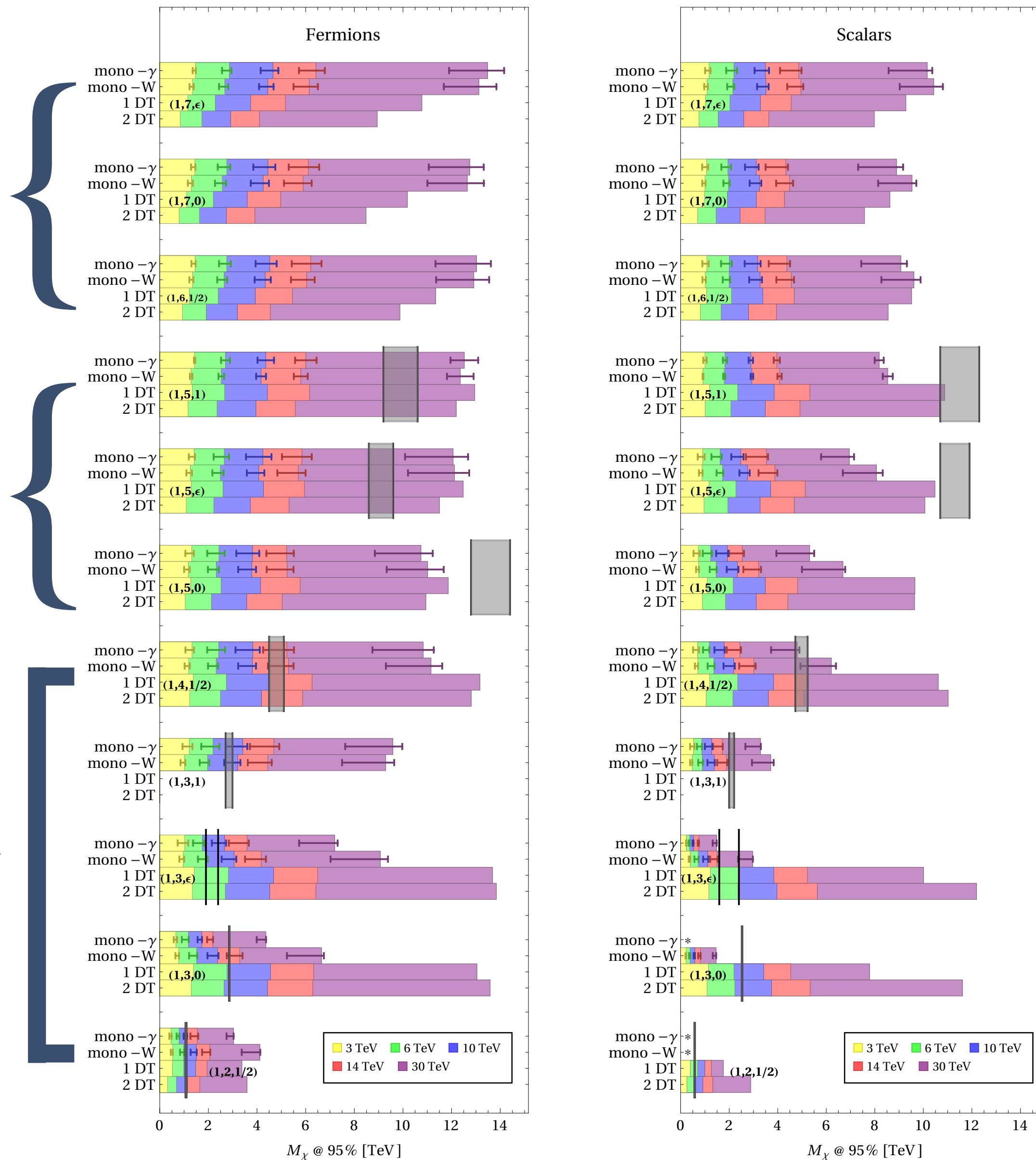


**2040s**  
up to 10+ TeV

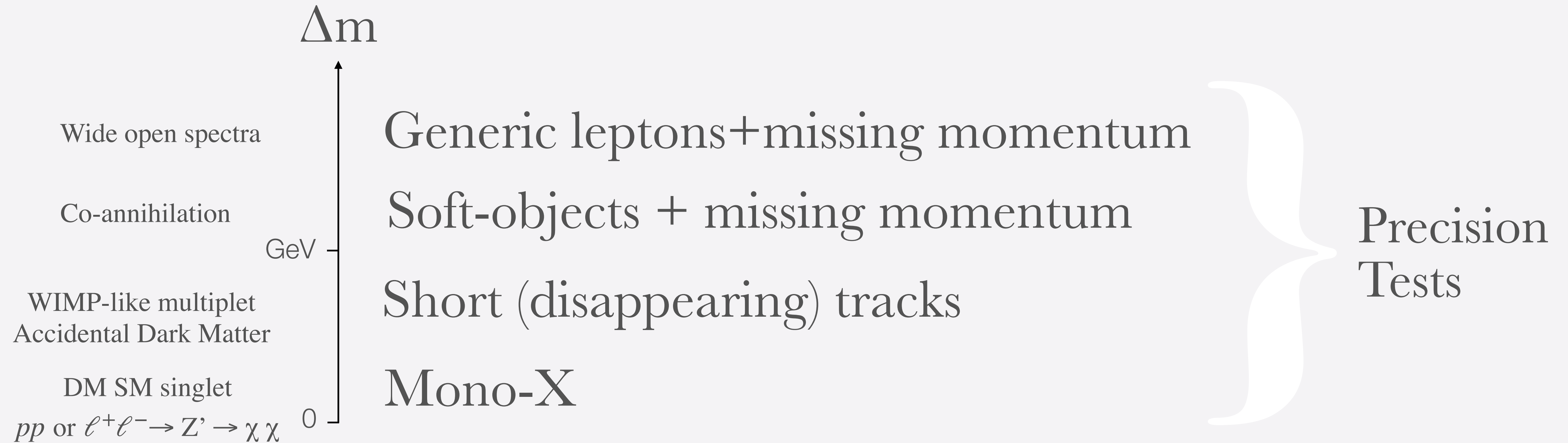
$M_7 \sim 50 \text{ TeV}$

$M_5 \sim 15 \text{ TeV}$

$M_2, M_3, M_4 \leq 5 \text{ TeV}$

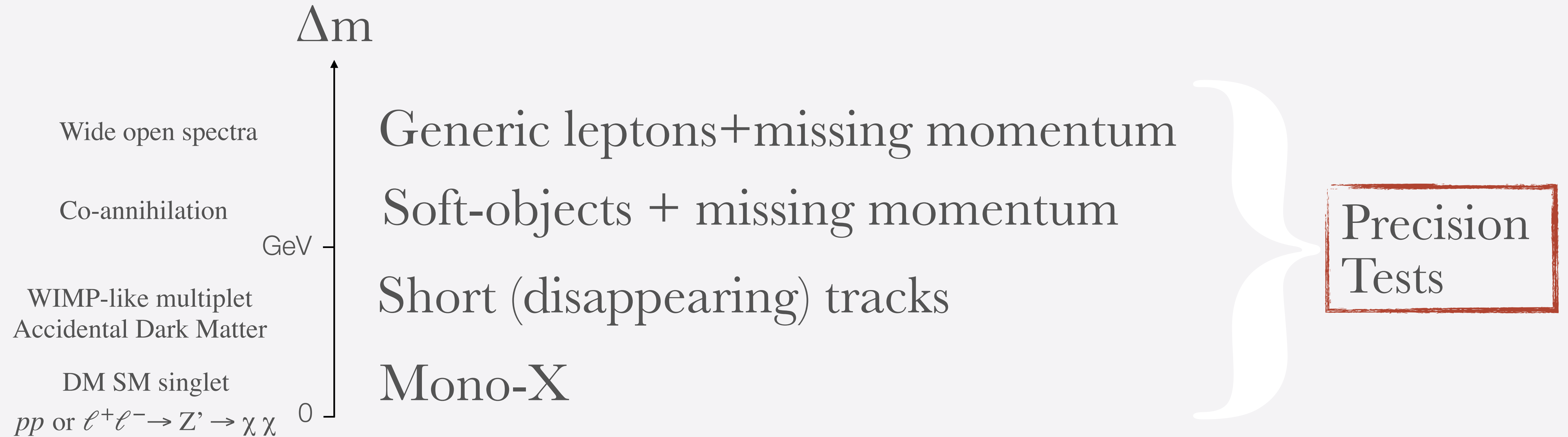


# DIRECT SIGNALS AT COLLIDERS



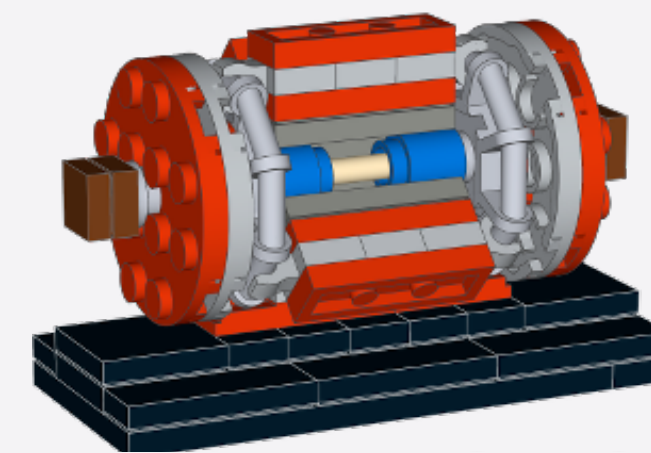


# DIRECT SIGNALS AT COLLIDERS



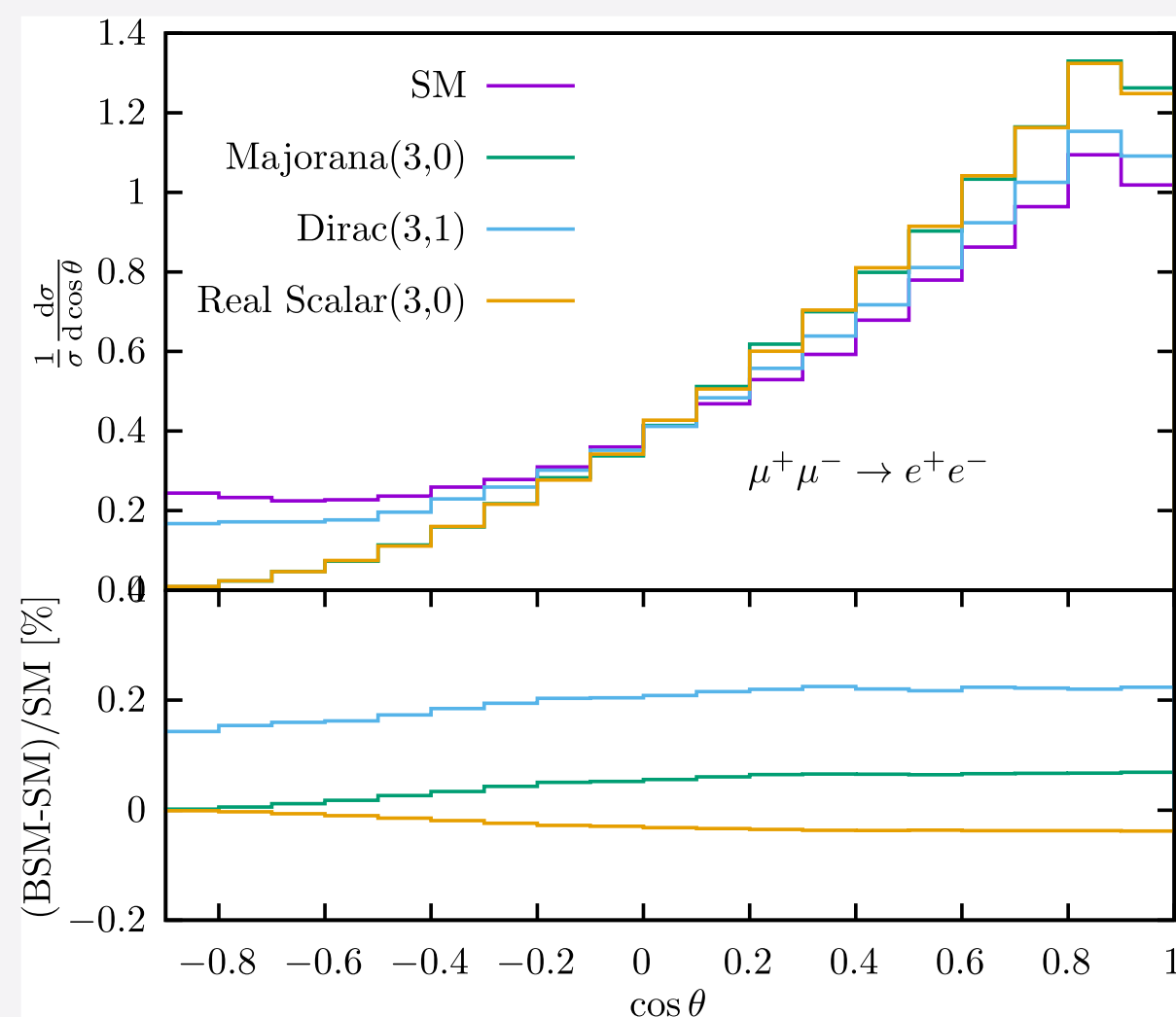
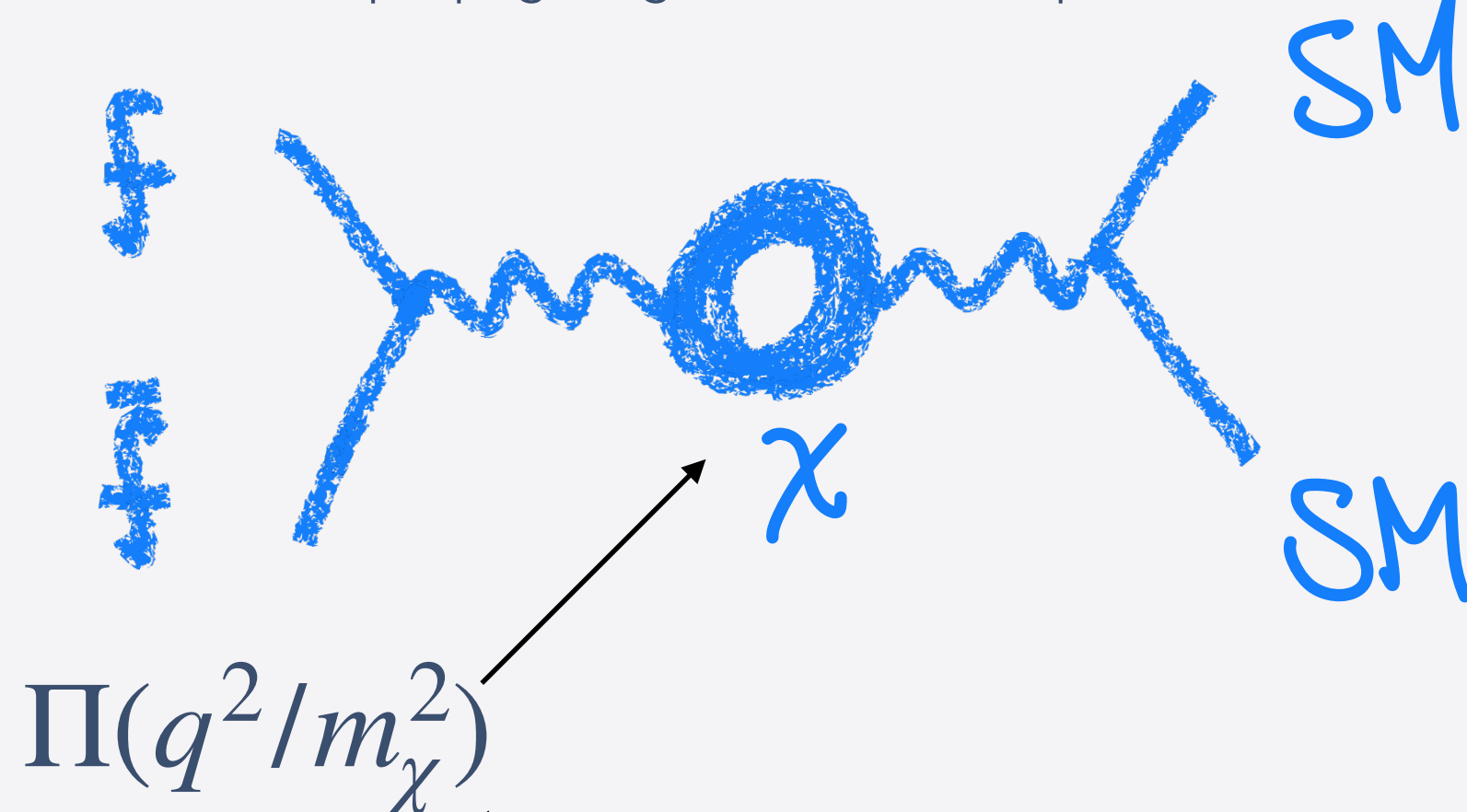
# VIRTUAL\* PRODUCTION

## *s*-channel and *t*-channel



2040s  
up to 10+ TeV

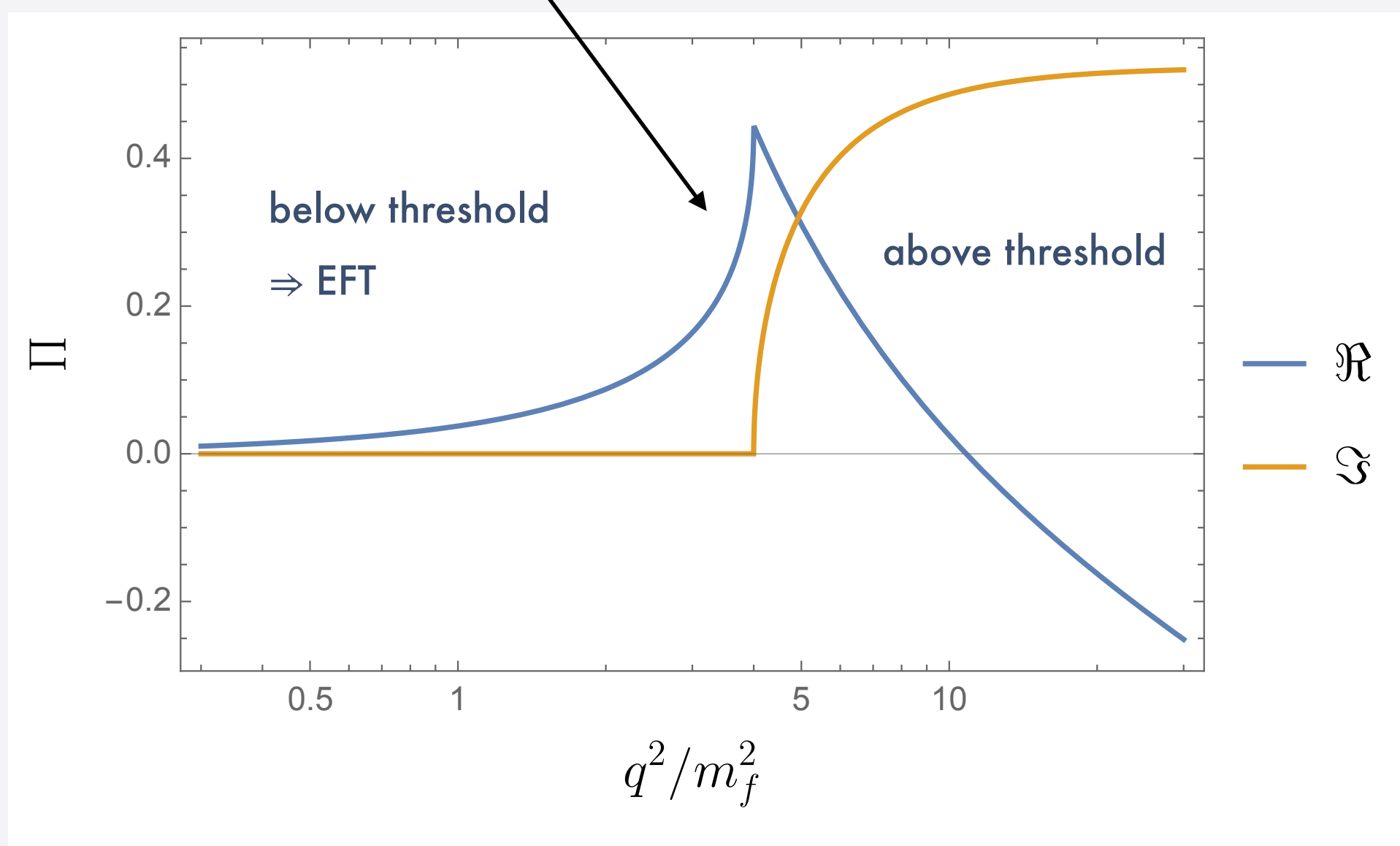
Virtual or propagating DM affects SM production rates



$$SM \subset ff$$

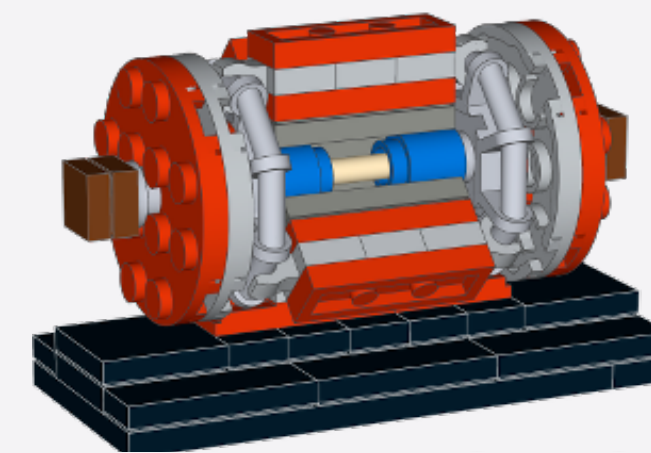
$$\ell^+ \ell^- \rightarrow e^+ e^-, b\bar{b}, \mu^+ \mu^-, c\bar{c}$$

- differential distributions  $\frac{d\sigma}{d\cos\theta^*}$
- differential distributions  $\frac{d\sigma}{d|\cos\theta^*|}$



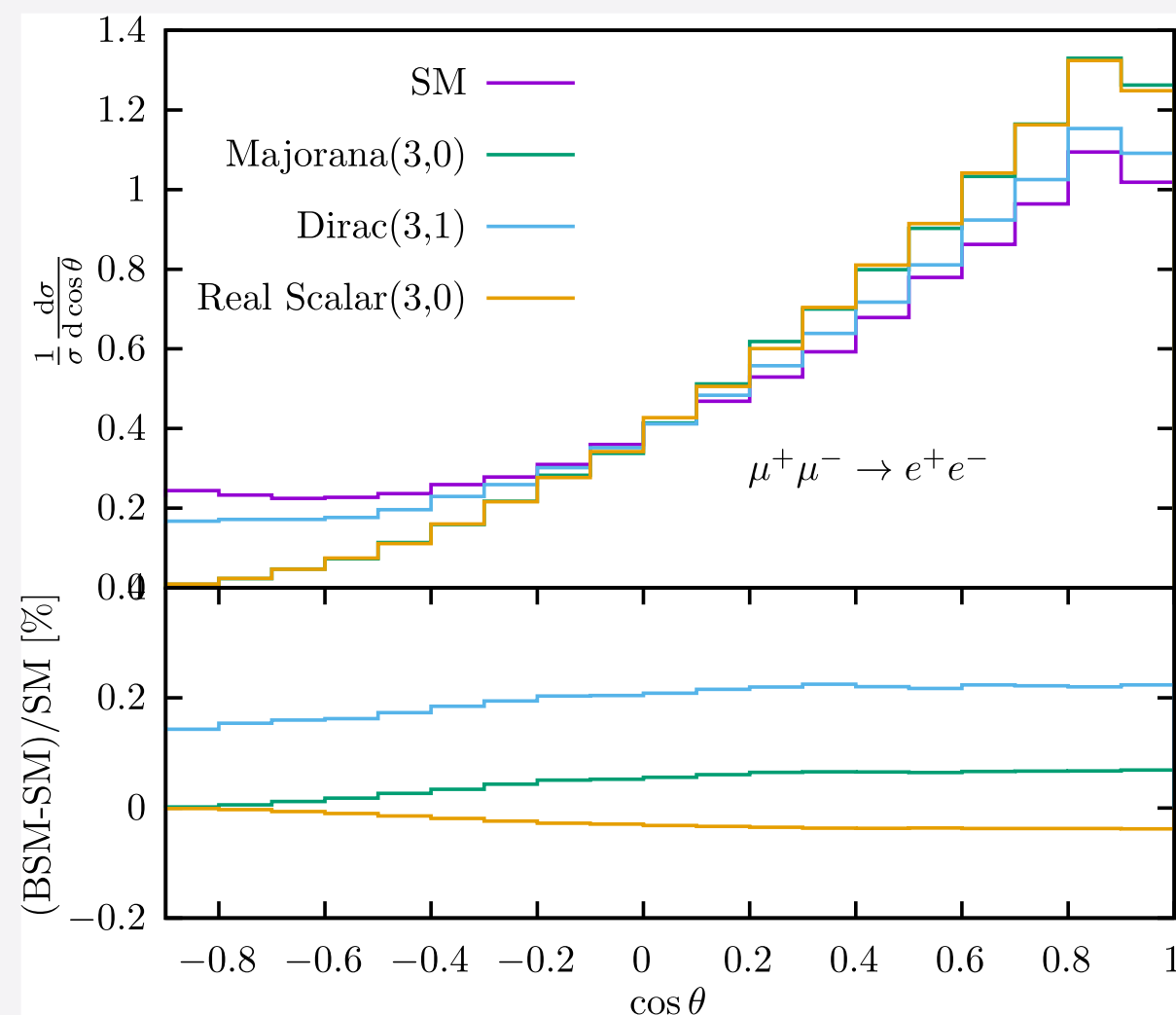
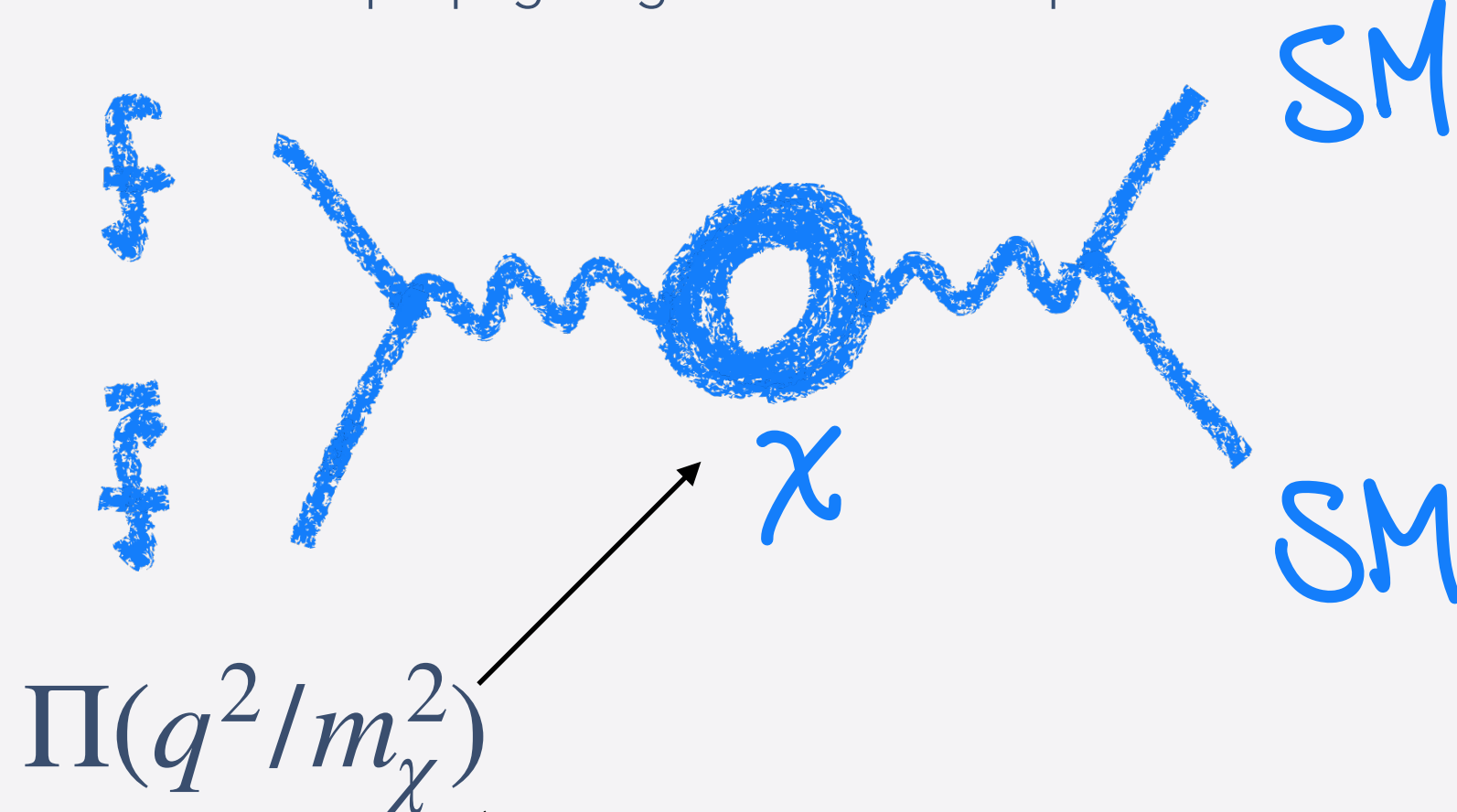
# VIRTUAL\* PRODUCTION

## *s*-channel and *t*-channel



2040s  
up to 10+ TeV

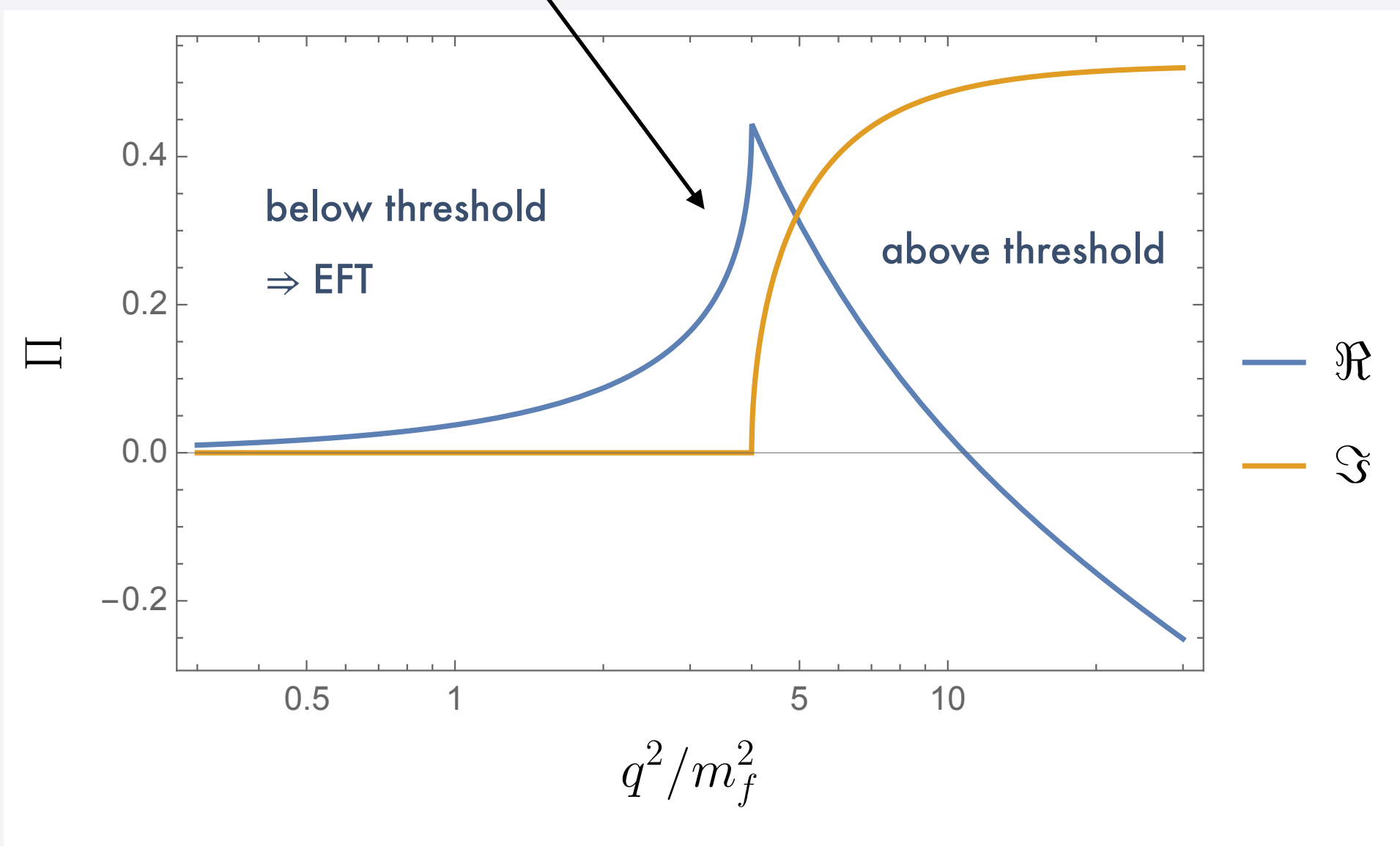
Virtual or propagating DM affects SM production rates



$$SM \subset ff$$

$$\ell^+ \ell^- \rightarrow e^+ e^-, b\bar{b}, \mu^+ \mu^-, c\bar{c}$$

- differential distributions  $\frac{d\sigma}{d\cos\theta^*}$
- differential distributions  $\frac{d\sigma}{d|\cos\theta^*|}$



1810.10993

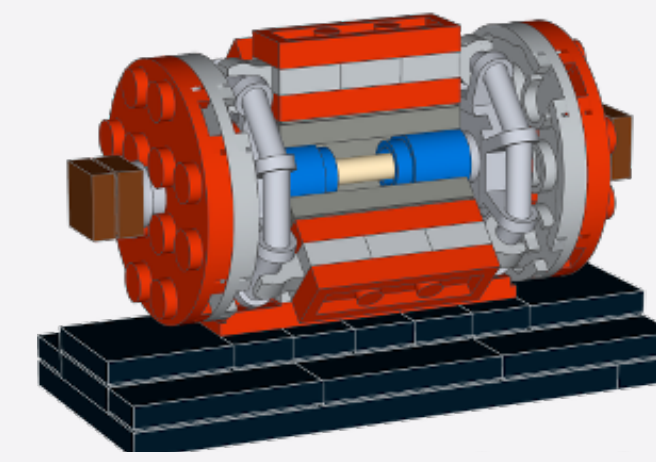
$\chi / m_\chi$ [TeV]	DM	HL-LHC	HE-LHC	FCC-100	CLIC-3	Muon-14
$(1, 2, 1/2)_{DF}$	1.1	—	—	—	0.4	0.6
$(1, 3, \epsilon)_{CS}$	1.6	—	—	—	0.2	0.2
$(1, 3, \epsilon)_{DF}$	2.0	—	0.6	1.5	0.8 & [1.0, 2.0]	2.2 & [6.3, 7.1]
$(1, 3, 0)_{MF}$	2.8	—	—	0.4	0.6 & [1.2, 1.6]	1.0
$(1, 5, \epsilon)_{CS}$	6.6	0.2	0.4	1.0	0.5 & [0.7, 1.6]	1.6
$(1, 5, \epsilon)_{DF}$	6.6	1.5	2.8	7.1	3.9	11
$(1, 5, 0)_{MF}$	14	0.9	1.8	4.4	2.9	3.5 & [5.1, 8.7]

clear advantage with respect to *pp*



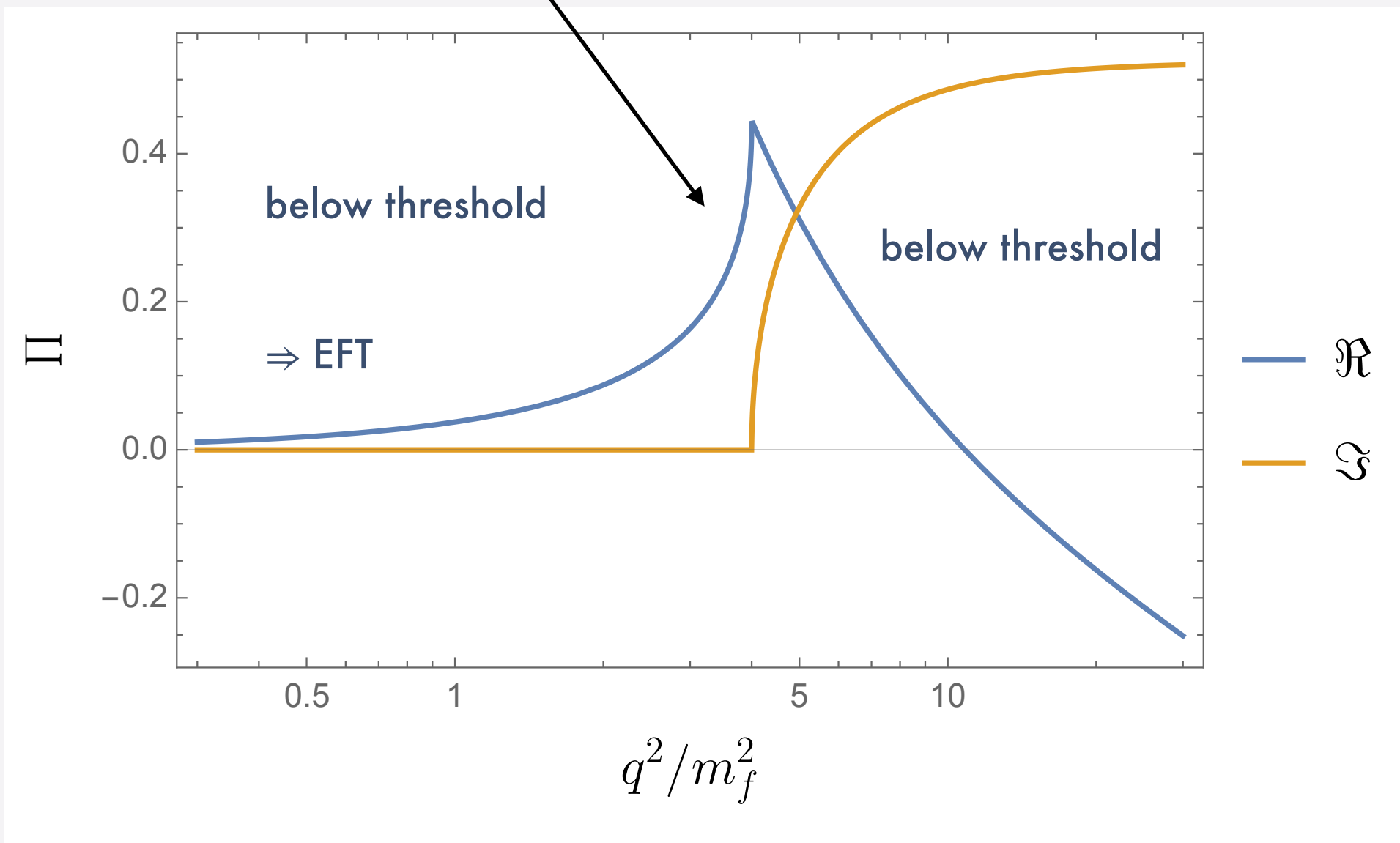
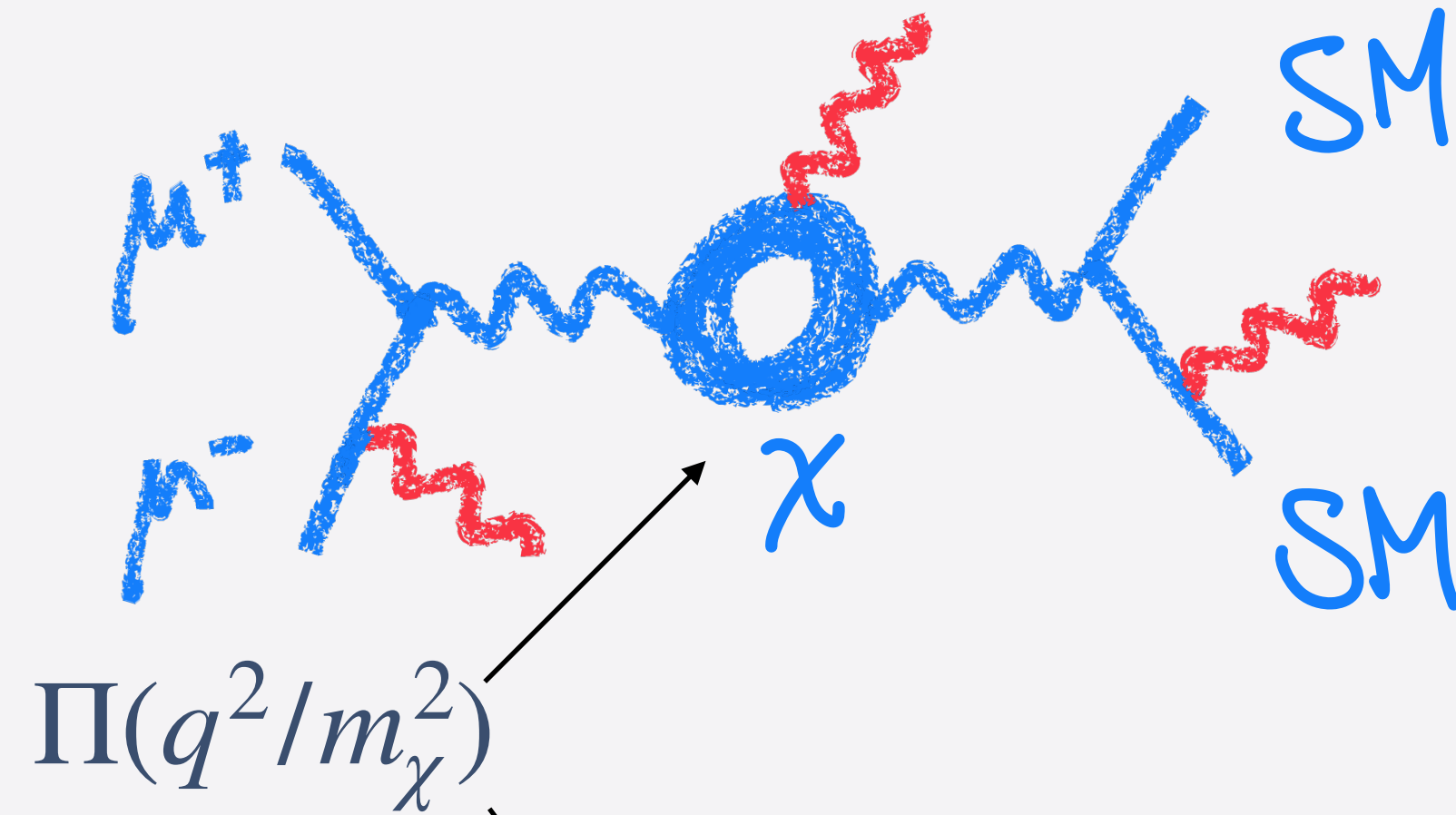
# VIRTUAL\* PRODUCTION

## *s*-channel and *t*-channel



2040s  
up to 10+ TeV

Virtual or propagating DM affects SM production rates



$$SM SM = (f\bar{f}, VV) + X$$

$$\ell^+\ell^- \rightarrow e^+e^-, b\bar{b}, \mu^+\mu^-, c\bar{c}$$

- differential distributions  $\frac{d\sigma}{d\cos\theta^*}$
- differential distributions  $\frac{d\sigma}{d|\cos\theta^*|}$

$$\ell^+\ell^- \rightarrow jj, tt, Zh, W^+W^-, Wff'$$

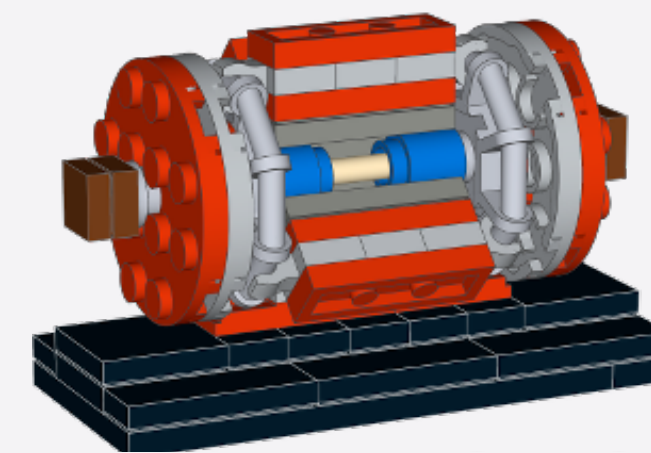
- inclusive fiducial rates

precision SM studies  $\Rightarrow$  systematics are the key

- luminosity measurements for inclusive fiducial measurements  
 $\mu\text{had}\mu\text{had}$  scattering  $\Rightarrow \delta\mathcal{L}/\mathcal{L} = 0.2\%$  at 1.5 TeV (ref)
- other systematics affecting SM final states

# VIRTUAL\* PRODUCTION

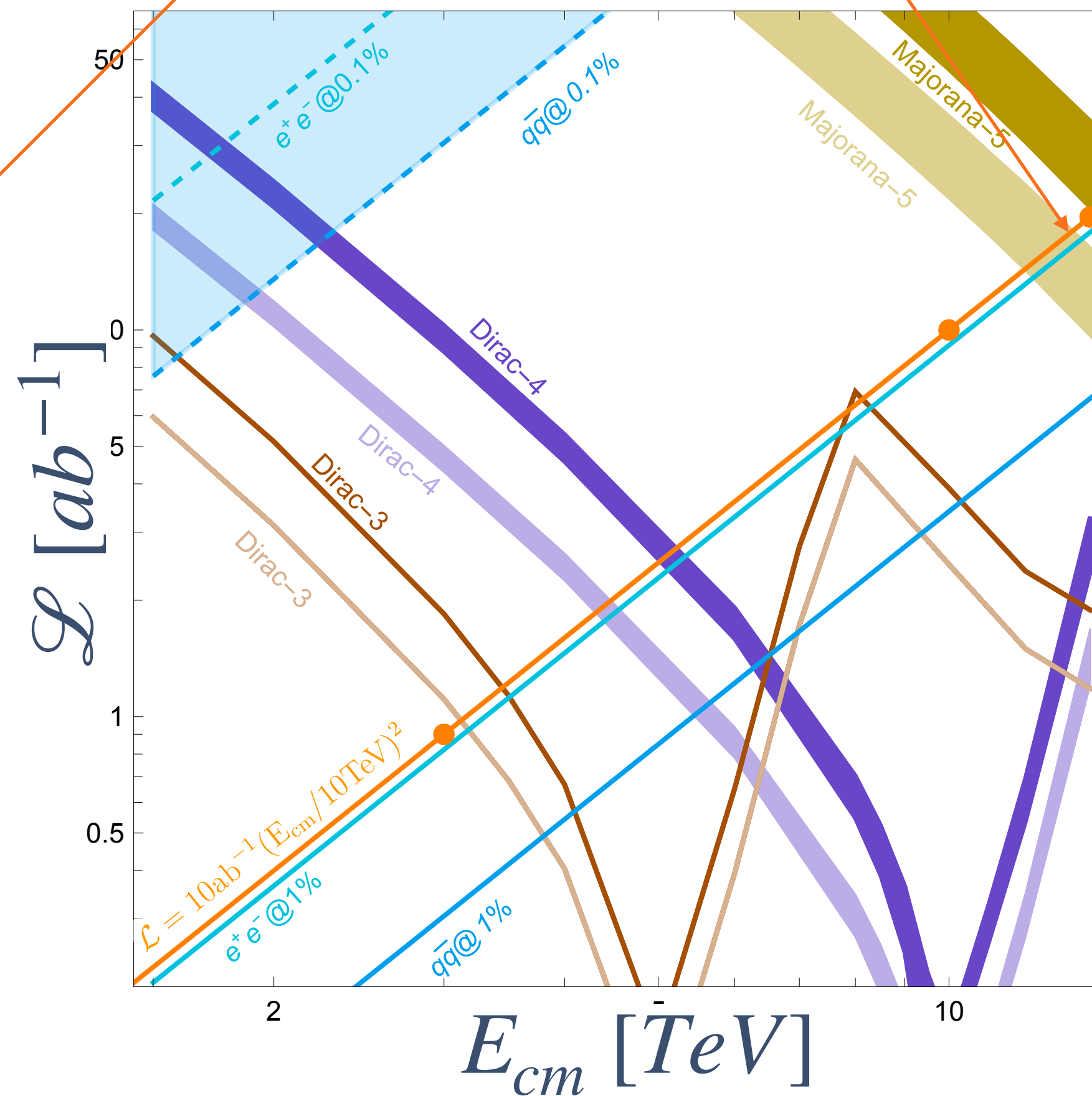
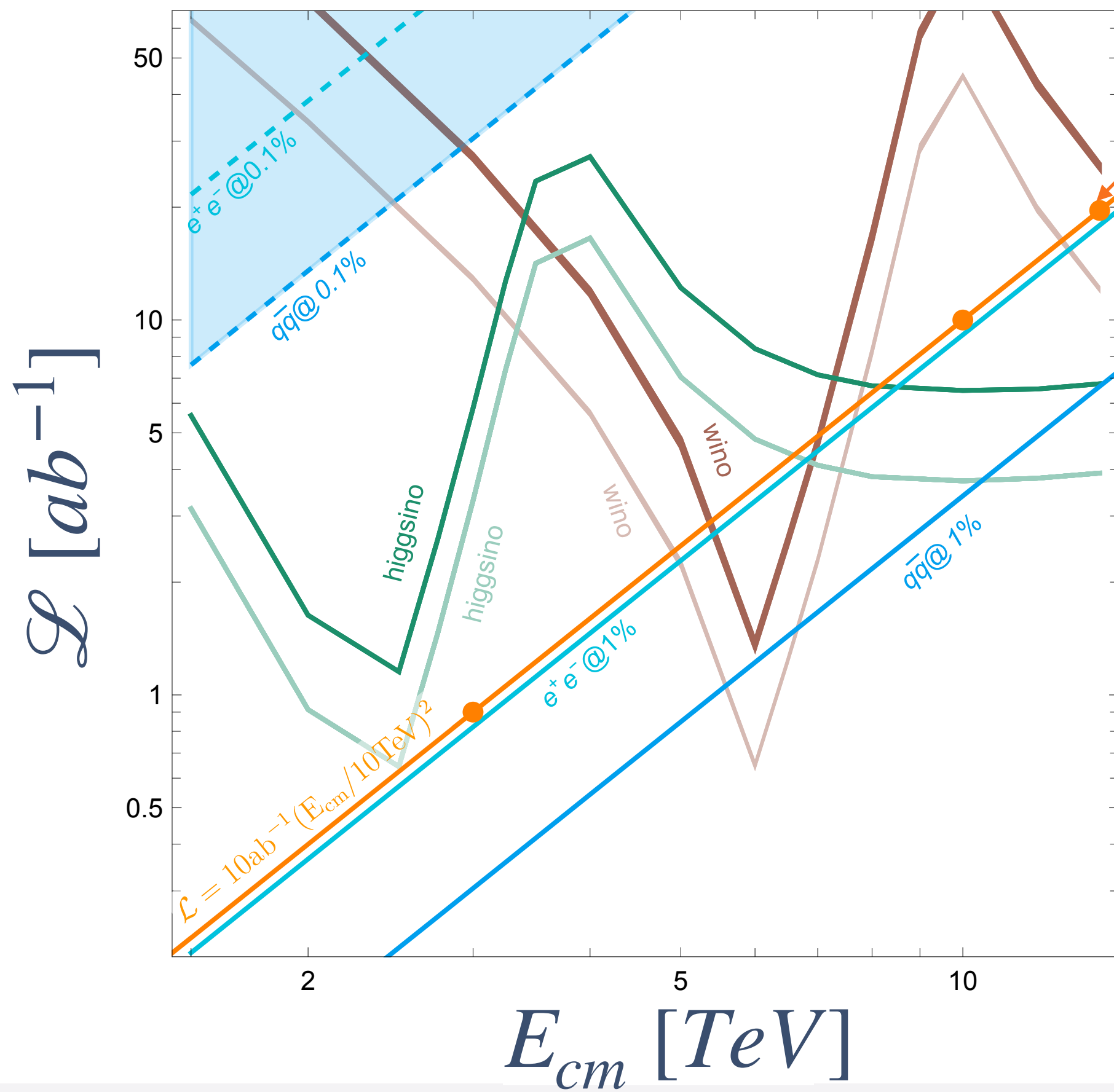
$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



# 2040s

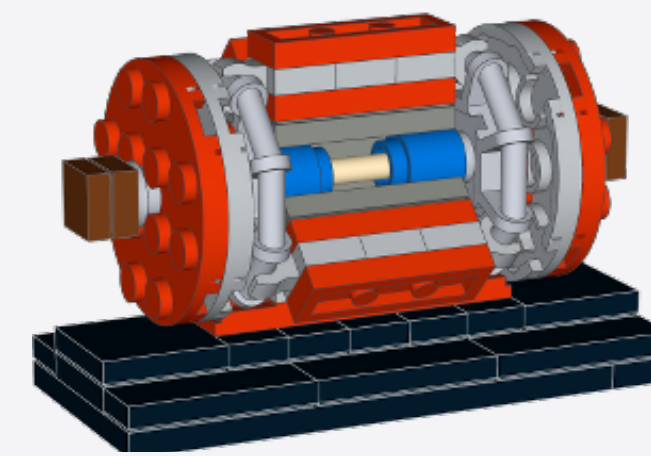
up to 10+ TeV

$$\mathcal{L} = 10 \text{ ab}^{-1} \cdot (E_{com}/10 \text{ TeV})^2$$



# VIRTUAL\* PRODUCTION

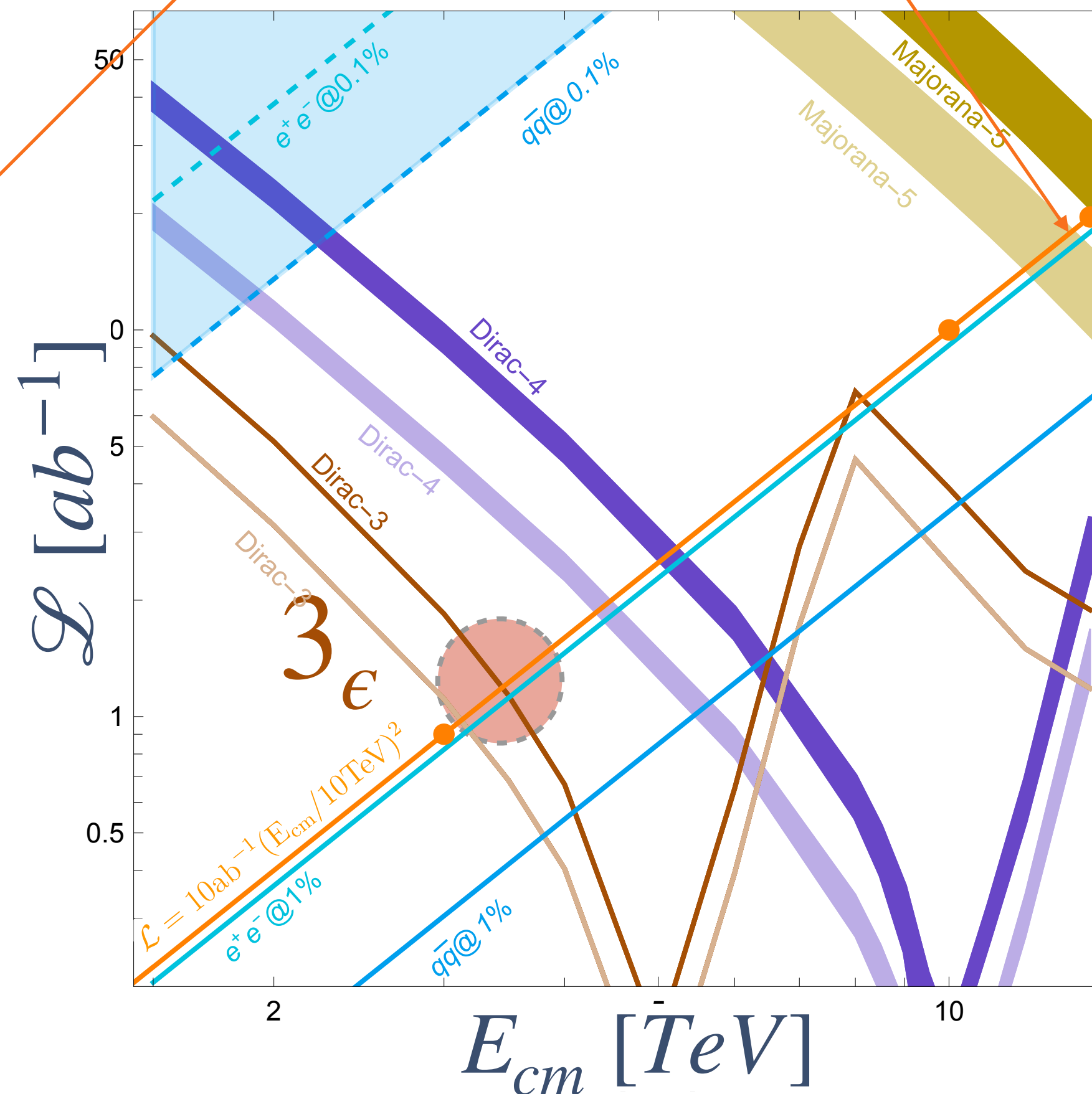
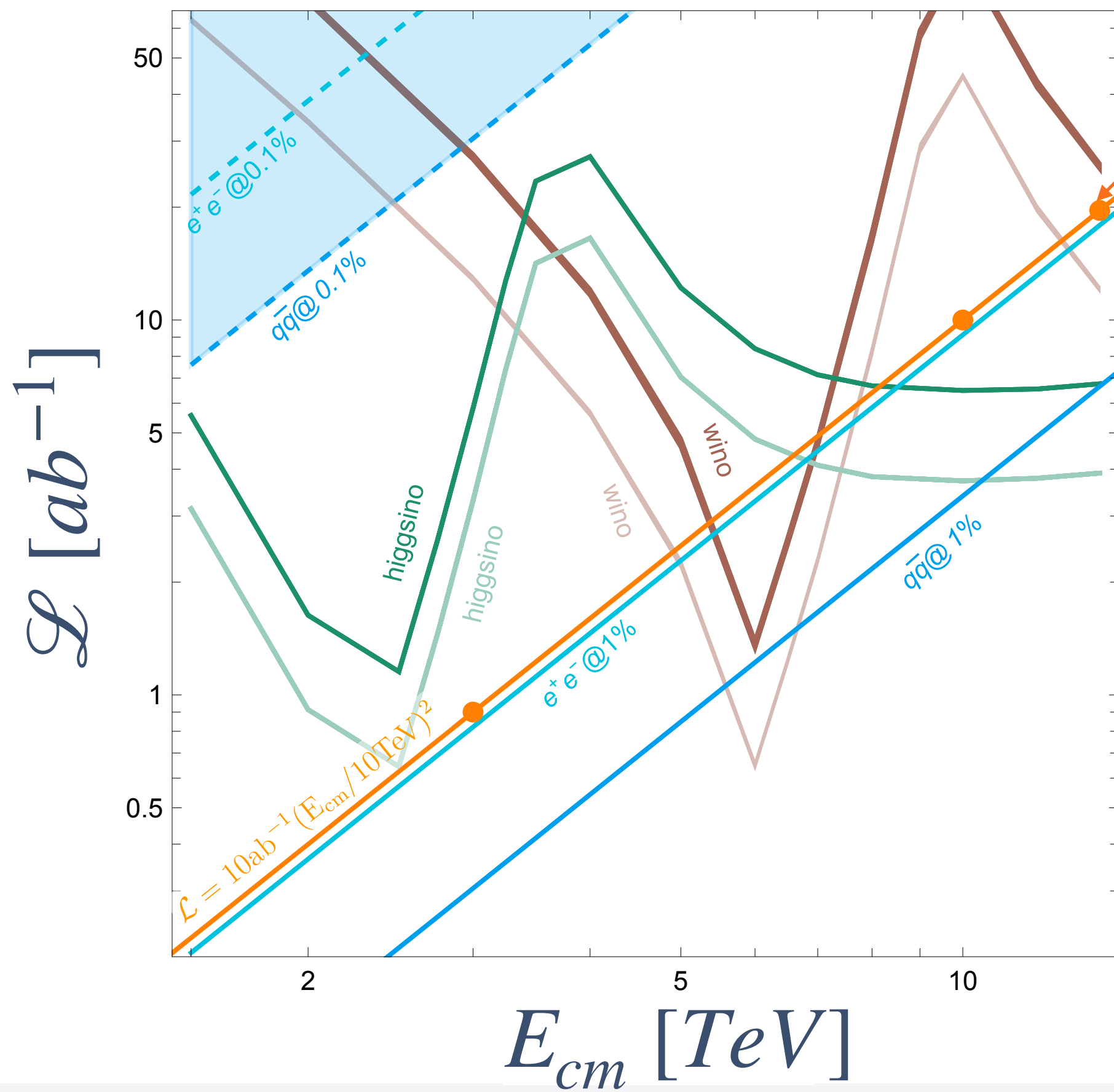
$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



# 2040s

up to 10+ TeV

$$\mathcal{L} = 10 \text{ ab}^{-1} \cdot (E_{com}/10 \text{ TeV})^2$$



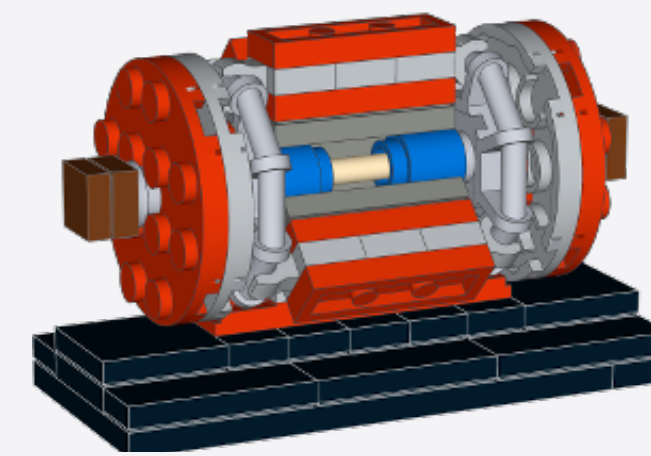
$(3, \epsilon)_{Dirac}$

$\ell^+ \ell^- 3 \text{ TeV } 1 \text{ ab}^{-1}$



# VIRTUAL\* PRODUCTION

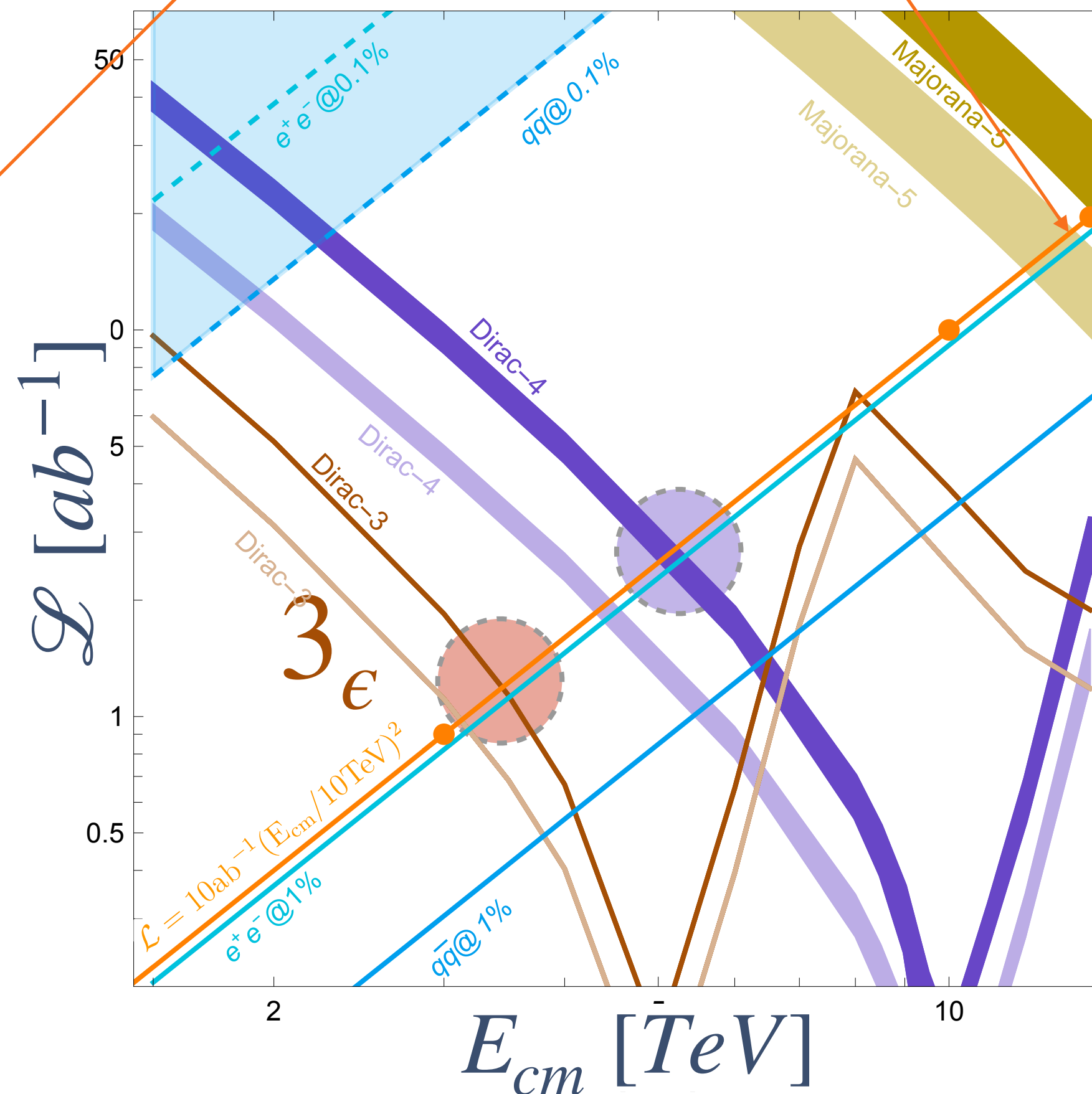
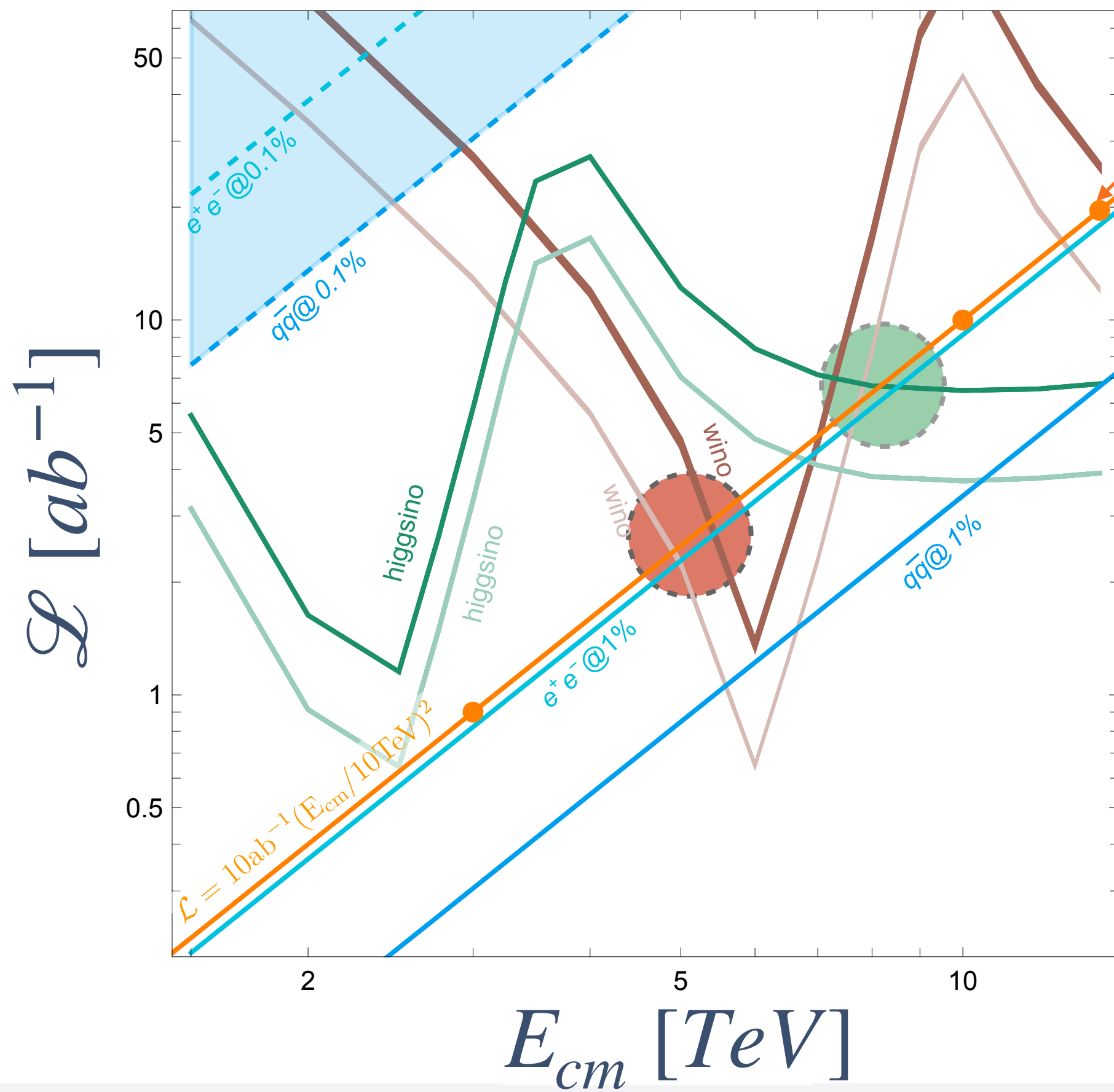
$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



# 2040s

up to 10+ TeV

$$\mathcal{L} = 10 \text{ ab}^{-1} \cdot (E_{com}/10 \text{ TeV})^2$$



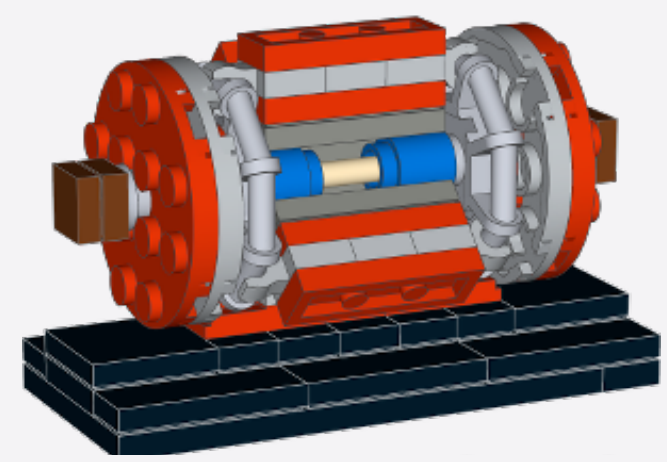
- $\left(4, \frac{1}{2}\right)_{Dirac}$
- $(3, 0)_{Majorana}$
- $(3, \epsilon)_{Dirac}$
- $\left(2, \frac{1}{2}\right)_{Dirac}$

$\ell^+ \ell^-$  10 TeV  $10 \text{ ab}^{-1}$

$\ell^+ \ell^-$  3 TeV  $1 \text{ ab}^{-1}$

# VIRTUAL\* PRODUCTION

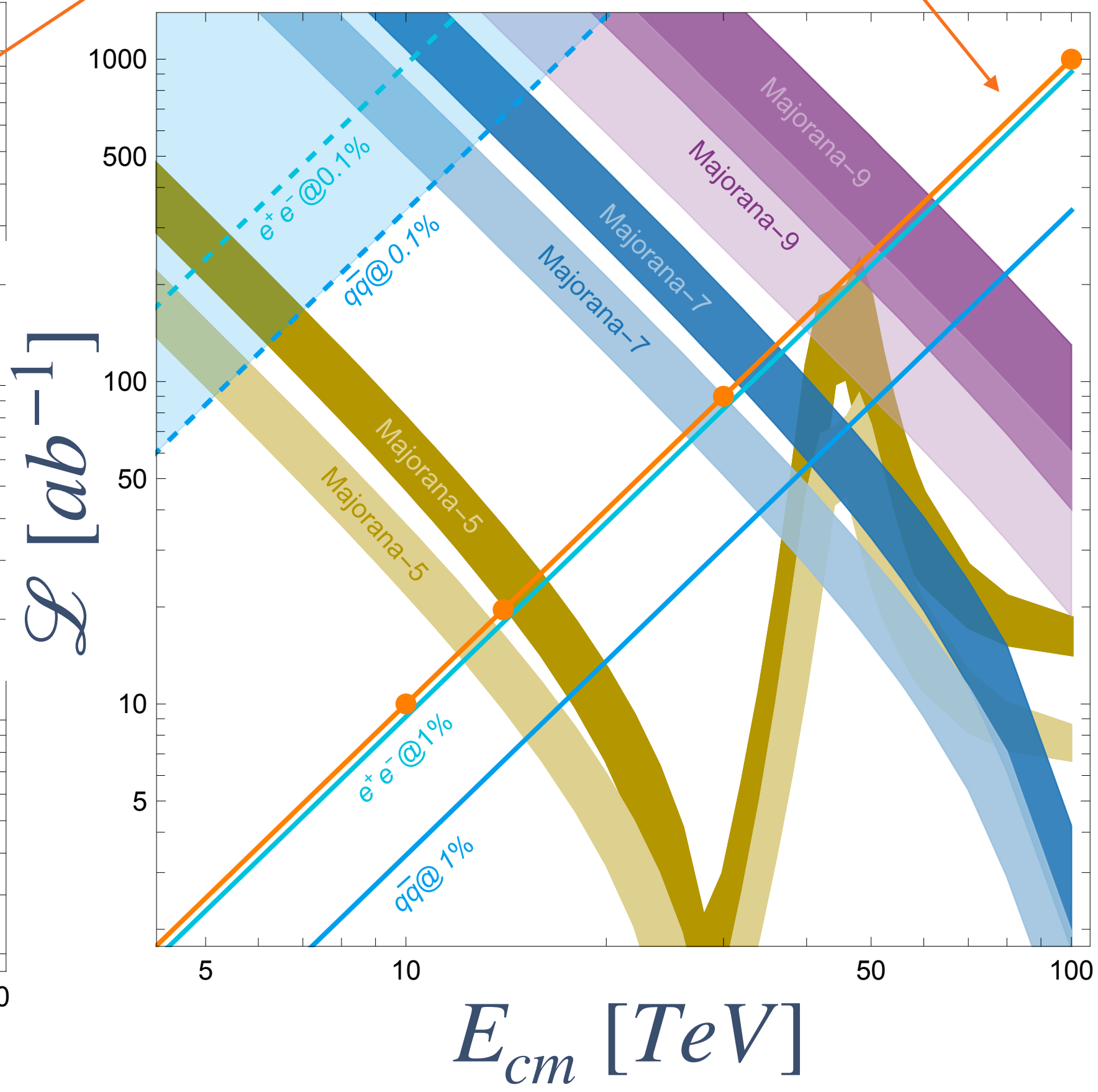
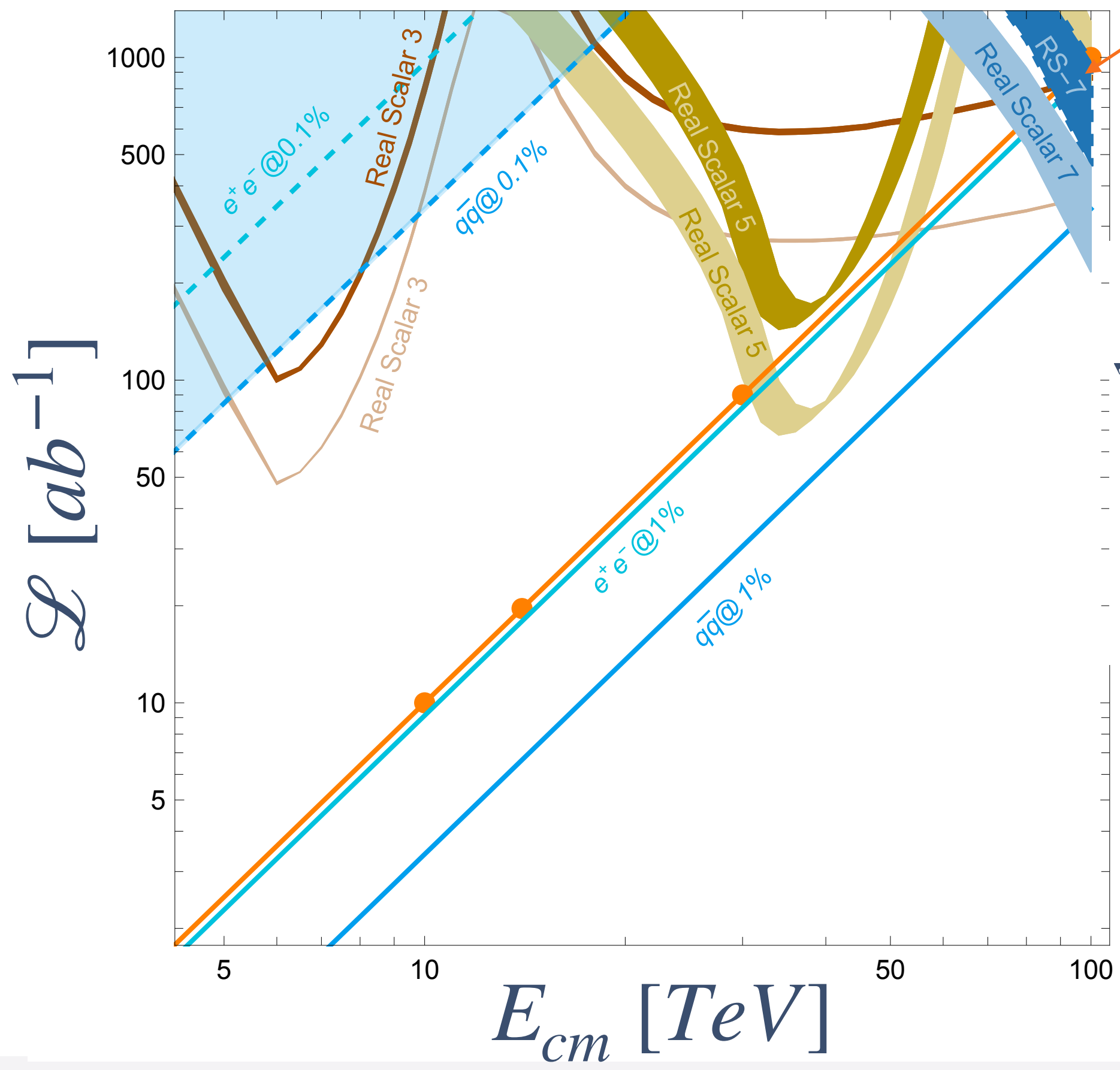
$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



# 2040s

up to 10+ TeV

$$\mathcal{L} = 10 \text{ ab}^{-1} \cdot (E_{com}/10 \text{ TeV})^2$$



- $\left(4, \frac{1}{2}\right)_{Dirac}$
- $(3, 0)_{Majorana}$
- $(3, \epsilon)_{Dirac}$
- $\left(2, \frac{1}{2}\right)_{Dirac}$

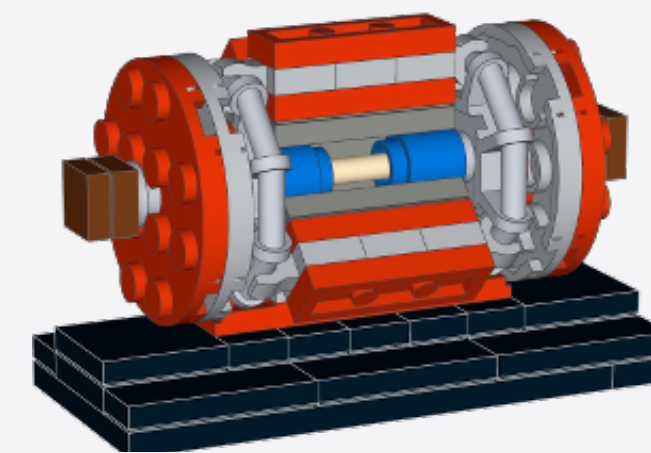
$\ell^+ \ell^-$  10 TeV  $10 \text{ ab}^{-1}$

$\ell^+ \ell^-$  3 TeV  $1 \text{ ab}^{-1}$



# VIRTUAL\* PRODUCTION

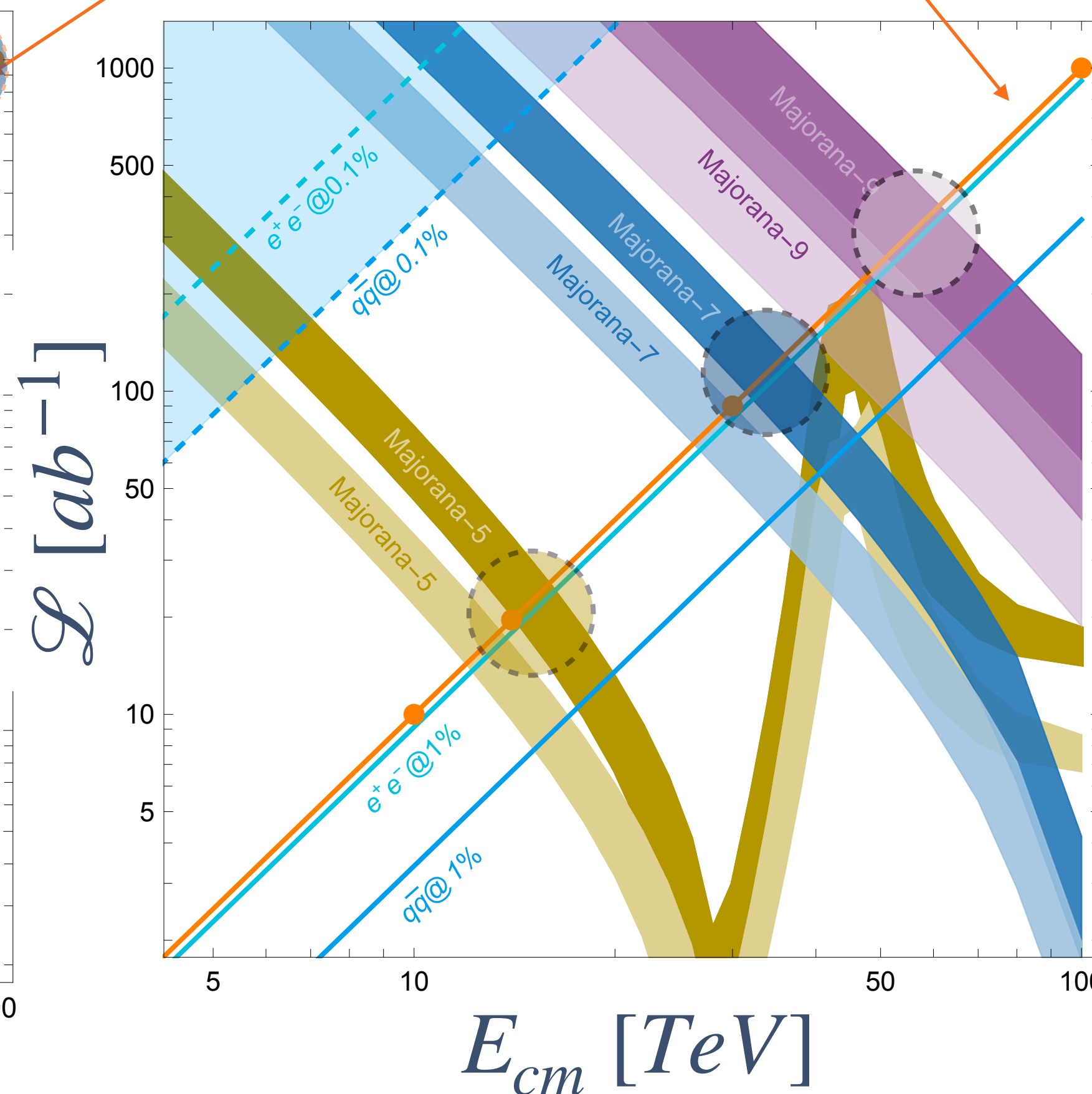
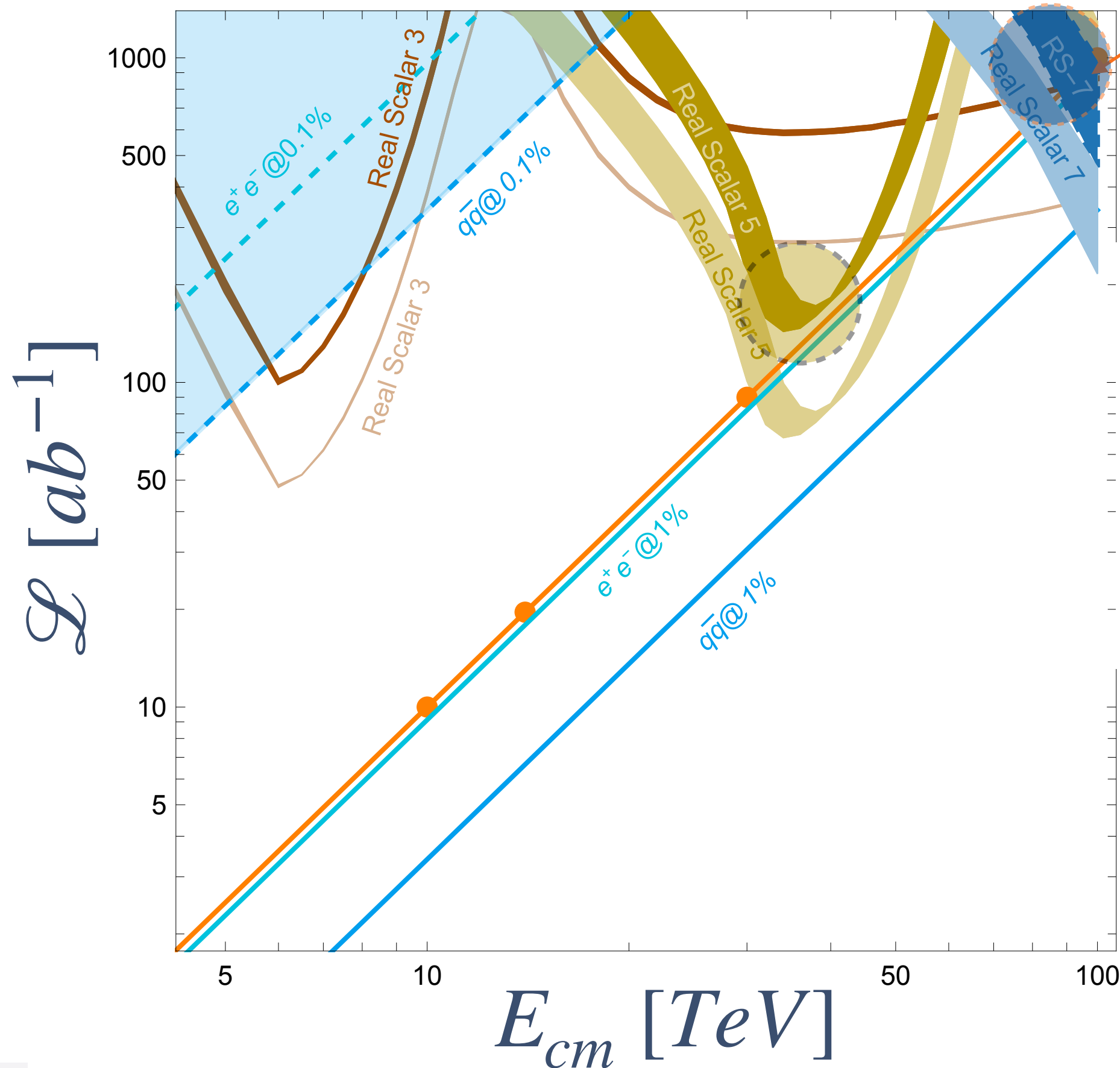
$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



# 2040s

up to 10+ TeV

$$\mathcal{L} = 10 \text{ ab}^{-1} \cdot (E_{com}/10 \text{ TeV})^2$$



- $(7,0)_{Majorana}$
- $(7, \epsilon)_{Dirac}$
- $(5,0)_{Majorana}$
- $(5, \epsilon)_{Dirac}$
- $(4, \frac{1}{2})_{Dirac}$
- $(3,0)_{Majorana}$
- $(3, \epsilon)_{Dirac}$
- $(2, \frac{1}{2})_{Dirac}$

$\ell^+ \ell^-$  10+ TeV 10+  $ab^{-1}$

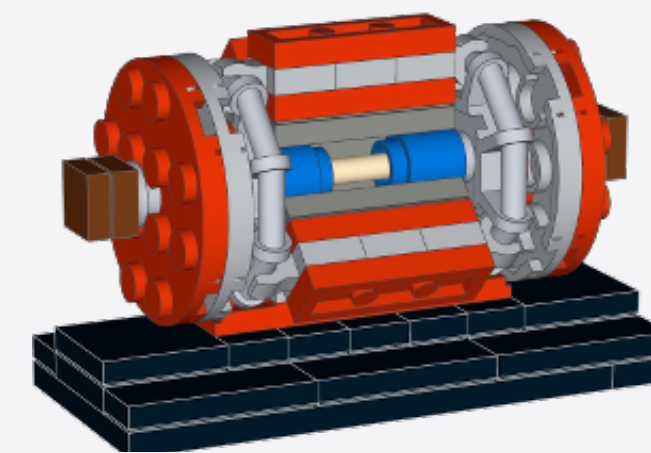
$\ell^+ \ell^-$  10 TeV 10  $ab^{-1}$

$\ell^+ \ell^-$  3 TeV 1  $ab^{-1}$



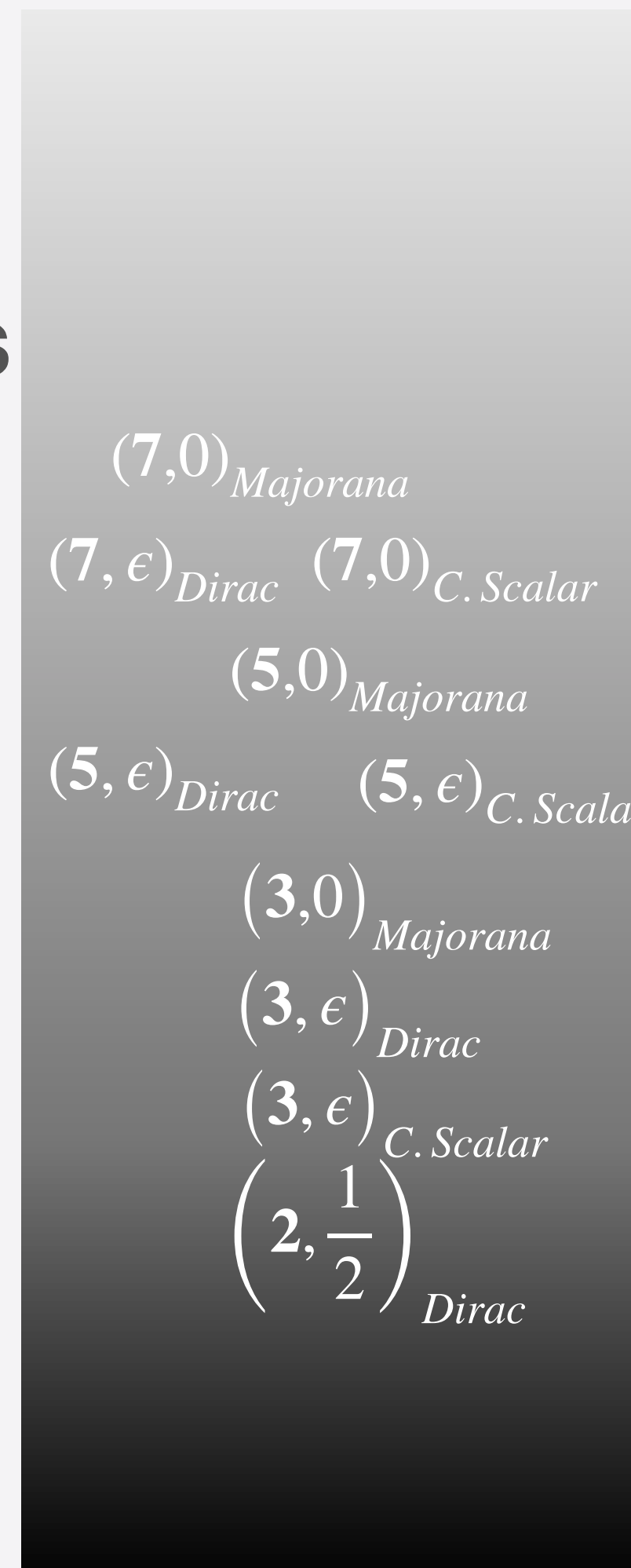
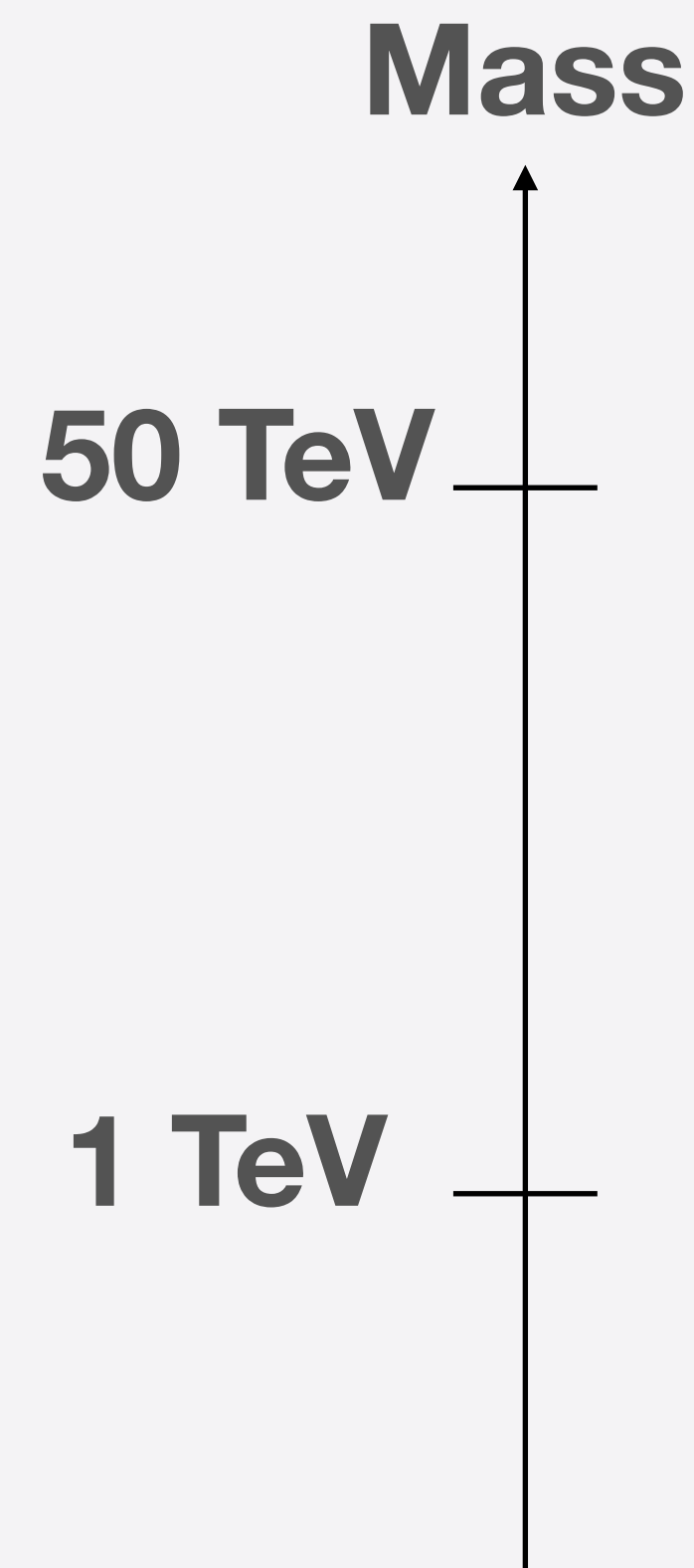
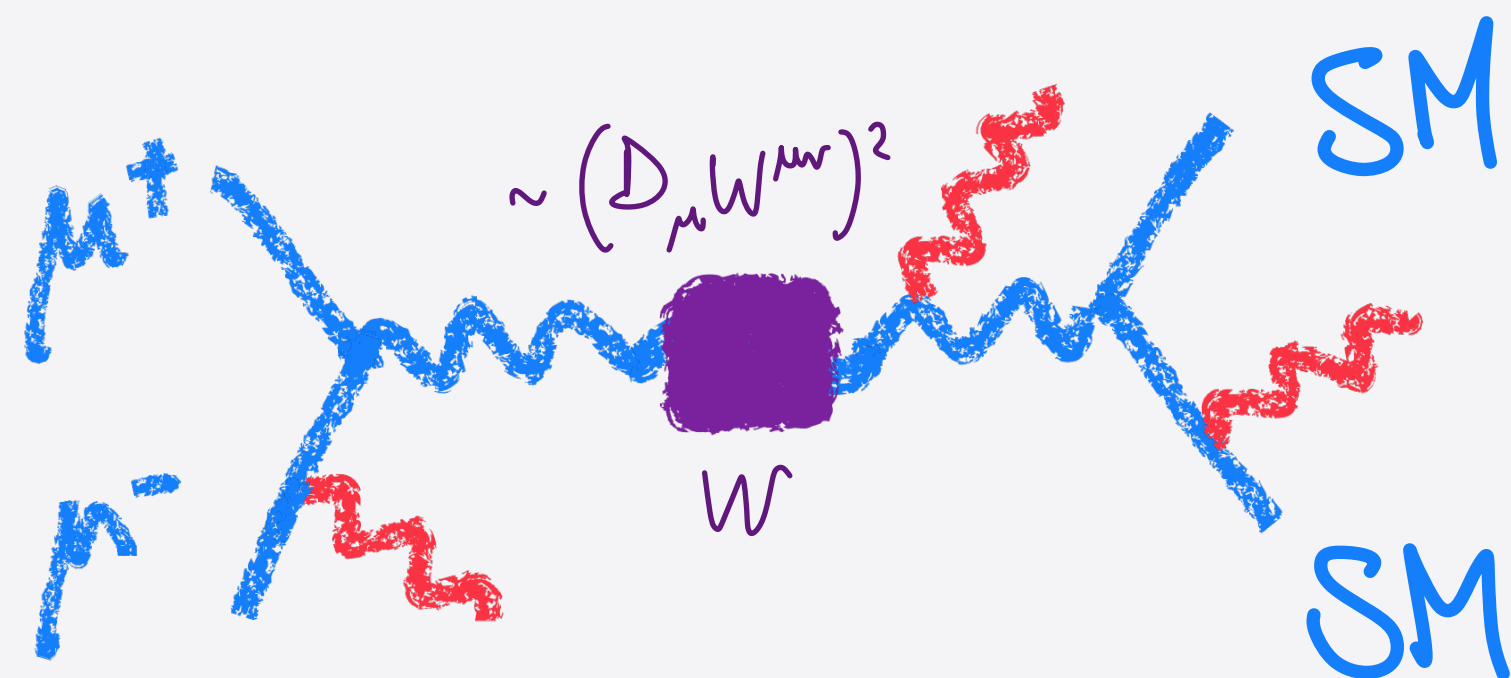
# VIRTUAL\* PRODUCTION

$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



# 2040s

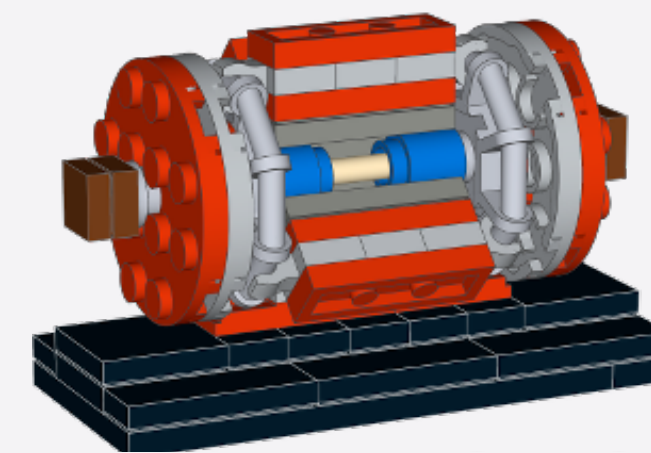
up to 10+ TeV



**“WIMP” Dark Matter**

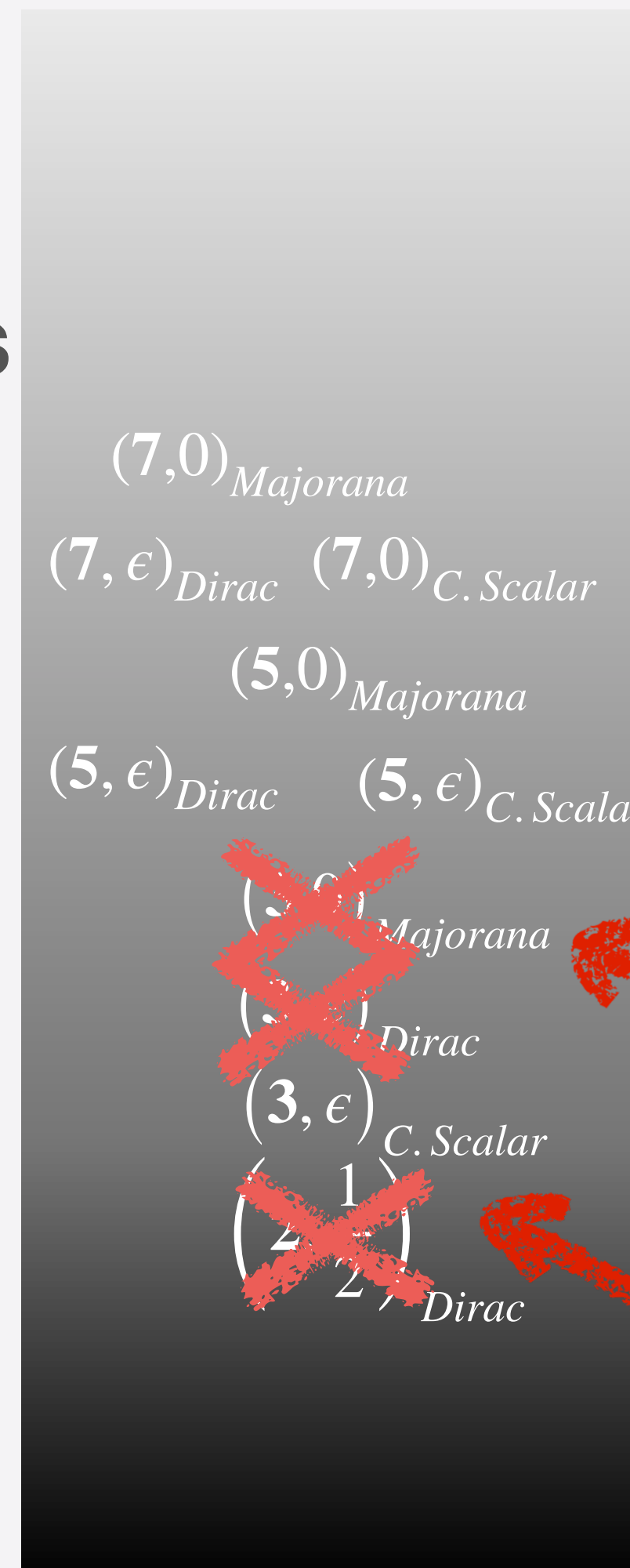
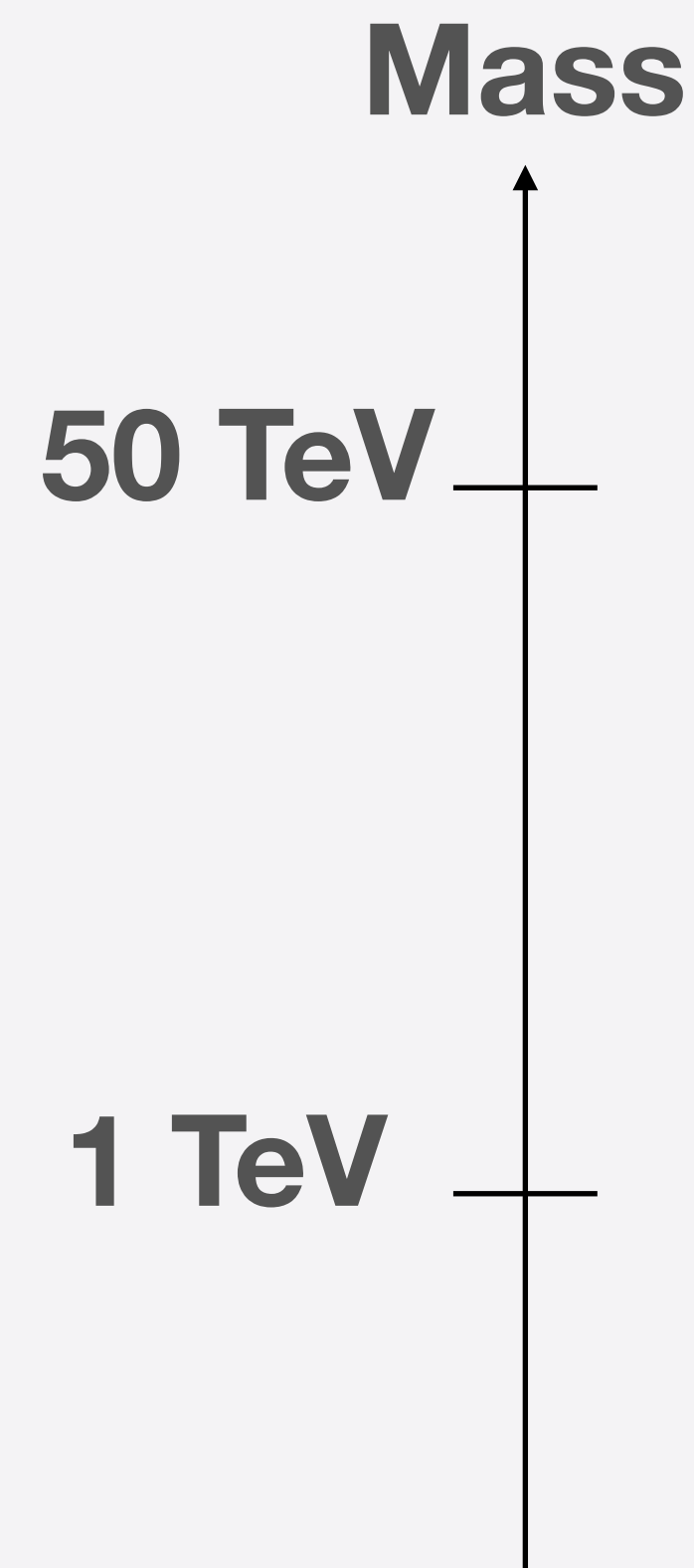
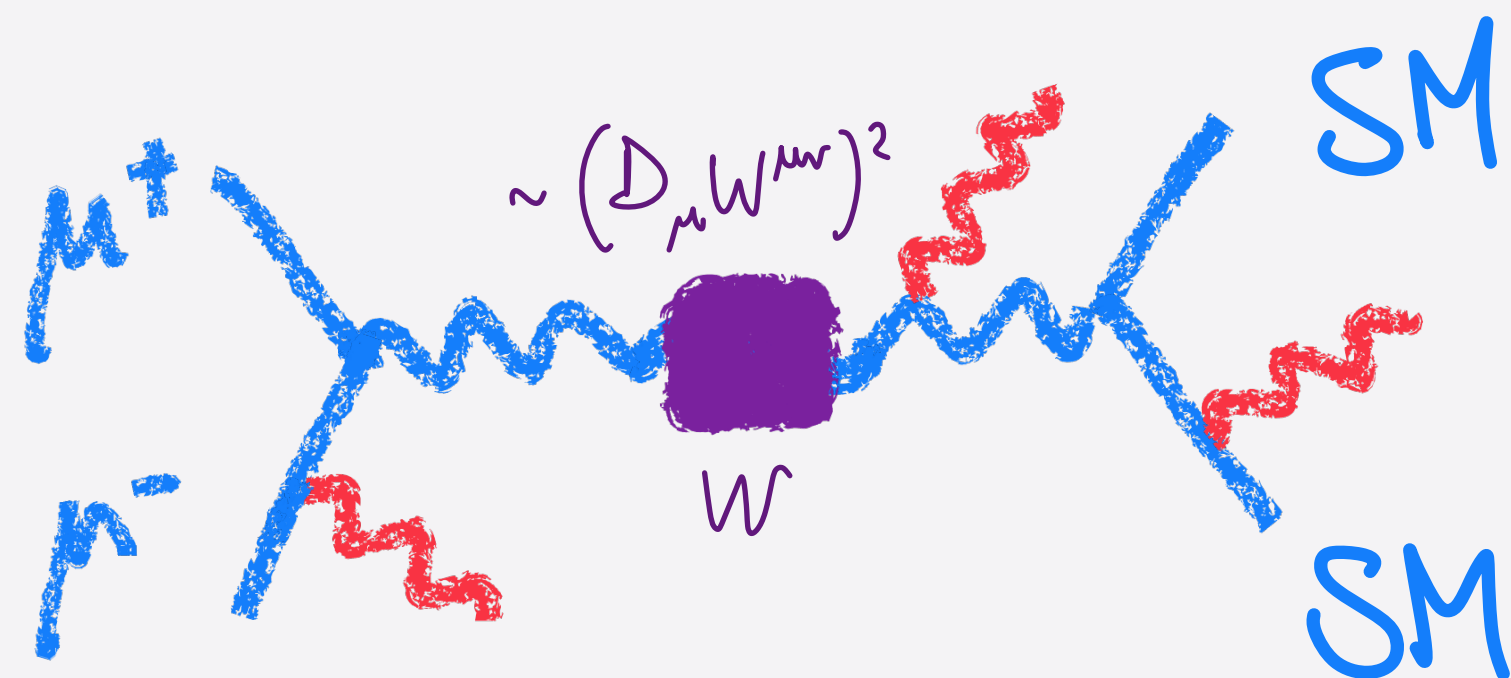
# VIRTUAL\* PRODUCTION

$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



# 2040s

up to 10+ TeV



$\ell^+ \ell^-$  10 TeV 10  $ab^{-1}$

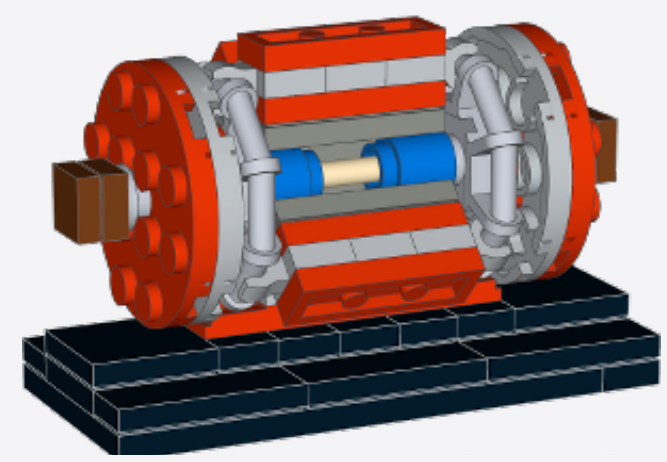
SUSY  
WINO

SUSY  
HIGGSINO

“WIMP” Dark Matter

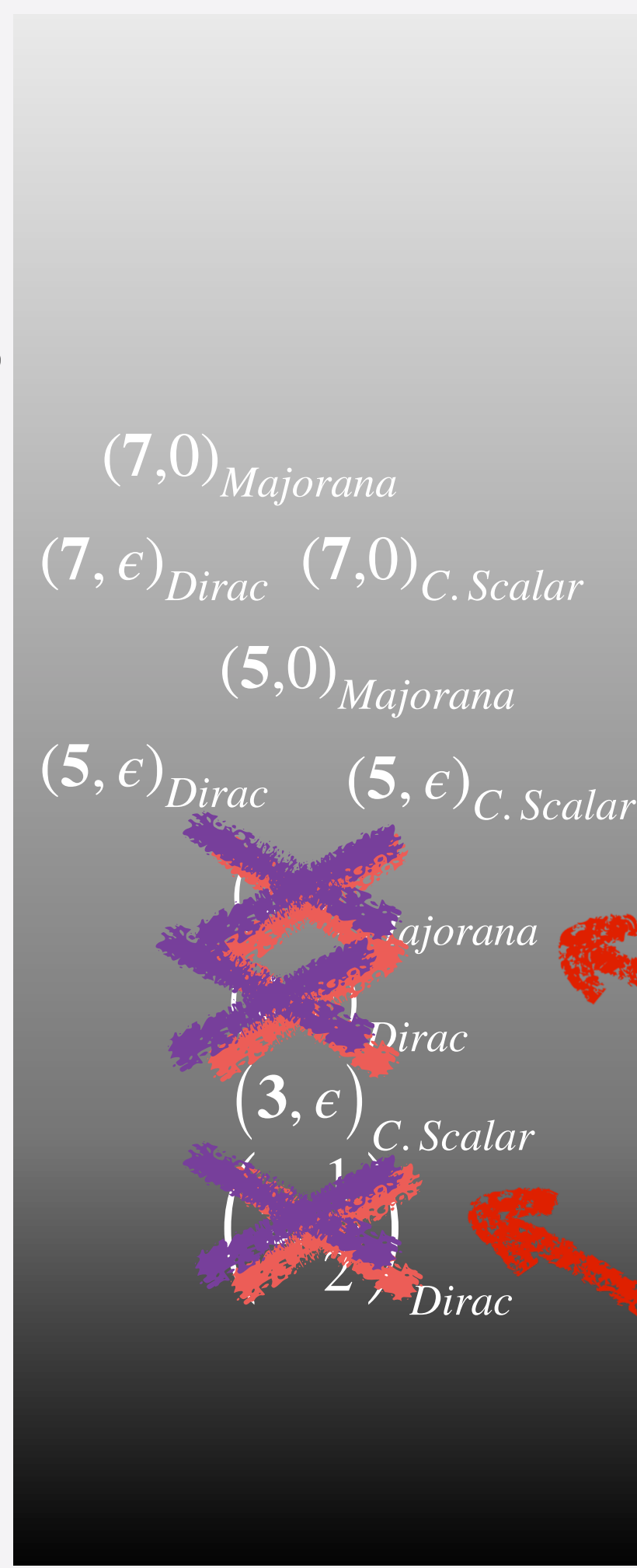
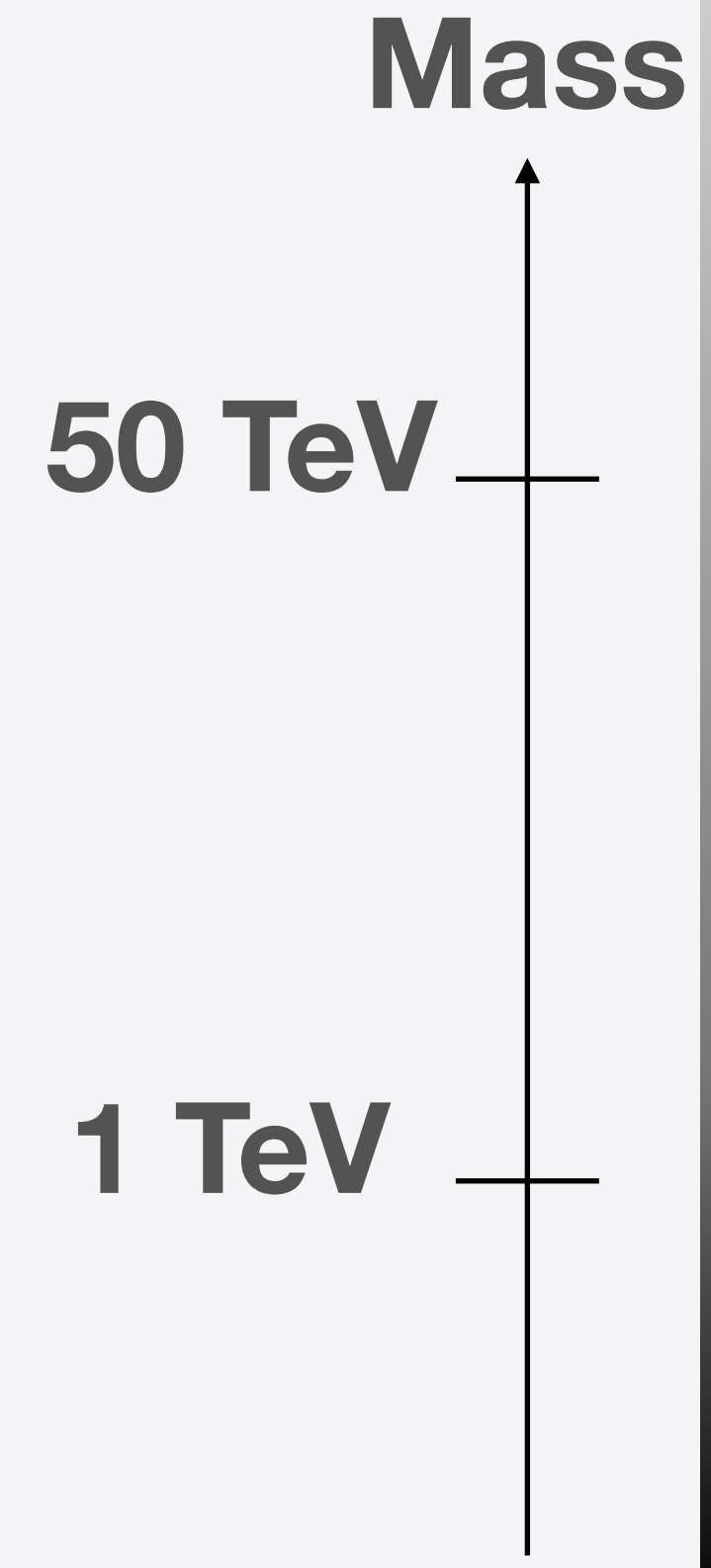
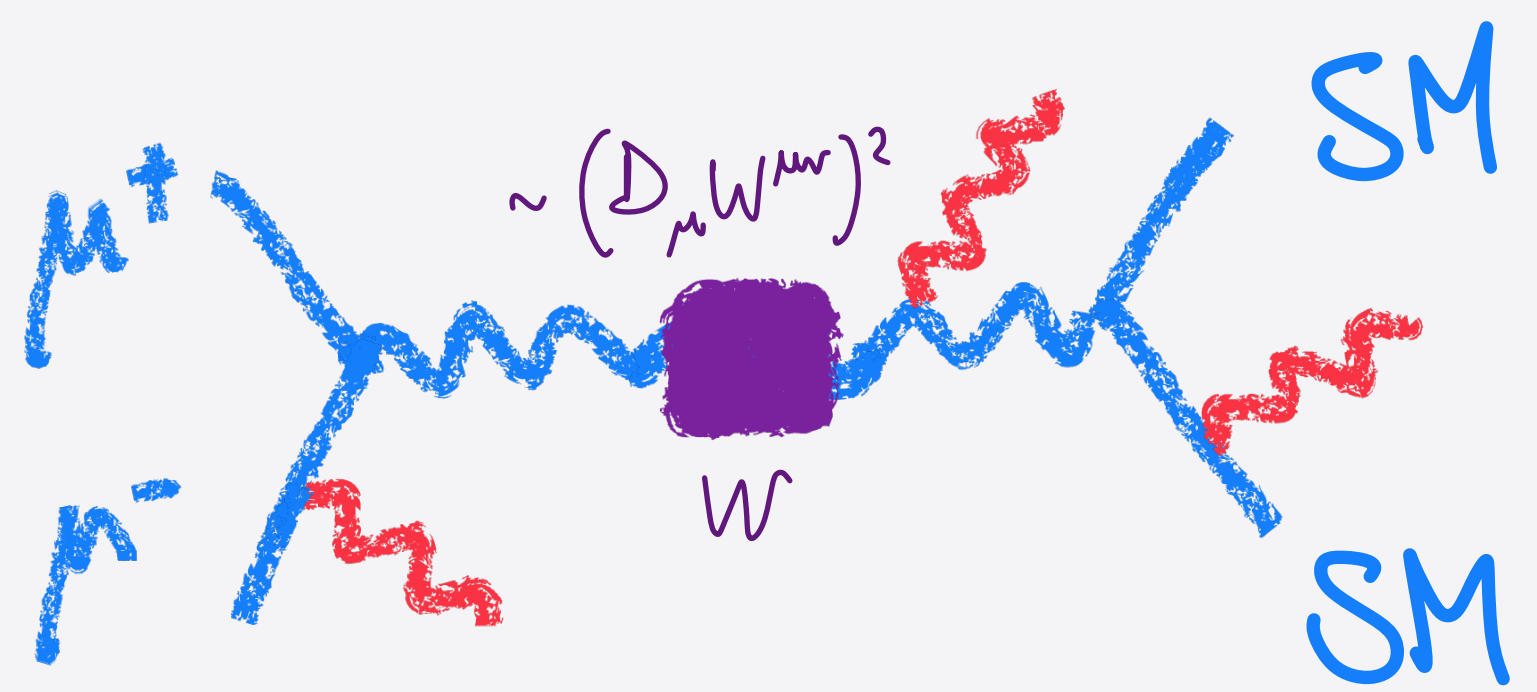
# VIRTUAL\* PRODUCTION

$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



# 2040s

up to 10+ TeV



$\ell^+ \ell^-$  10 TeV 10  $ab^{-1}$   
 $pp$  100 TeV 30  $ab^{-1}$

SUSY  
WINO

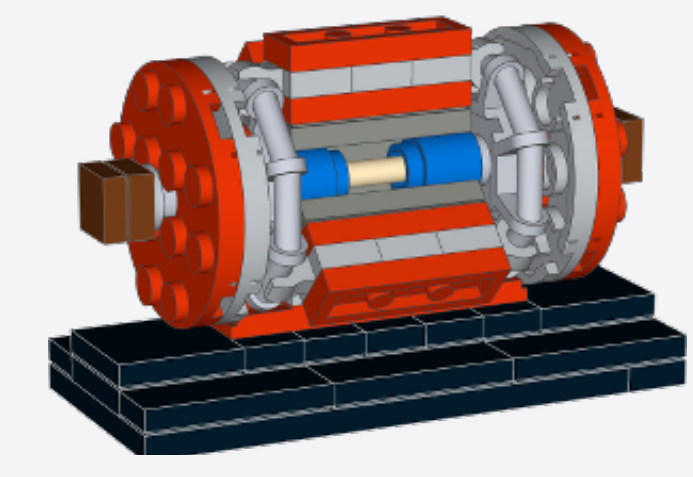
SUSY  
HIGGSINO

“WIMP” Dark Matter



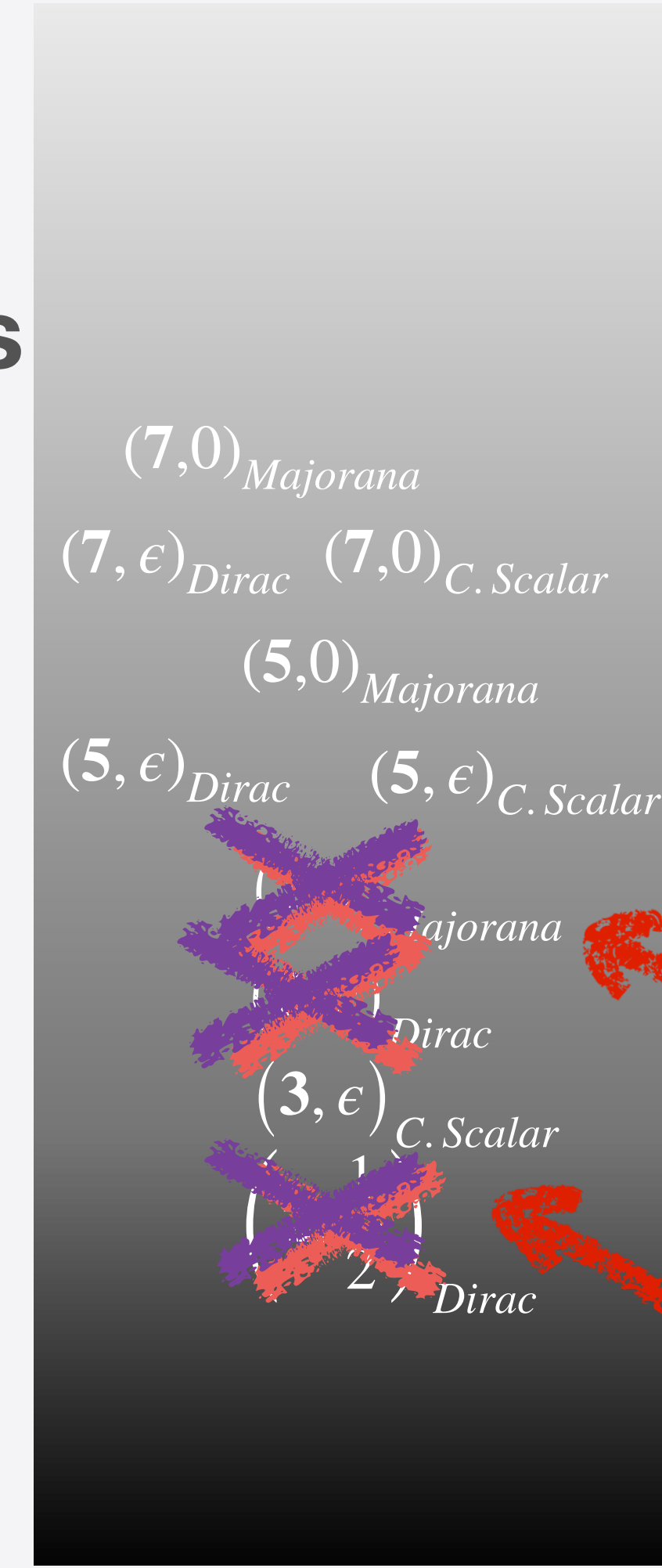
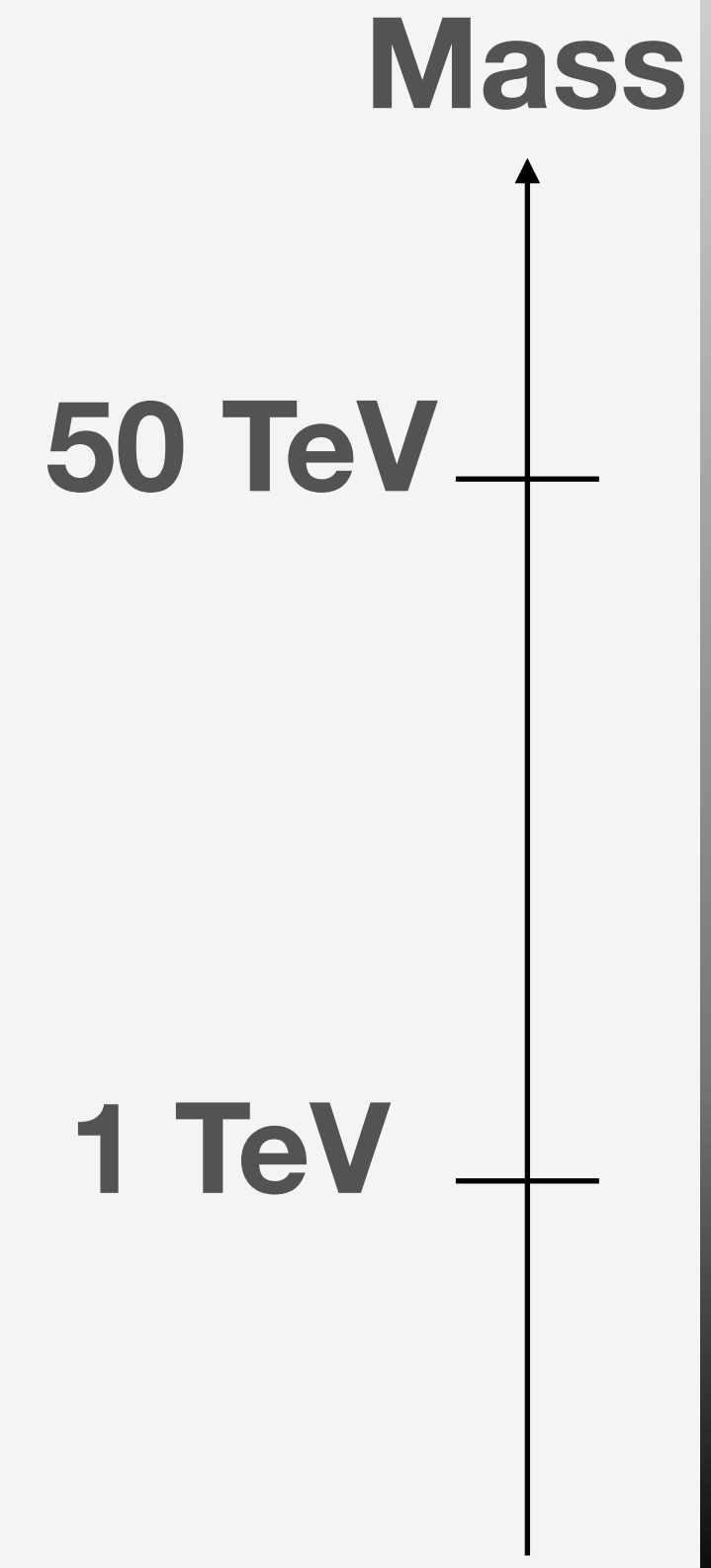
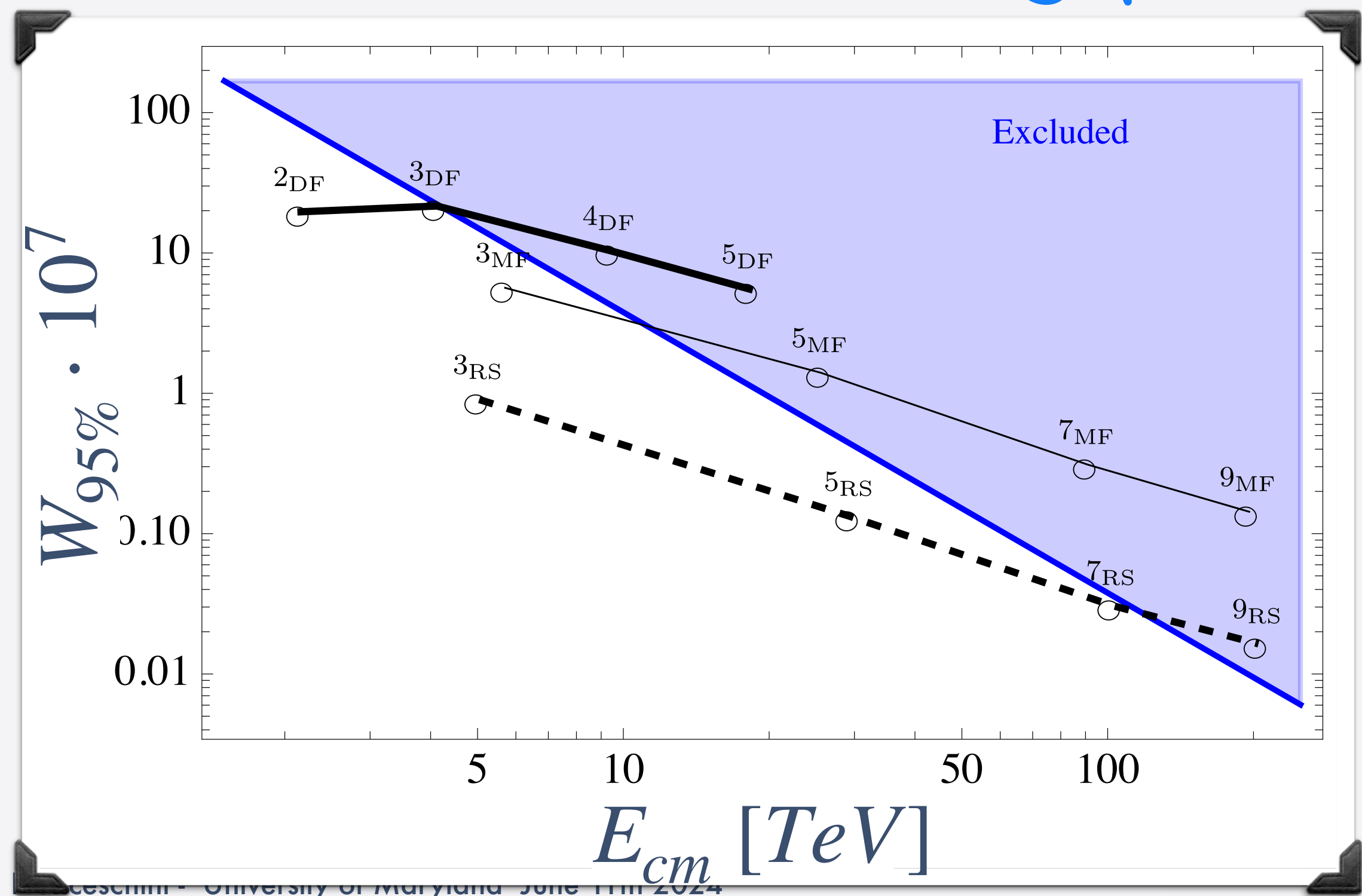
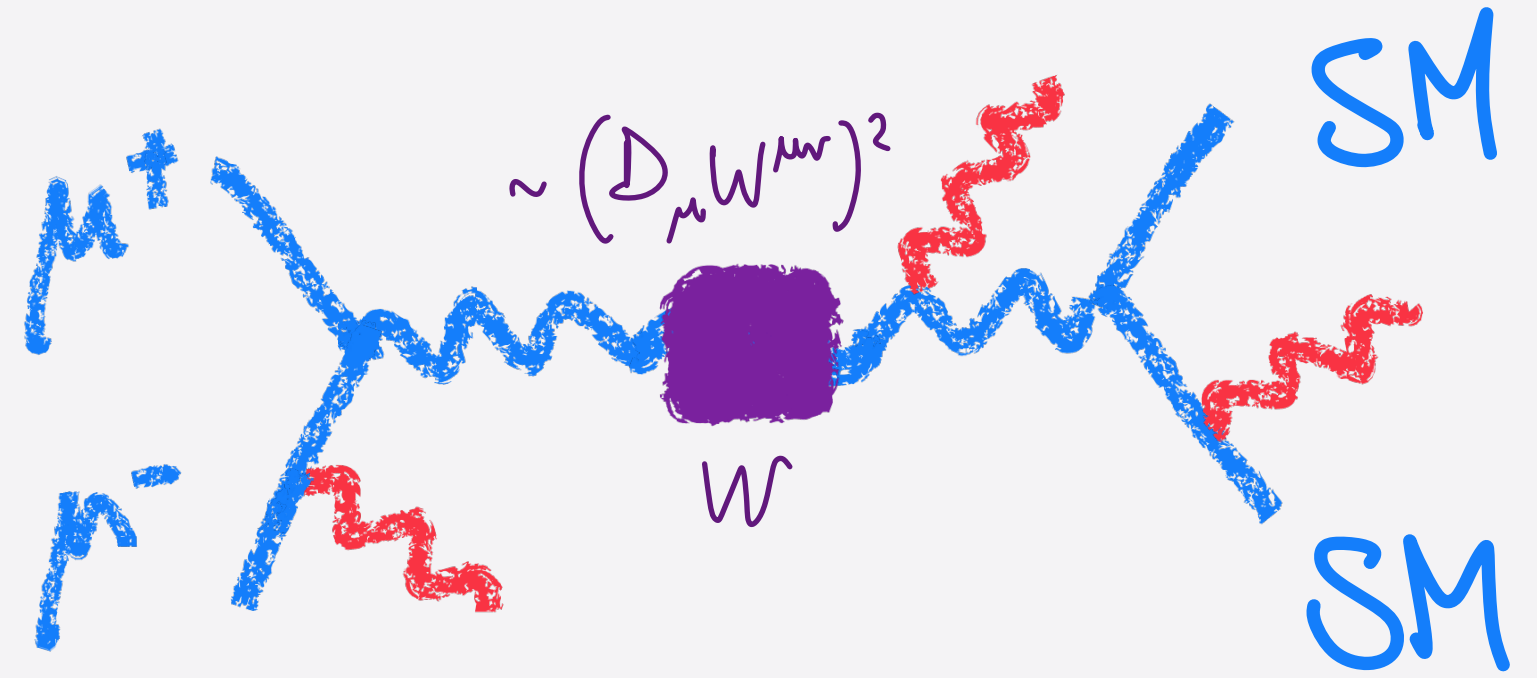
# VIRTUAL\* PRODUCTION

$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



# 2040s

up to 10+ TeV



$\ell^+ \ell^-$  10 TeV 10  $ab^{-1}$   
 $pp$  100 TeV 30  $ab^{-1}$

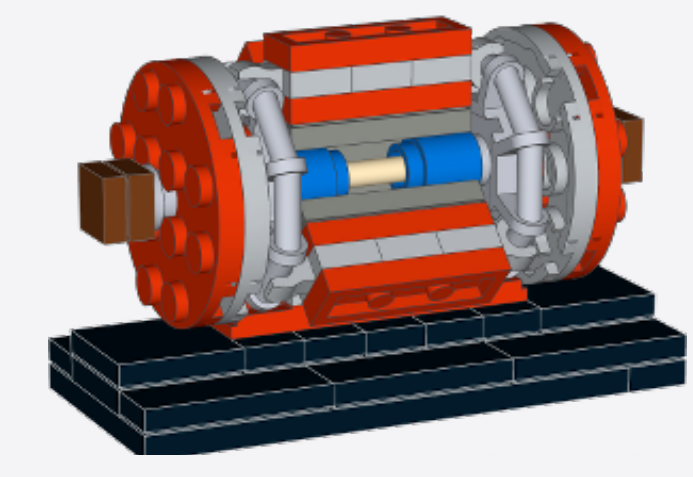
SUSY WINO

SUSY HIGGSINO

"WIMP" Dark Matter

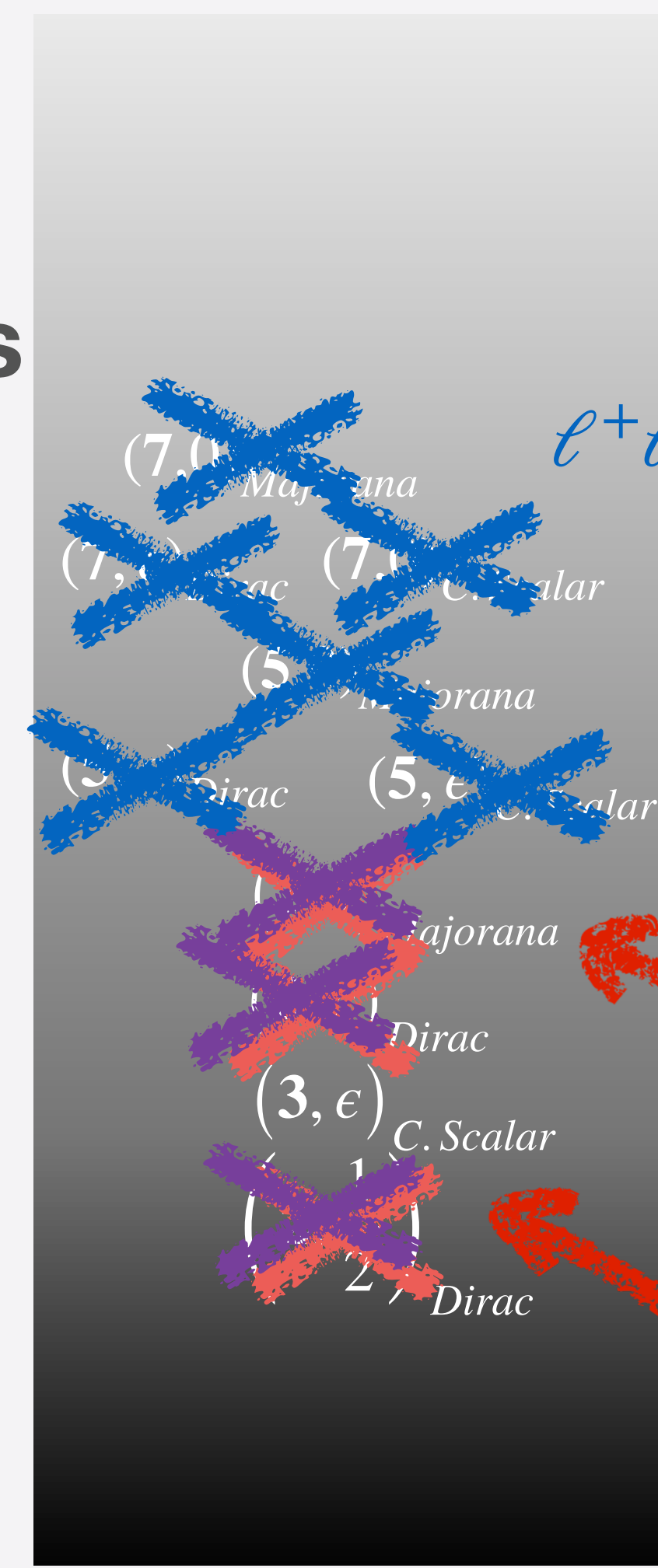
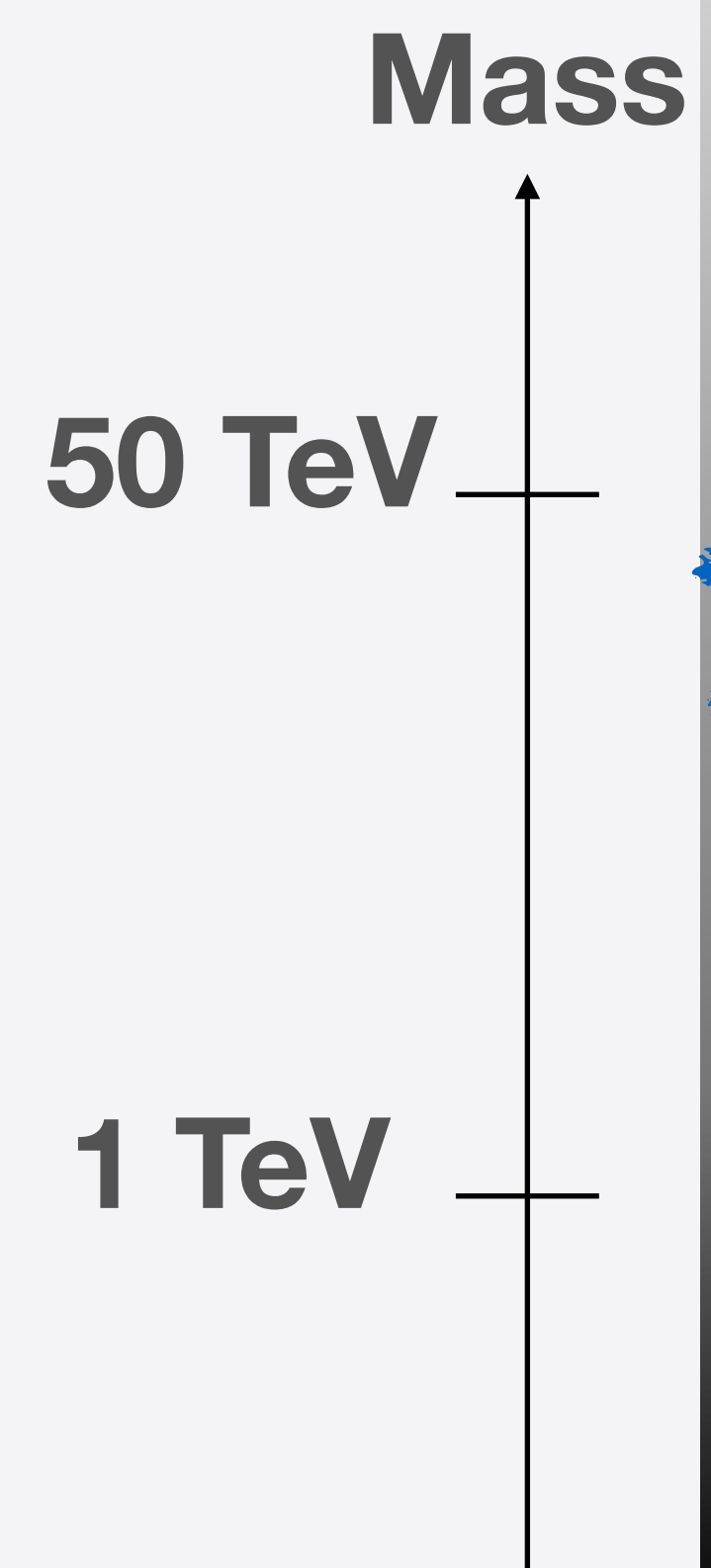
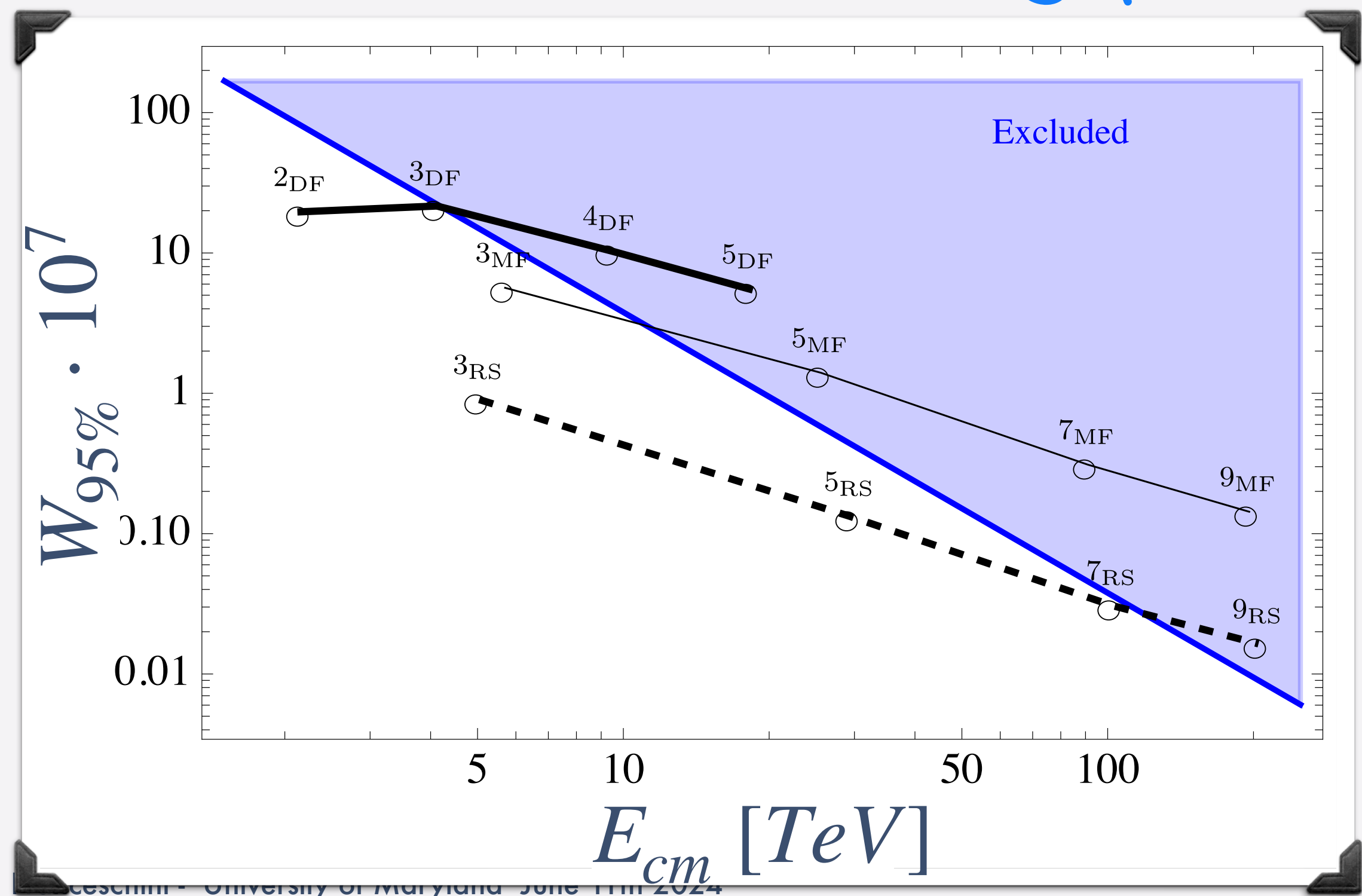
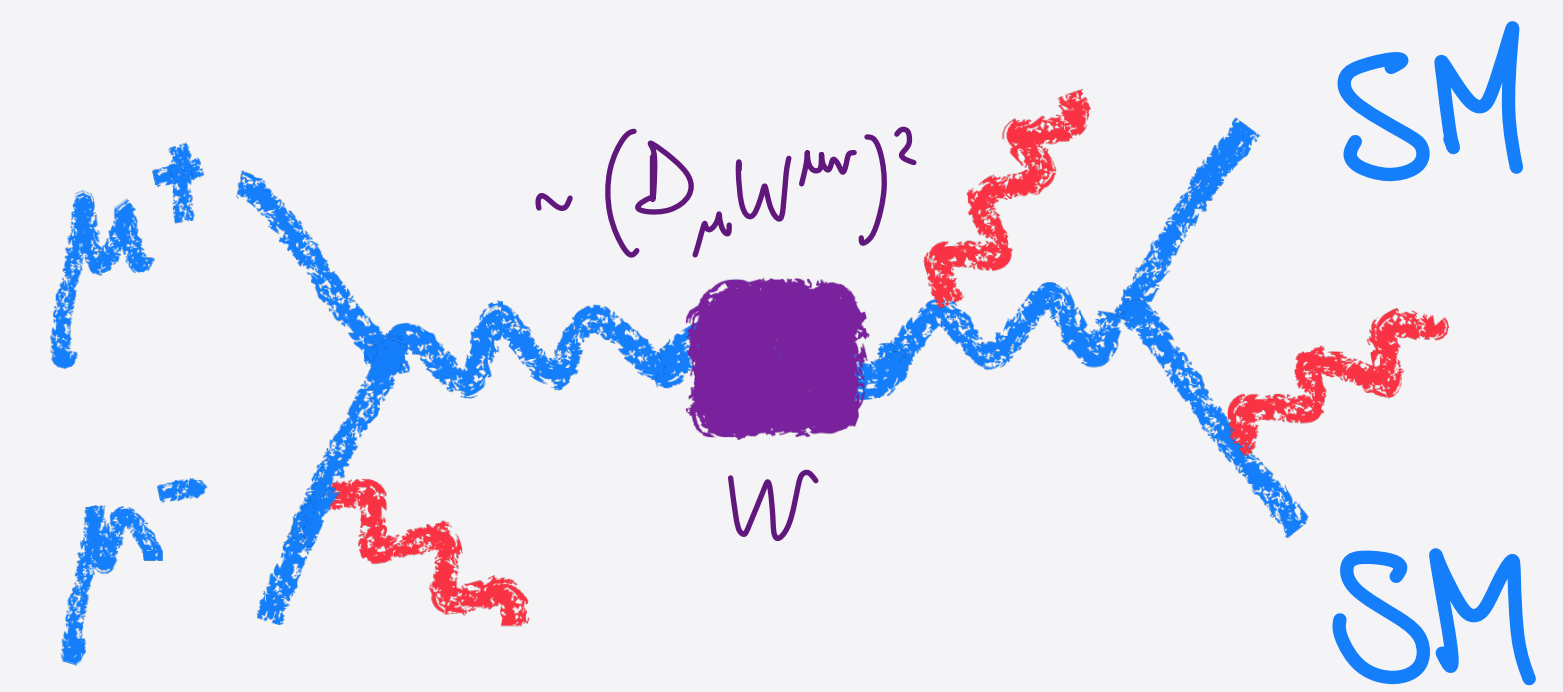
# VIRTUAL\* PRODUCTION

$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



## 2040s

up to 10+ TeV



$\ell^+ \ell^-$  10+ TeV 10+  $ab^{-1}$   
 $\ell^+ \ell^-$  10 TeV 10  $ab^{-1}$   
 $pp$  100 TeV 30  $ab^{-1}$

SUSY WINO

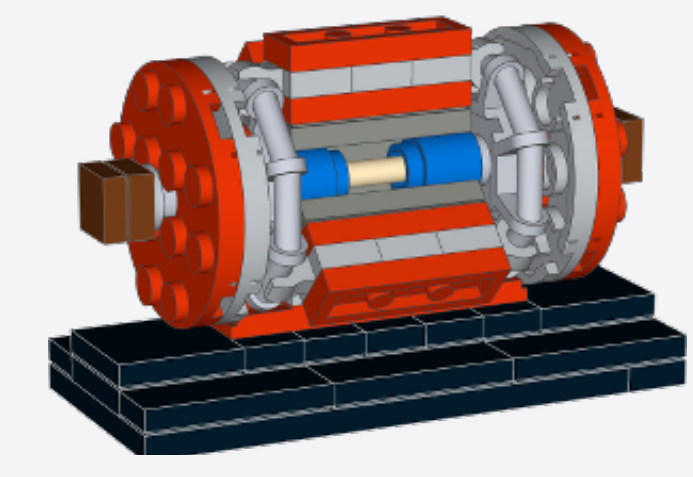
SUSY HIGGSINO

"WIMP" Dark Matter



# VIRTUAL\* PRODUCTION

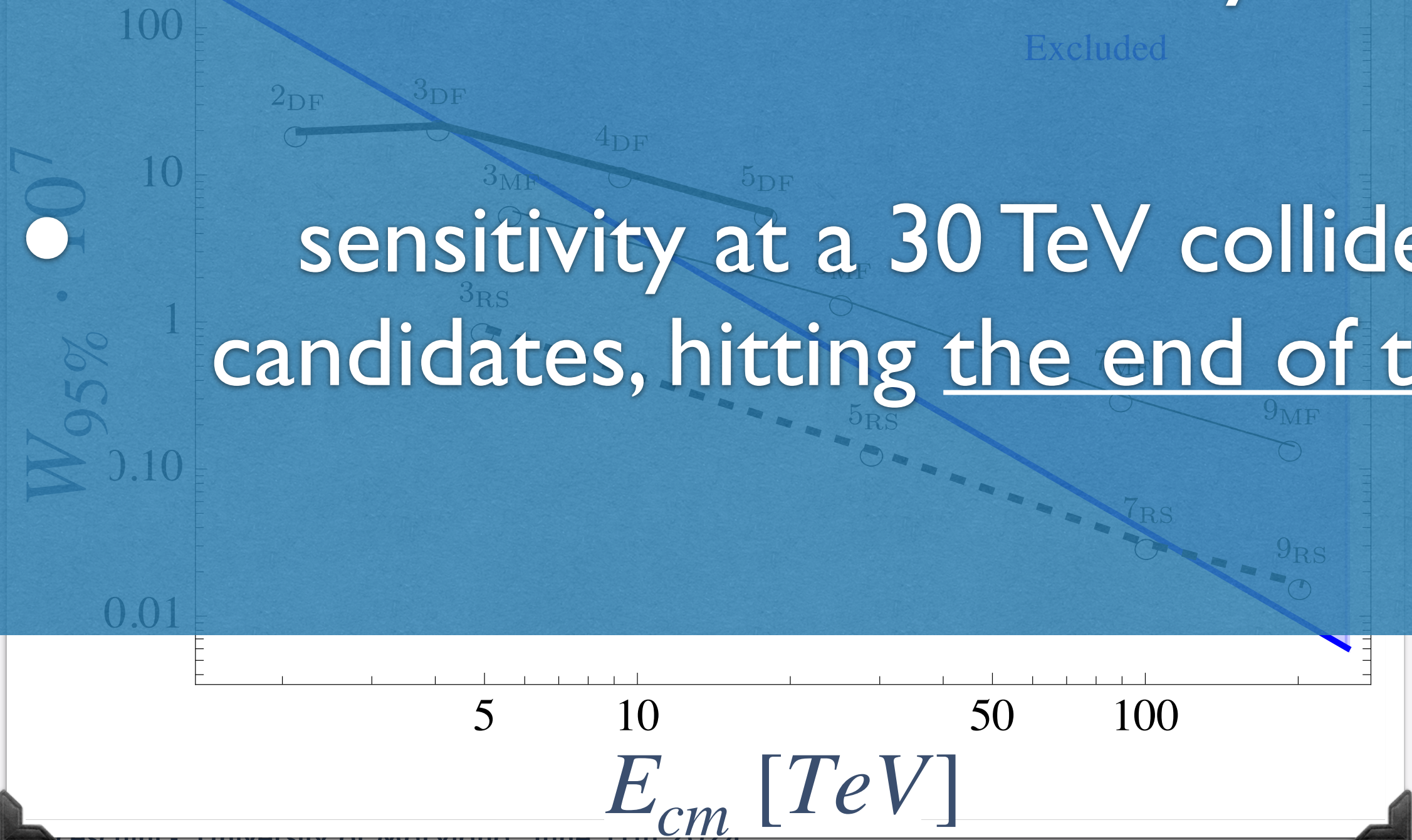
$$\mu^+ \mu^- \rightarrow f\bar{f}, Zh, W^+W^-, Wff'$$



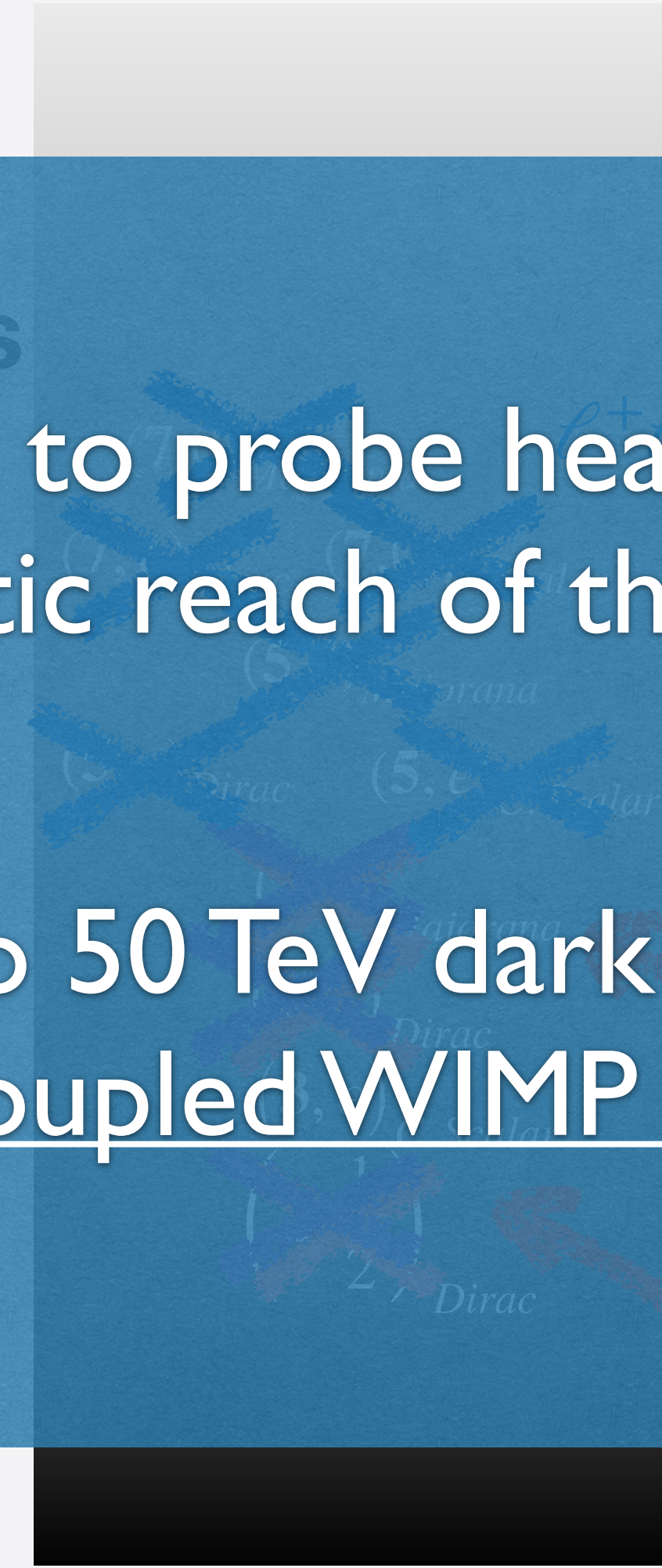
# 2040s

up to 10+ TeV

- muon collider provides a systematic way to probe heavy dark matter candidates even beyond the kinematic reach of the machine



- sensitivity at a 30 TeV collider extends to 50 TeV dark matter candidates, hitting the end of the weakly coupled WIMP catalog(!)



“WIMP” Dark Matter

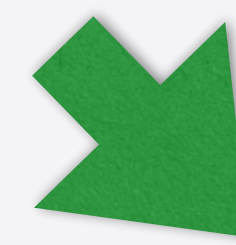
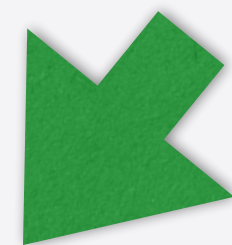
SUSY  
HIGGSINO



# CONCLUSIONS AND OUTLOOK

WIMP dark matter can be challengingly heavy for production at colliders ... still

- We can look for WIMPs in the sky
  - Establishing clear signals from the sky may prove quite hard, due to backgrounds, but are certainly intriguing
  - Signal rates are also subject to uncertainties that can make WIMPs not accessible
- We can try to detect WIMPs from the big-bang
  - Underground ultra-low background experiments can give signals soon, but cannot measure the mass of the WIMP
  - Half or so of the WIMP candidates are easily below the sensitivity of the next generations of Direct Detection experiments



Signals from the sky and from underground laboratories in the next 10-20 years can be a huge motivation for a new collider

Even in absence of signals from the sky and from underground laboratories in the next 10-20 years there is plenty of room left for WIMPs of the most simple kind

Muon collider can probe it all, up to the perturbative unitarity limit

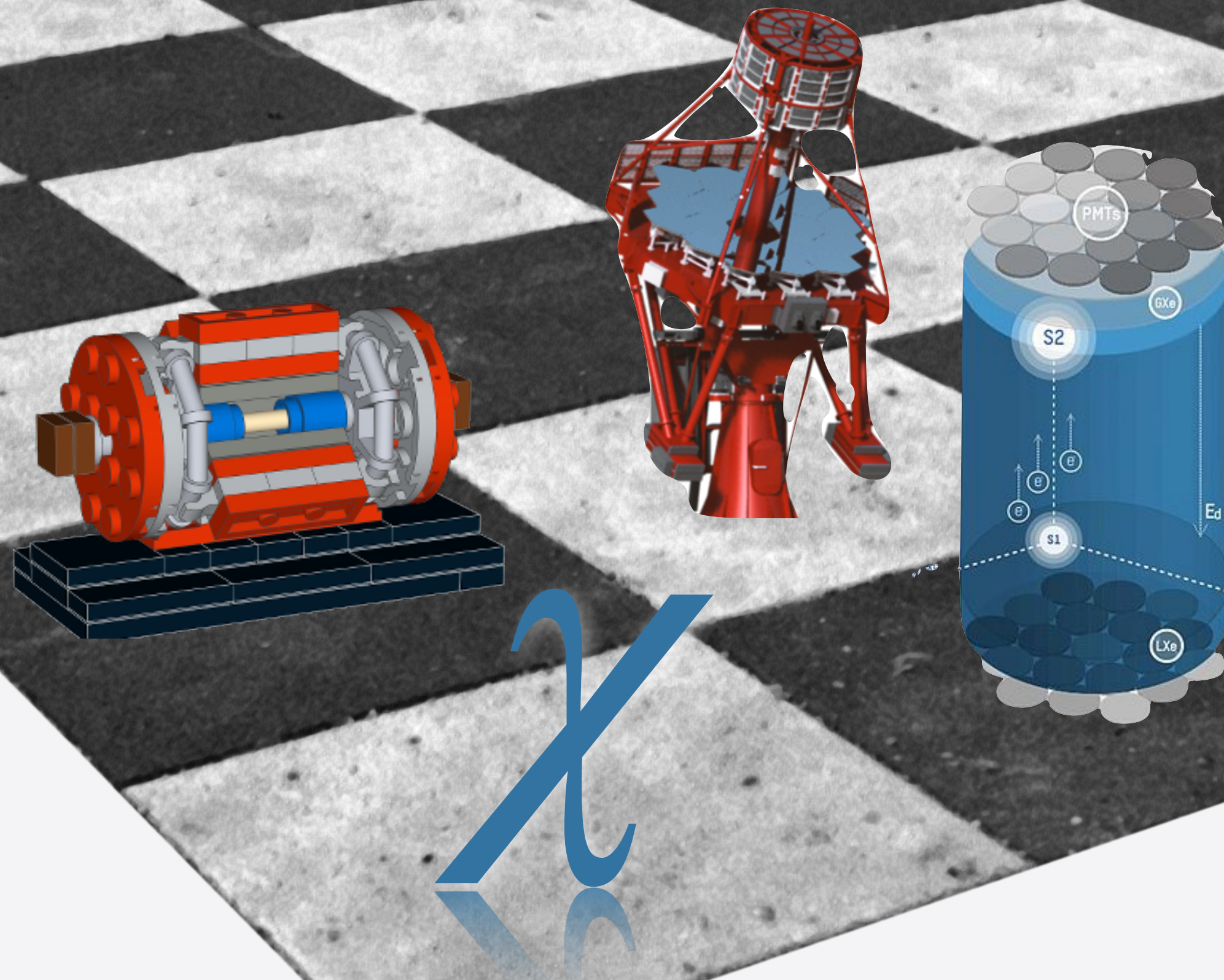


# WIMP DARK MATTER ENDGAME

The 3-10 TeV muon collider can discover Higgsino, Wino and light minimal dark matter ( $n=2,3,4$ ) up to their thermal mass for 100% of  $\Omega_{DM}$

$E_{cm} > 10$  TeV is conceivable thanks to the muon beams. Heavier MDM candidates ( $n=5,7$ ) up to their thermal mass for 100% of  $\Omega_{DM}$  are in reach

In conjunction with direct and indirect detection experiments we have a path forward for the complete and definitive exploration of the idea of WIMPs as Dark Matter





Thank you!



- The scale of large(ish) weak representations of WIMP Dark Matter points towards 10s of TeV
- For EWSB dynamics “10 TeV is the new 1 TeV” given that LHC seems to not find supersymmetric tops, or supersymmetric Higgs or gauge bosons, or top-like new vector-like fermions,  $VV$  resonances or anything like that ...
- **Question: Can we accommodate 10 TeV Dark Matter in models of 10 TeV EWSB dynamics such as “split” Composite Higgs models?**
  - What is the consequence of this marriage?
- Taking it from another perspective: In Composite Higgs Dark Matter is obtained as a *singlet* pNGB  $\eta$  which has the notable feature to be stable due to a parity that is part of the unbroken symmetries of  $SO(6) \rightarrow SO(5) \rightarrow SO(4)$ . Can we do DM with electroweak charges? Are there other stabilization mechanisms available?

# Variants of Partial Compositeness, embedding of matter, $g_{zb}$

model		$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)_X$	
doublet	$Q$	<b>3</b>	<b>2</b>	<b>1</b>	$\frac{1}{6}$	$Q \equiv q$
	$R$	<b>3</b>	<b>1</b>	<b>2</b>	$\frac{1}{6}$	$R \equiv u, d$
triplet	$L$	<b>3</b>	<b>2</b>	<b>2</b>	$\frac{2}{3}$	$L \supset q + \text{stuff}$
	$R$	<b>3</b>	<b>1</b>	<b>3</b>	$\frac{2}{3}$	$R \supset u, d + \text{stuff}$
	$R'$	<b>3</b>	<b>3</b>	<b>1</b>	$\frac{2}{3}$	$R' \equiv \text{stuff}$
bidoublet	$L_U$	<b>3</b>	<b>2</b>	<b>2</b>	$\frac{2}{3}$	$L_U \supset q + \text{stuff}$
	$L_D$	<b>3</b>	<b>2</b>	<b>2</b>	$-\frac{1}{3}$	$L_D \supset q + \text{stuff}$
	$U$	<b>3</b>	<b>1</b>	<b>1</b>	$\frac{2}{3}$	$U \equiv u$
	$D$	<b>3</b>	<b>1</b>	<b>1</b>	$-\frac{1}{3}$	$D \equiv d$

$$\mathcal{L}_{PC}^{\text{bidoublet}} = \lambda_q q L_U + \lambda'_q q L_D + \lambda_u u U + \lambda_d d D$$

model		$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)_X$
bidoublet	$L_U$	<b>3</b>	<b>2</b>	<b>2</b>	$\frac{2}{3}$
	$L_D$	<b>3</b>	<b>2</b>	<b>2</b>	$-\frac{1}{3}$
	$U$	<b>3</b>	<b>1</b>	<b>1</b>	$\frac{2}{3}$
	$D$	<b>3</b>	<b>1</b>	<b>1</b>	$-\frac{1}{3}$

$U(1)_X$  broken by  $y_t \cdot y_b \propto \lambda'_q \lambda_q \lambda_u \lambda_d$

model		$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)_X$
triplet	$L$	<b>3</b>	<b>2</b>	<b>2</b>	$\frac{2}{3}$
	$R$	<b>3</b>	<b>1</b>	<b>3</b>	$\frac{2}{3}$
	$R'$	<b>3</b>	<b>3</b>	<b>1</b>	$\frac{2}{3}$
	$K$	<b>1</b>	<b>2</b>	<b>2</b>	$-1$
	$E$	<b>1</b>	<b>1</b>	<b>1</b>	$-1$

$$\mathcal{L}_{PC}^{\text{triplet}} = \lambda_q q L + \lambda_u u U + \lambda_d d D + \lambda_\ell \ell K + \lambda_e e E$$

quarks :  $10_{2/3} \rightarrow (3,1) + (1,3) + (2,2)$

leptons :  $5_{-1} \rightarrow (2,2) + (1,1)$

$\chi \supset \text{WIMP} + \text{stuff}_\chi$

$usp_4 \supset su_2 \oplus su_2(\mathbb{R})$
1 = (1, 1)
4 = (2, 1) $\oplus$ (1, 2)
5 = (2, 2) $\oplus$ (1, 1)
10 = (3, 1) $\oplus$ (2, 2) $\oplus$ (1, 3)
14 = (3, 3) $\oplus$ (2, 2) $\oplus$ (1, 1)
16 = (3, 2) $\oplus$ (2, 3) $\oplus$ (2, 1) $\oplus$ (1, 2)
20 = (4, 1) $\oplus$ (3, 2) $\oplus$ (2, 3) $\oplus$ (1, 4)
30 = (4, 4) $\oplus$ (3, 3) $\oplus$ (2, 2) $\oplus$ (1, 1)
35 = (4, 2) $\oplus$ (3, 3) $\oplus$ (3, 1) $\oplus$ (2, 4) $\oplus$ (2, 2) $\oplus$ (1, 3)
35' = (5, 1) $\oplus$ (4, 2) $\oplus$ (3, 3) $\oplus$ (2, 4) $\oplus$ (1, 5)
40 = (4, 3) $\oplus$ (3, 4) $\oplus$ (3, 2) $\oplus$ (2, 3) $\oplus$ (2, 1) $\oplus$ (1, 2)
55 = (5, 5) $\oplus$ (4, 4) $\oplus$ (3, 3) $\oplus$ (2, 2) $\oplus$ (1, 1)
56 = (6, 1) $\oplus$ (5, 2) $\oplus$ (4, 3) $\oplus$ (3, 4) $\oplus$ (2, 5) $\oplus$ (1, 6)
64 = (5, 2) $\oplus$ (4, 3) $\oplus$ (4, 1) $\oplus$ (3, 4) $\oplus$ (3, 2) $\oplus$ (2, 5) $\oplus$ (2, 3) $\oplus$ (1, 4)



# Variants of Partial Compositeness, embedding of matter, $g_{Zbb}$

model		$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)_X$	
doublet	$Q$	3	2	1	$\frac{1}{6}$	$Q \equiv q$
	$R$	3	1	2	$\frac{1}{6}$	$R \equiv u, d$
triplet	$L$	3	2	2	$\frac{2}{3}$	$L \supset q + \text{stuff}$
	$R$	3	1	3	$\frac{2}{3}$	$R \supset u, d + \text{stuff}$
	$R'$	3	3	1	$\frac{2}{3}$	$R' \equiv \text{stuff}$
bidoublet	$L_U$	3	2	2	$\frac{2}{3}$	$L_U \supset q + \text{stuff}$
	$L_D$	3	2	2	$-\frac{1}{3}$	$L_D \supset q + \text{stuff}$
	$U$	3	1	1	$\frac{2}{3}$	$U \equiv u$
	$D$	3	1	1	$-\frac{1}{3}$	$D \equiv d$

model		$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)_X$
triplet	$L$	3	2	2	$\frac{2}{3}$
	$R$	3	1	3	$\frac{2}{3}$
	$R'$	3	3	1	$\frac{2}{3}$
	$K$	1	2	2	-1
	$E$	1	1	1	-1

$$\mathcal{L}_{PC}^{\text{triplet}} = \lambda_q qL + \lambda_u uU + \lambda_d dD + \lambda_\ell \ell K + \lambda_e eE$$

quarks :  $10_{2/3} \rightarrow (3,1) + (1,3) + (2,2)$

leptons :  $5_{-1} \rightarrow (2,2) + (1,1)$

~~$$\mathcal{L}_{PC}^{\text{bidoublet}} = \lambda_q qL_U + \lambda'_q qL_D + \lambda_u uU + \lambda_d dD$$~~

~~| model     |       | $SU(3)_c$ | $SU(2)_L$ | $SU(2)_R$ | $U(1)_X$       |
|-----------|-------|-----------|-----------|-----------|----------------|
| bidoublet | $L_U$ | 3         | 2         | 2         | $\frac{2}{3}$  |
|           | $L_D$ | 3         | 2         | 2         | $-\frac{1}{3}$ |
|           | $U$   | 3         | 1         | 1         | $\frac{2}{3}$  |
|           | $D$   | 3         | 1         | 1         | $-\frac{1}{3}$ |~~
~~$$U(1)_X \text{ broken by } y_t \cdot y_b \propto \lambda'_q \lambda_q \lambda_u \lambda_d$$~~

in reality it is broken to  $\mathbb{Z}_3$

$\chi \supset \text{WIMP} + \text{stuff}_\chi$

$usp_4 \supset su_2 \oplus su_2(\mathbb{R})$

1	=	(1, 1)
4	=	(2, 1) $\oplus$ (1, 2)
5	=	(2, 2) $\oplus$ (1, 1)
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35'	=	(5, 1) $\oplus$ (4, 2) $\oplus$ (3, 3) $\oplus$ (2, 4) $\oplus$ (1, 5)
40	=	(4, 3) $\oplus$ (3, 4) $\oplus$ (3, 2) $\oplus$ (2, 3) $\oplus$ (2, 1) $\oplus$ (1, 2)
55	=	(5, 5) $\oplus$ (4, 4) $\oplus$ (3, 3) $\oplus$ (2, 2) $\oplus$ (1, 1)
56	=	(6, 1) $\oplus$ (5, 2) $\oplus$ (4, 3) $\oplus$ (3, 4) $\oplus$ (2, 5) $\oplus$ (1, 6)
64	=	(5, 2) $\oplus$ (4, 3) $\oplus$ (4, 1) $\oplus$ (3, 4) $\oplus$ (3, 2) $\oplus$ (2, 5) $\oplus$ (2, 3) $\oplus$ (1, 4)

# Variants of Partial Compositeness, embedding of matter, $g_{Zbb}$

unbroken  $U(1)_X$

model		$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)_X$	
doublet	$Q$	3	2	1	$\frac{1}{6}$	$Q \equiv q$
	$R$	3	1	2	$\frac{1}{6}$	$R \equiv u, d$
triplet	$L$	3	2	2	$\frac{2}{3}$	$L \supset q + \text{stuff}$
	$R$	3	1	3	$\frac{2}{3}$	$R \supset u, d + \text{stuff}$
	$R'$	3	3	1	$\frac{2}{3}$	$R' \equiv \text{stuff}$
bidoublet	$L_U$	3	2	2	$\frac{2}{3}$	$L_U \supset q + \text{stuff}$
	$L_D$	3	2	2	$-\frac{1}{3}$	$L_D \supset q + \text{stuff}$
	$U$	3	1	1	$\frac{2}{3}$	$U \equiv u$
	$D$	3	1	1	$-\frac{1}{3}$	$D \equiv d$

triplet	$L$	3	2	2	$\frac{2}{3}$
	$R$	3	1	3	$\frac{2}{3}$
	$R'$	3	3	1	$\frac{2}{3}$
	$K$	1	2	2	-1
	$E$	1	1	1	-1

$$\mathcal{L}_{PC}^{\text{triplet}} = \lambda_q qL + \lambda_u uU + \lambda_d dD + \lambda_\ell \ell K + \lambda_e eE$$

quarks :  $10_{2/3} \rightarrow (3,1) + (1,3) + (2,2)$   
 leptons :  $5_{-1} \rightarrow (2,2) + (1,1)$

~~$\mathcal{L}_{PC}^{\text{bidoublet}} = \lambda_q qL_U + \lambda'_q qL_D + \lambda_u uU + \lambda_d dD$~~

model		$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)_X$
bidoublet	$L_U$	3	2	2	$\frac{2}{3}$
	$L_D$	3	2	2	$-\frac{1}{3}$
	$U$	3	1	1	$\frac{2}{3}$
	$D$	3	1	1	$-\frac{1}{3}$

~~$U(1)_X$  broken by  $y_t \cdot y_b \propto \lambda'_q \lambda_q \lambda_u \lambda_d$~~

in reality it is broken to  $\mathbb{Z}_3$

$\chi \supset \text{WIMP} + \text{stuff}_\chi$

$usp_4 \supset su_2 \oplus su_2(\mathbb{R})$
1 = (1, 1)
4 = (2, 1) $\oplus$ (1, 2)
5 = (2, 2) $\oplus$ (1, 1)
10 = (3, 1) $\oplus$ (2, 2) $\oplus$ (1, 3)
14 = (3, 3) $\oplus$ (2, 2) $\oplus$ (1, 1)
16 = (3, 2) $\oplus$ (2, 3) $\oplus$ (2, 1) $\oplus$ (1, 2)
20 = (4, 1) $\oplus$ (3, 2) $\oplus$ (2, 3) $\oplus$ (1, 4)
30 = (4, 4) $\oplus$ (3, 3) $\oplus$ (2, 2) $\oplus$ (1, 1)
35 = (4, 2) $\oplus$ (3, 3) $\oplus$ (3, 1) $\oplus$ (2, 4) $\oplus$ (2, 2) $\oplus$ (1, 3)
35' = (5, 1) $\oplus$ (4, 2) $\oplus$ (3, 3) $\oplus$ (2, 4) $\oplus$ (1, 5)
40 = (4, 3) $\oplus$ (3, 4) $\oplus$ (3, 2) $\oplus$ (2, 3) $\oplus$ (2, 1) $\oplus$ (1, 2)
55 = (5, 5) $\oplus$ (4, 4) $\oplus$ (3, 3) $\oplus$ (2, 2) $\oplus$ (1, 1)
56 = (6, 1) $\oplus$ (5, 2) $\oplus$ (4, 3) $\oplus$ (3, 4) $\oplus$ (2, 5) $\oplus$ (1, 6)
64 = (5, 2) $\oplus$ (4, 3) $\oplus$ (4, 1) $\oplus$ (3, 4) $\oplus$ (3, 2) $\oplus$ (2, 5) $\oplus$ (2, 3) $\oplus$ (1, 4)

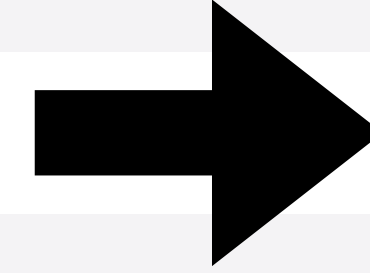


# Adding Dark Matter to the picture (as matter, no pNGB)

$$X \supset \chi + \text{stuff}_\chi$$

$$\mathbf{10}_{SO(5)} = \mathbf{(3, 1)}_{SO(4)} \oplus \mathbf{(2, 2)}_{SO(4)} \oplus \mathbf{(1, 3)}_{SO(4)} \quad 10_X \rightarrow (3, 1)_X$$

for a state with  $Y = T_{3R} + X = 0$  to be comprised in  $(3, 1)_X$  the value of  $X$  has to be 0



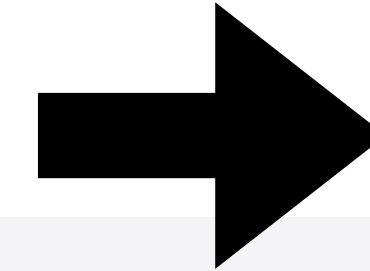
$X = 0$  does not help to stabilize the DM, **DM is unstable** under  $X$

$$\mathbf{16} = \mathbf{(3, 2)} \oplus \mathbf{(2, 3)} \oplus \mathbf{(2, 1)} \oplus \mathbf{(1, 2)}$$

$$\mathbf{20} = \mathbf{(4, 1)} \oplus \mathbf{(3, 2)} \oplus \mathbf{(2, 3)} \oplus \mathbf{(1, 4)}$$

$$16_X \rightarrow (3, 2)_X$$

for a state with  $Y = 0$  to be comprised in  $(3, 2)_X$  the value of  $X$  has to be an integer chosen in  $\pm \frac{1}{2}$



$X = \pm 1/2$  makes the DM **absolutely stable** because it is not a multiple of the other charges (quantized in thirds)

model		$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)_X$
triplet	$L$	<b>3</b>	<b>2</b>	<b>2</b>	$\frac{2}{3}$
	$R$	<b>3</b>	<b>1</b>	<b>3</b>	$\frac{2}{3}$
	$R'$	<b>3</b>	<b>3</b>	<b>1</b>	$\frac{2}{3}$
	$K$	<b>1</b>	<b>2</b>	<b>2</b>	$-1$
	$E$	<b>1</b>	<b>1</b>	<b>1</b>	$-1$

Requiring  $Y = 0$ , as to be compatible with direct detection limits on dark matter, fixes a choice for charge under  $U(1)_X$  that makes DM stable

# Adding Dark Matter to the picture (as matter, no pNGB)

$$X \supset \chi + \text{stuff}_\chi$$

$SO(5)$                        $SO(4)$

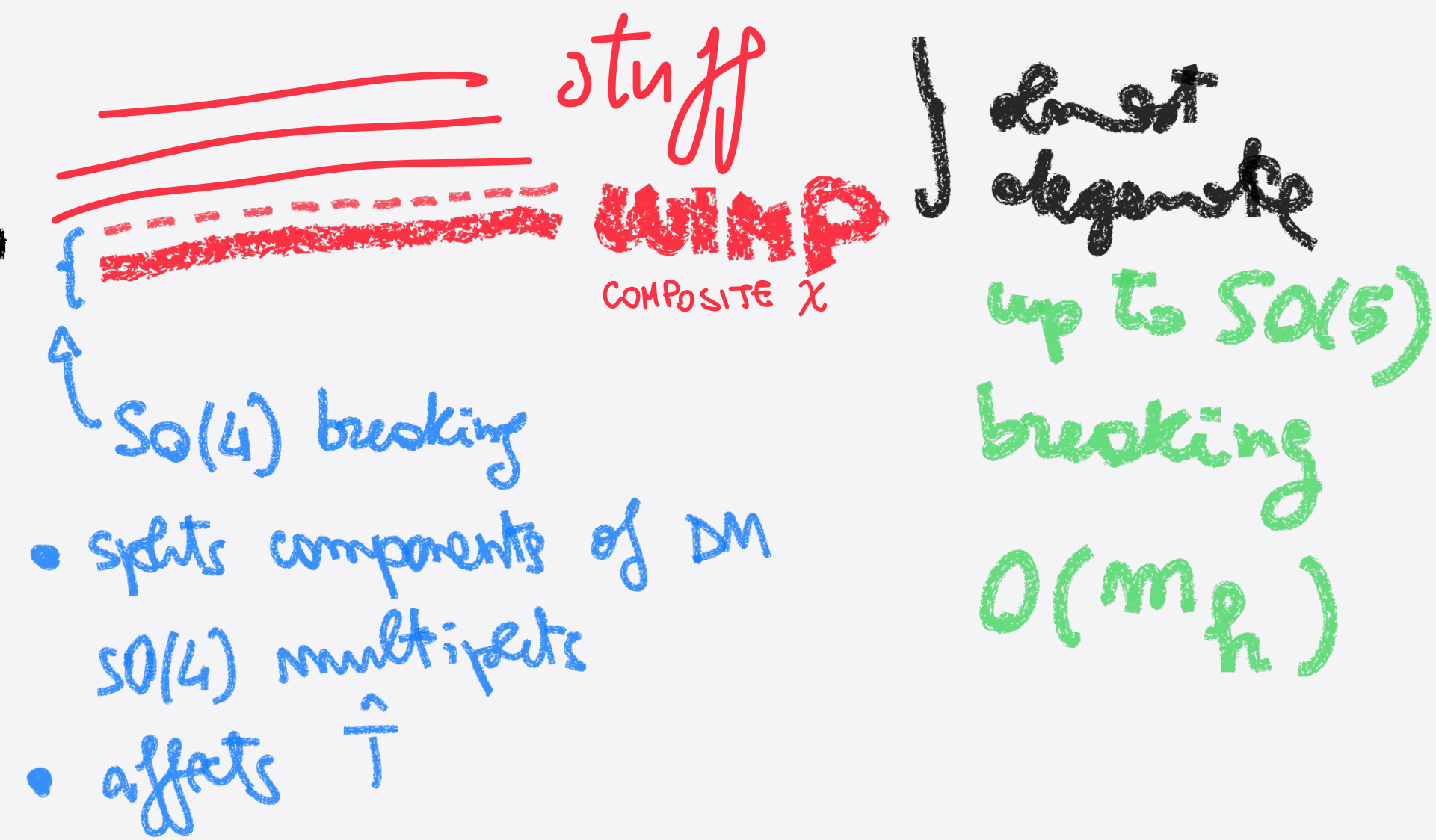
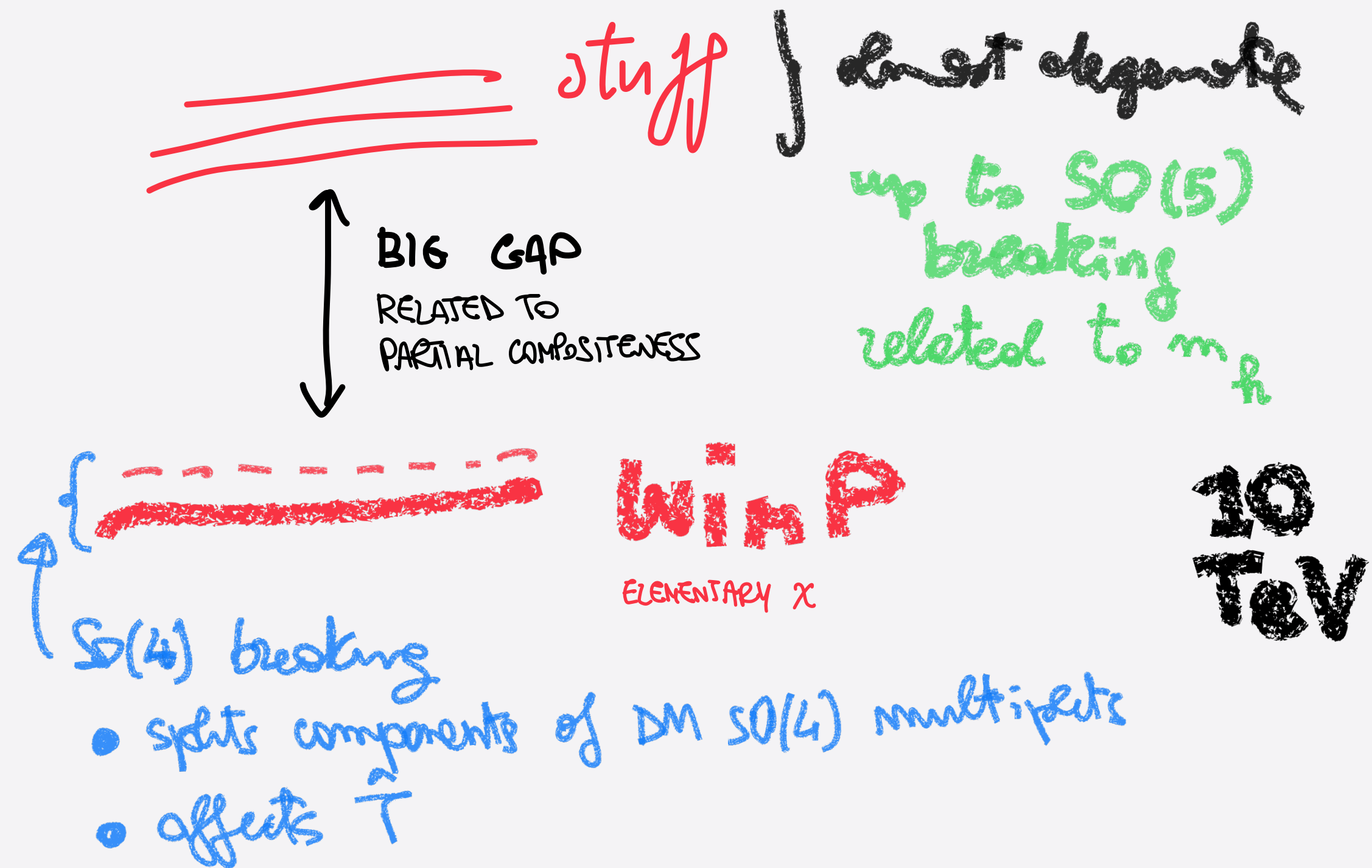
$$16 = (3, 2) \oplus (2, 3) \oplus (2, 1) \oplus (1, 2)$$

$\chi$                        $\rho$                        $\rho'$                        $\rho''$

model		$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)_X$
triplet	$L$	3	2	2	$\frac{2}{3}$
	$R$	3	1	3	$\frac{2}{3}$
	$R'$	3	3	1	$\frac{2}{3}$
	$K$	1	2	2	-1
	$E$	1	1	1	-1

partially composite O(10) TeV DM

fully composite O(10) TeV DM





# Adding Dark Matter to the picture (as matter, no pNGB)

$$X \supset \chi + \text{stuff}_\chi$$

$SO(5)$                        $SO(4)$

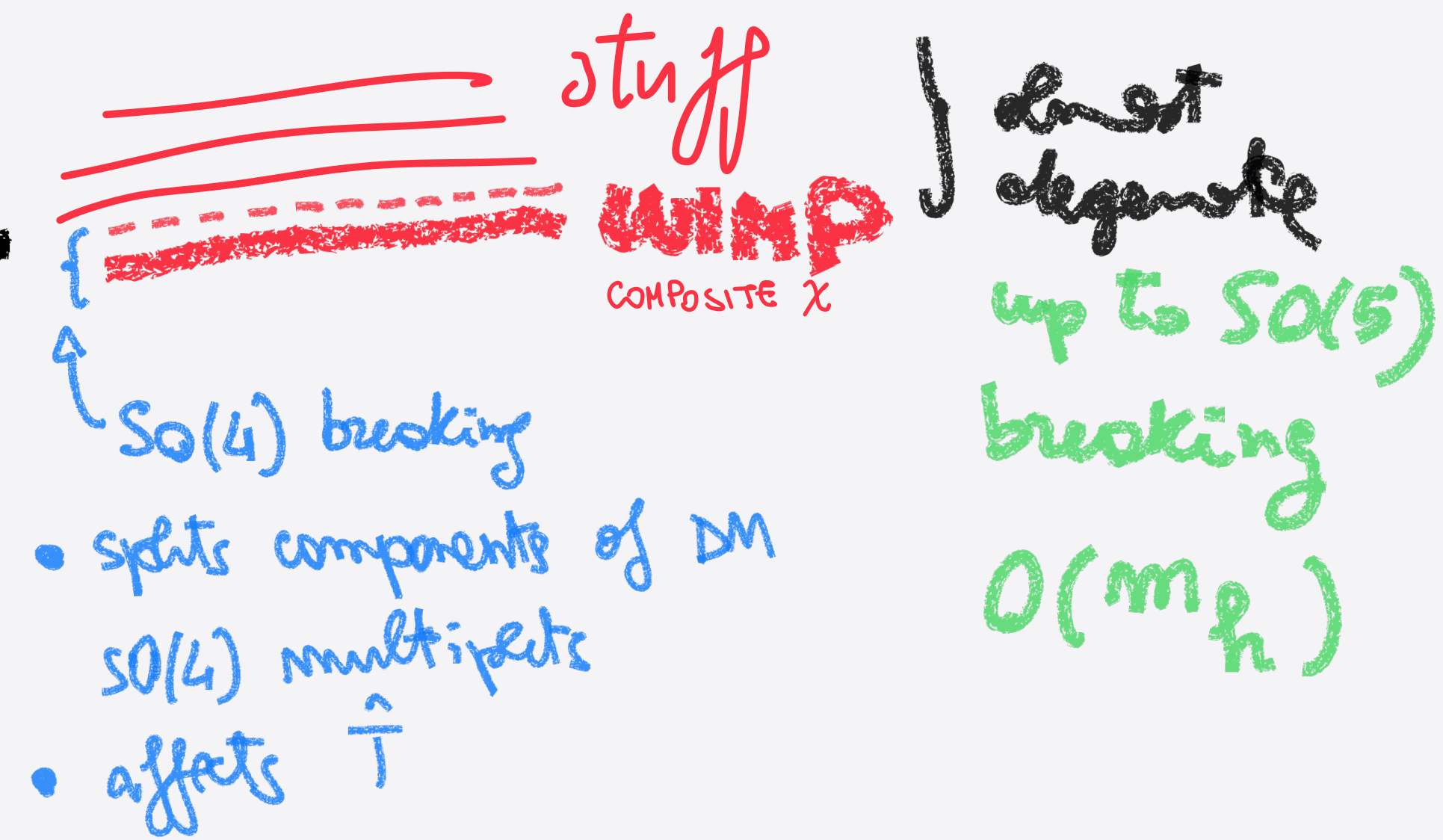
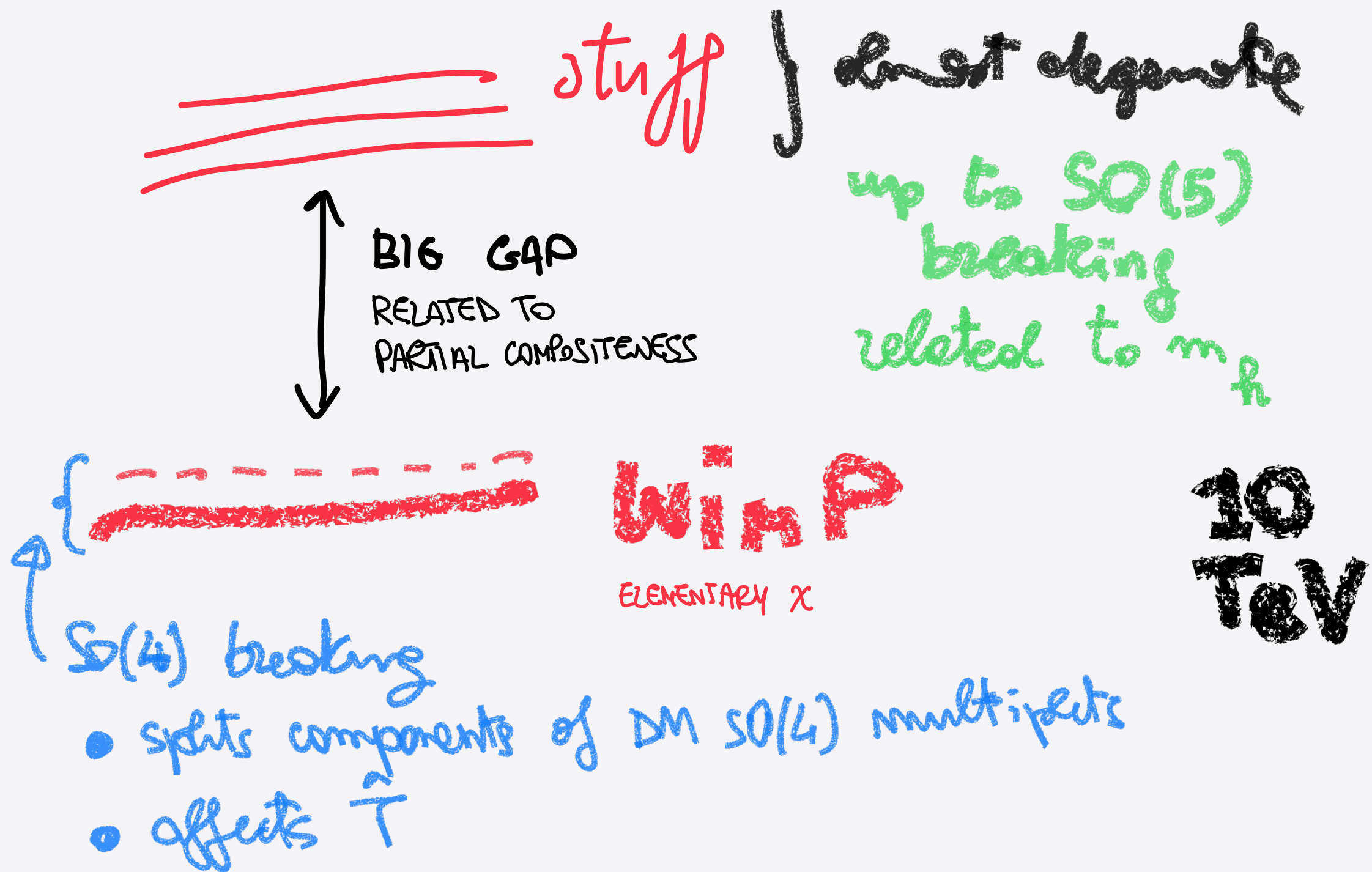
$$16 = (3, 2) \oplus (2, 3) \oplus (2, 1) \oplus (1, 2)$$

$\chi$                        $\rho$                        $\rho'$                        $\rho''$

model		$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)_X$
triplet	$L$	3	2	2	$\frac{2}{3}$
	$R$	3	1	3	$\frac{2}{3}$
	$R'$	3	3	1	$\frac{2}{3}$
	$K$	1	2	2	-1
	$E$	1	1	1	-1

partially composite O(10) TeV DM

fully composite O(10) TeV DM



DM spin	EW n-plet	$M_\chi$ (TeV)	$\Lambda_{\text{Landau}}/M_\chi$	$(\sigma v)_{\text{tot}}^{J=0}/(\sigma v)_{\text{max}}^{J=0}$	$\Delta M_0$ [MeV]	$\Lambda_{\text{UV}}^{\text{max}}(\Delta M_0^{\text{min}})/M_\chi$	$\Delta M_-$ [MeV]
Complex scalar	2	$0.58 \pm 0.01$	$> M_{\text{Pl}}$	-	$0.22 - 4.6 \times 10^4$	-	4.2 - 9600
	4	$4.98 \pm 0.05$	$> M_{\text{Pl}}$	0.004	$0.22 - 10^4$	-	3.2 - 2000
	6	$34.9 \pm 0.5$	$\simeq 6 \times 10^{13}$	0.016	0.54 - 2300	-	280 - 660
	8	$88 \pm 2$	$2 \times 10^4$	0.12	$0.89 - 1.2 \times 10^3$	-	324 - 507
	10	$167 \pm 4$	20	0.45	1.27 - 800	-	340 - 450
Dirac fermion	2	$1.08 \pm 0.01$	$> M_{\text{Pl}}$	-	0.22 - 5000	$2 \times 10^5$	4.8 - 7800
	4	$4.8 \pm 0.1$	$\simeq M_{\text{Pl}}$	0.013	0.21 - 2200	$\times 10^5$	3.6 - 2600
	6	$31.7 \pm 0.5$	$2 \times 10^4$	0.057	0.51 - 510	$\times 10^4$	185 - 780
	8	$82 \pm 2$	14	0.37	0.86 - 800	3000	290 - 550

DM spin	EW n-plet	$M_\chi$ (TeV)	$(\sigma v)_{\text{tot}}^{J=0}/(\sigma v)_{\text{max}}^{J=0}$	$\Lambda_{\text{Landau}}/M_{\text{DM}}$	$\Lambda_{\text{UV}}/M_{\text{DM}}$
Real scalar	3	$2.53 \pm 0.01$	-	$3 \times 10^{37}$	$4 \times 10^{24*}$
	5	$15.4 \pm 0.7$	0.002	$5 \times 10^{36}$	$2 \times 10^{24}$
	7	$54.2 \pm 3.1$	0.022	$2 \times 10^{19}$	$2 \times 10^{24}$
	9	$117.8 \pm 15.4$	0.088	$3 \times 10^3$	$2 \times 10^{24}$
	11	$199 \pm 42$	0.25	20	$3 \times 10^{24}$
	13	$338 \pm 102$	0.6	3.5	$3 \times 10^{24}$
Majorana fermion	3	$2.86 \pm 0.01$	-	$3 \times 10^{37}$	$8 \times 10^{12*}$
	5	$13.6 \pm 0.8$	0.003	$3 \times 10^{17}$	$5 \times 10^{12}$
	7	$48.8 \pm 3.3$	0.019	$1 \times 10^4$	$4 \times 10^7$
	9	$113 \pm 15$	0.07	30	$3 \times 10^7$
	11	$202 \pm 43$	0.2	6	$3 \times 10^7$
	13	$324.6 \pm 94$	0.5	2.6	$3 \times 10^7$

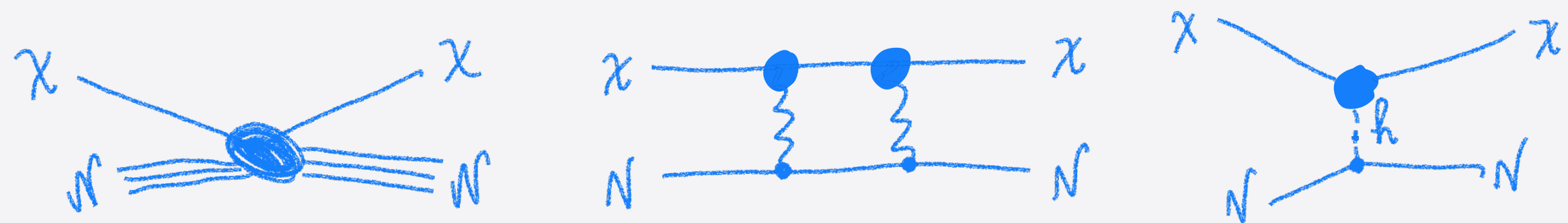
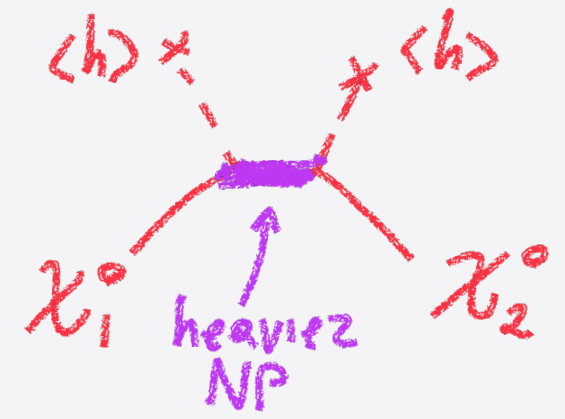


DM spin	$n_Y$	$M_{\text{DM}}$ (TeV)	DM spin	EW n-plet	$M_\chi$ (TeV)	DM spin	$n_\epsilon$	$M_{\text{DM}}$ (TeV)
Dirac fermion	$2_{1/2}$	$1.08 \pm 0.02$	Real scalar	3	$2.53 \pm 0.01$	Complex scalar	3	$1.60 \pm 0.01 - 2.4^*$
	$3_1$	$2.85 \pm 0.14$		5	$15.4 \pm 0.7$		5	$11.3 \pm 0.6$
	$4_{1/2}$	$4.8 \pm 0.3$		7	$54.2 \pm 3.1$		7	$47 \pm 3$
	$5_1$	$9.9 \pm 0.7$		9	$117.8 \pm 15.4$		9	$118 \pm 9$
	$6_{1/2}$	$31.8 \pm 5.2$		11	$199 \pm 42$		11	$217 \pm 17$
	$8_{1/2}$	$82 \pm 8$		13	$338 \pm 102$		13	$352 \pm 30$
	$10_{1/2}$	$158 \pm 12$						
Complex scalar	$2_{1/2}$	$0.58 \pm 0.01$	Majorana fermion	3	$2.86 \pm 0.01$	Dirac fermion	3	$2.0 \pm 0.1 - 2.4^*$
	$3_1$	$2.1 \pm 0.1$		5	$13.6 \pm 0.8$		5	$9.1 \pm 0.5$
	$4_{1/2}$	$4.98 \pm 0.25$		7	$48.8 \pm 3.3$		7	$45 \pm 3$
	$5_1$	$11.5 \pm 0.8$		9	$113 \pm 15$		9	$115 \pm 9$
	$6_{1/2}$	$32.7 \pm 5.3$		11	$202 \pm 43$		11	$211 \pm 16$
	$8_{1/2}$	$84 \pm 8$		13	$324.6 \pm 94$		13	$340 \pm 27$
	$10_{1/2}$	$162 \pm 13$						
	$12_{1/2}$	$263 \pm 22$						



# DIRECT DETECTION

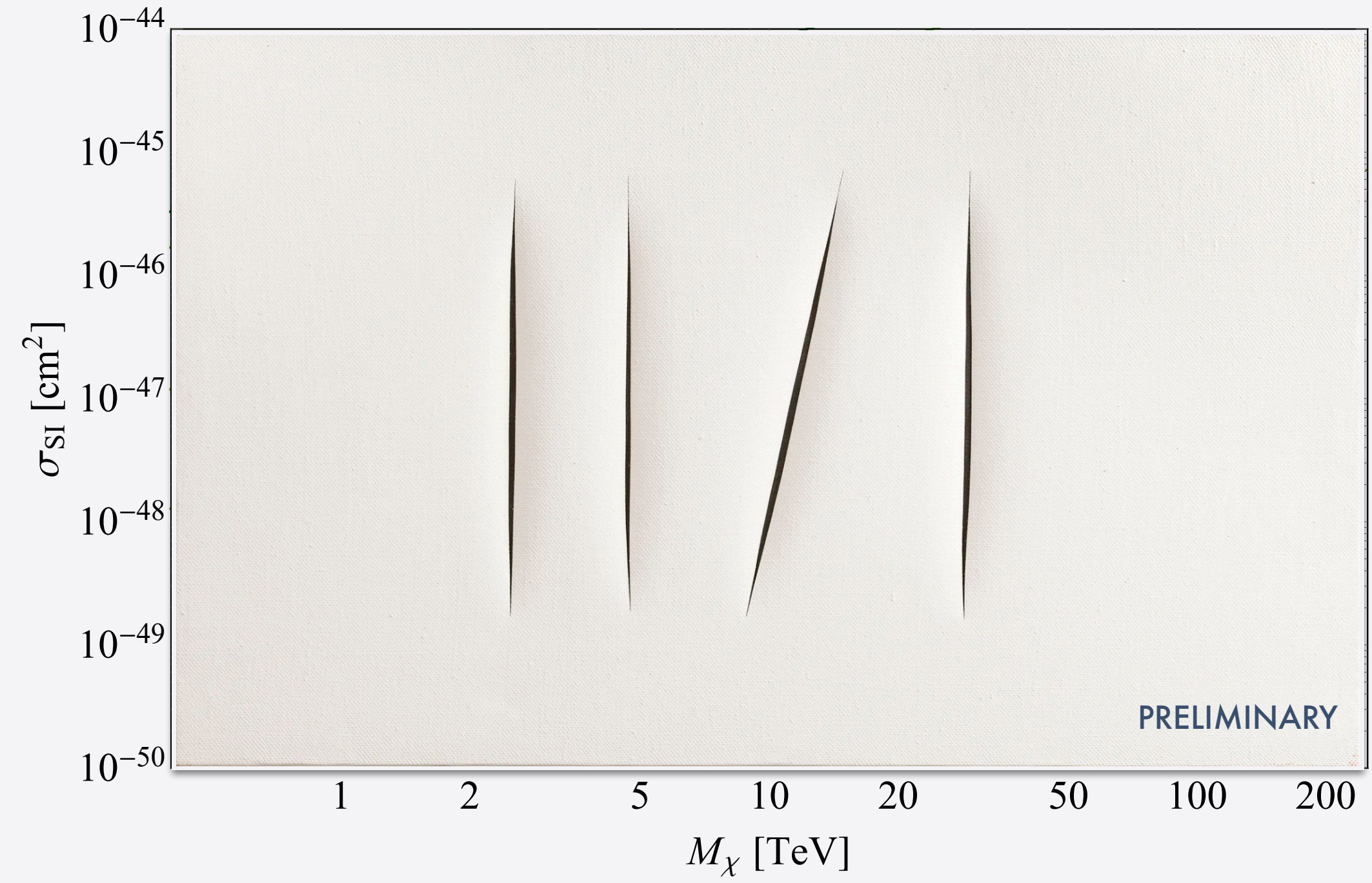
$Y \neq 0$ , Mass-Splitting from DIM>4



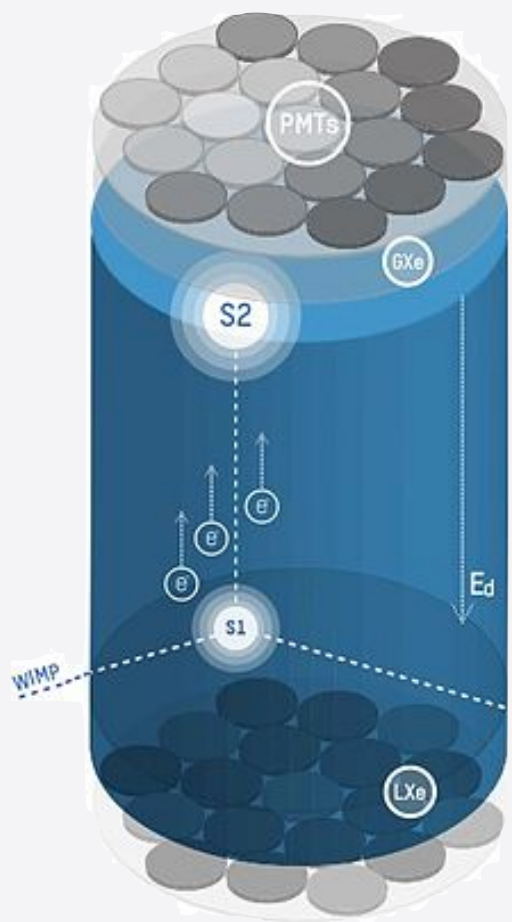
Scattering on SM materials can be detected in ultra-low background experiments

Larger rates for the larger  $n$ -plets keep them visible

For such large DM mass the signature does not depend on the DM mass.



An excess would require a "seasonality" check and maybe independent confirmation (many excesses in the past in this type of experiments, though most were at the lowest accessible masses)



## 2030s

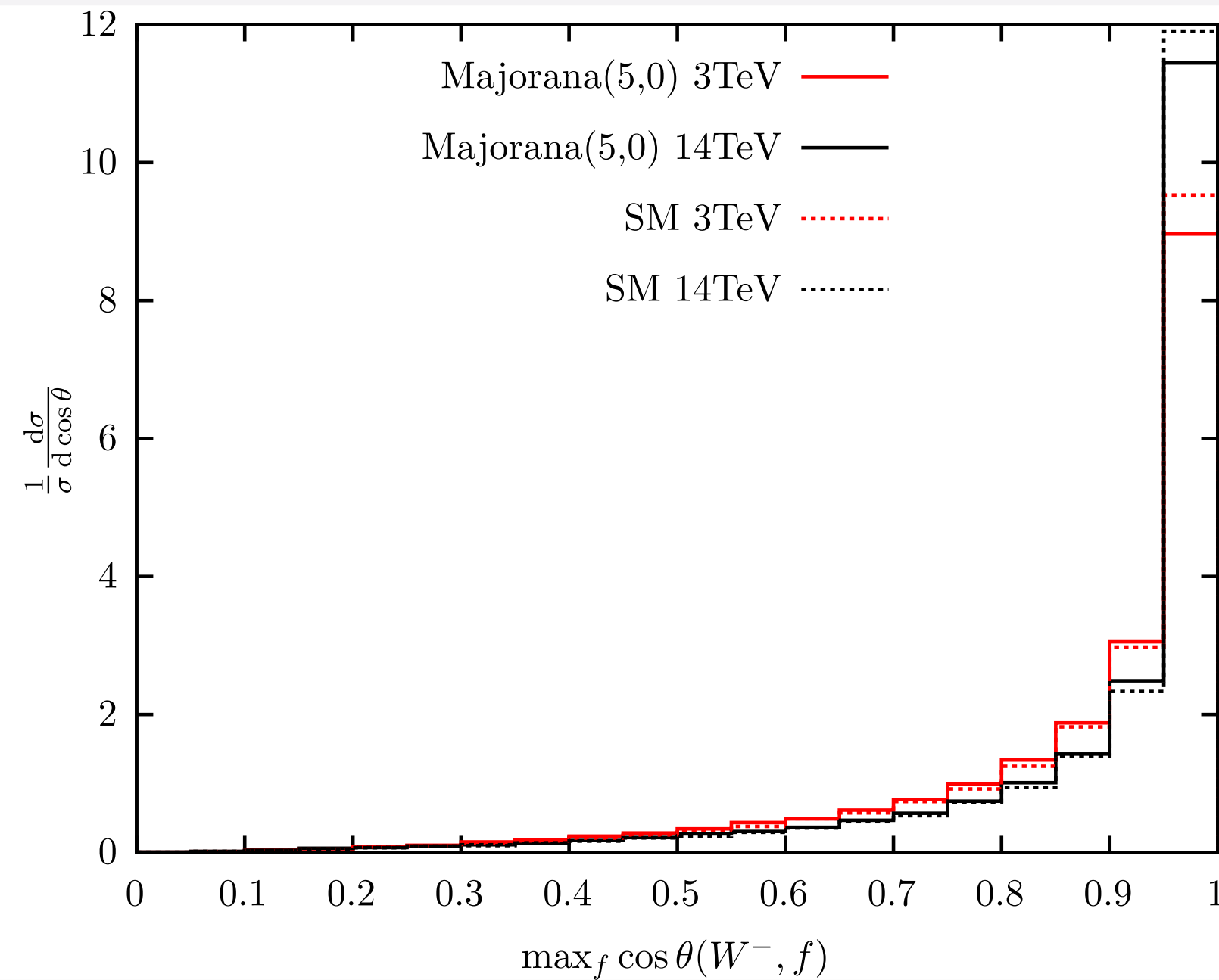
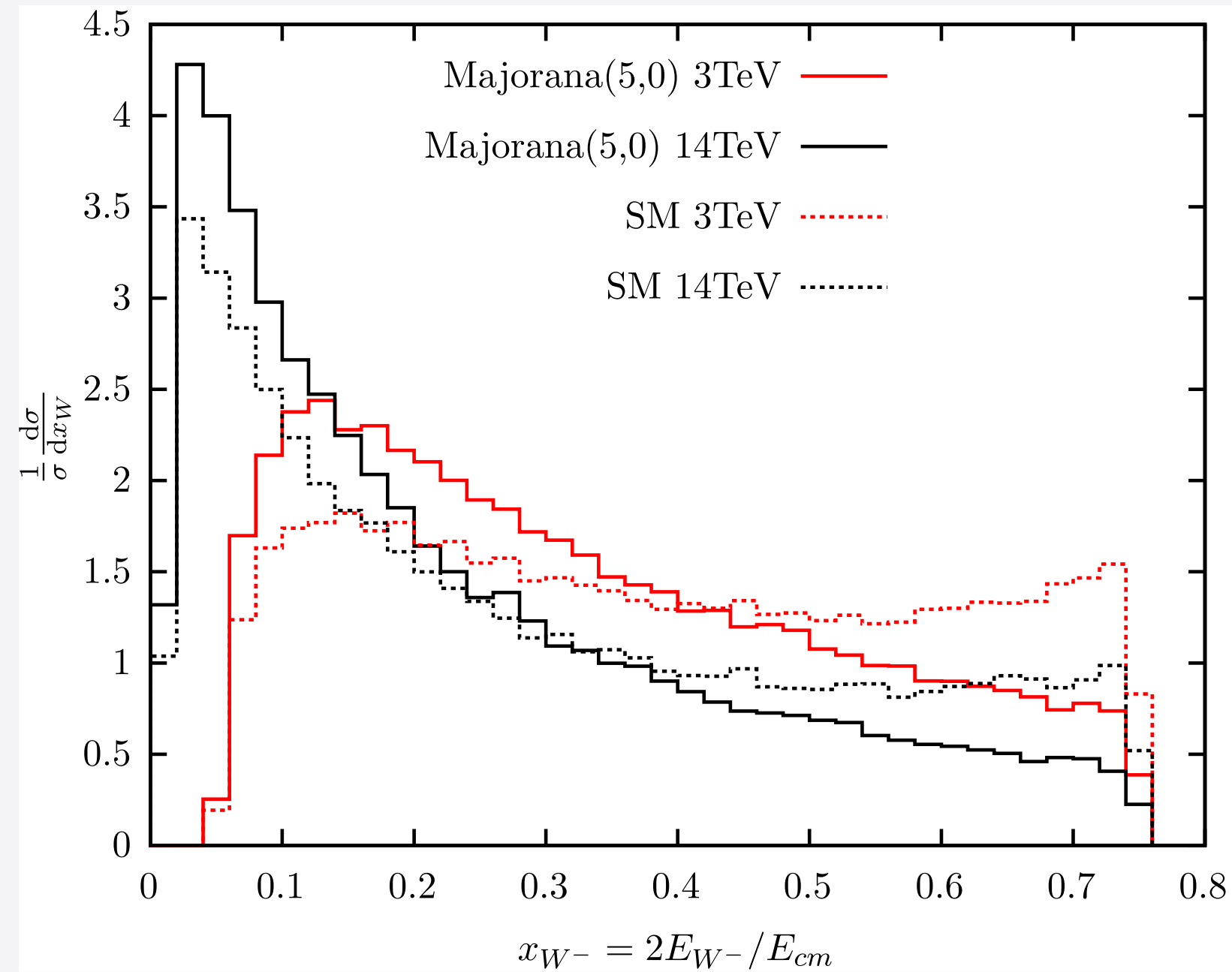
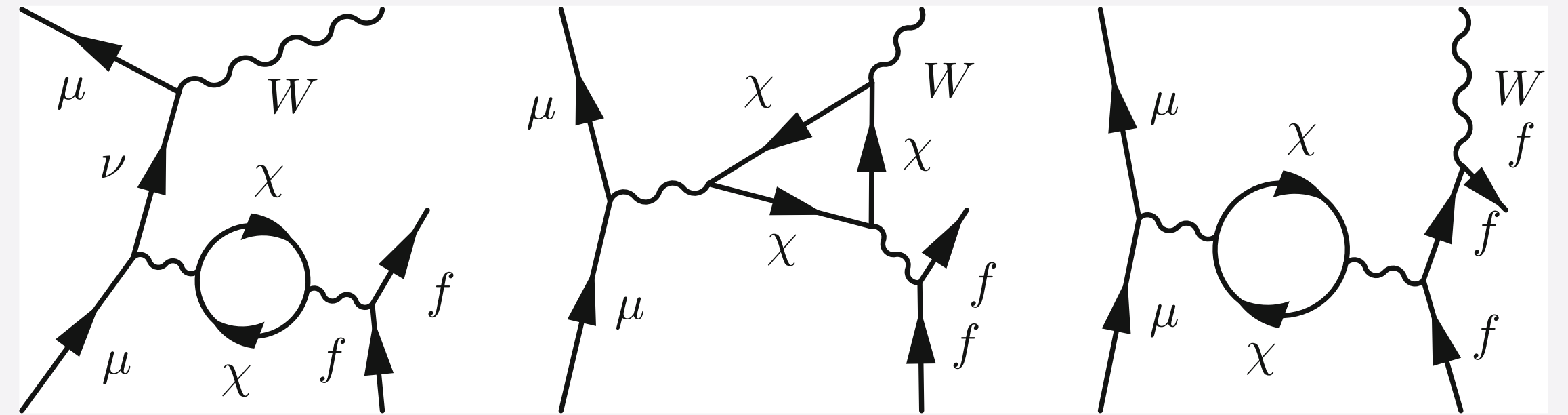
up to  $O(\text{PeV})$



# $Wff'$ PHASE SPACE

$$0.5 \cdot E_{cm} < m(f' \bar{f}) < 0.9 \cdot E_{cm}.$$

$$8^\circ < \theta(W) < 172^\circ,$$



**Fig. 5** Differential distribution of the normalized  $W$  boson energy ( $x_W = 2E_W/E_{cm}$ ) and maximal  $\cos\theta(W, f)$  ( $f = \mu^+, \mu^-, u, \bar{d}$ ) for the  $\mu^+\mu^- \rightarrow W^- u\bar{d}$  in the SM and the interference with a Majorana fermion 5-plet at the 3 TeV and 14 TeV muon collider

# SOFT AND COLLINEAR W

